

According to the decompilation of the Ciso Vigenere hash algorithm, when the password length is less than 16 the idea behind Ciso Vigenere hash algorithm is:

Let  $p$  be the password that the user types.

Let  $hp$  be the hardcoded password in the code of Packet Tracer.

Let  $lp$  be the length of the user input password.

Let  $h$  be the hash value obtained from the custom algorithm.

So that:

$$\begin{aligned}
& \forall h \forall lp \forall hp [(hp = \\
& (d, s, f, d, :, k, f, o, A, , , , i, y, e, w, r, k, l, d, J, K, D, H, S, U, B, s, g, v, c, a, 6, 9, 8, 3, 4, n, c, x, v), \\
& 0 < lp < 16, \\
& h_0 = 0, \\
& h_1 = 8, \\
& h = \\
& \Sigma_{i=2}^{lp} \begin{cases} ((p_i \oplus hp_{8+i}) \ggg 4) + 0x30, & \text{if } (p_i \oplus hp_{i+8} \wedge 0xfffffffff0 < 0xa0) \text{ and if } i \equiv 0 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \ggg 4) + 0x37, & \text{if } (p_i \oplus hp_{i+8} \wedge 0xfffffffff0 \geq 0xa0) \text{ and if } i \equiv 0 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \wedge 0xf) + 0x30, & \text{if } (p_i \oplus hp_{i+8} \wedge 0xf < 0x0a) \text{ and if } i \equiv 1 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \wedge 0xf) + 0x37, & \text{if } (p_i \oplus hp_{i+8} \wedge 0xf \geq 0x0a) \text{ and if } i \equiv 1 \pmod{2} \end{cases} \\
& ) \implies \#p[p = \mathbf{rev}(h)] \\
& (0)
\end{aligned}$$

So let's split each sub steps of the algorithm. In this wayt, we could start proving that if  $P \implies Q$  and if  $Q \implies R$  then  $P \implies R$

So for any  $P$  so that:

$$h = \Sigma_{i=2}^{lp} \begin{cases} (p_i \oplus hp_{i+8} \wedge 0xfffffffff0 < 0xa0) \text{ if } i \equiv 0 \pmod{2} \\ (p_i \oplus hp_{i+8} \wedge 0xfffffffff0 \geq 0xa0) \text{ if } i \equiv 0 \pmod{2} \\ (p_i \oplus hp_{i+8} \wedge 0xf < 0x0a) \text{ if } i \equiv 1 \pmod{2} \\ (p_i \oplus hp_{i+8} \wedge 0xf \geq 0x0a) \text{ if } i \equiv 1 \pmod{2} \end{cases}$$

$$\begin{array}{l} ) \implies \nexists p[p = \mathbf{rev}(h)] \\ (0) \end{array}$$

So for any Q so that:

$$\begin{array}{l} h = \Sigma_{i=2}^l p \left\{ \begin{array}{l} (p_i \oplus hp_{i+8} \wedge 0xfffffffff0 < 0xa0), \text{ if } i \equiv 0 \pmod{2} \\ (p_i \oplus hp_{i+8} \wedge 0xfffffffff0 \geq 0xa0) \text{ if } i \equiv 0 \pmod{2} \\ (p_i \oplus hp_{i+8} \wedge 0xf < 0x0a), \text{ if } i \equiv 1 \pmod{2} \\ (p_i \oplus hp_{i+8} \wedge 0xf \geq 0x0a), \text{ if } i \equiv 1 \pmod{2} \end{array} \right. \\ ) \implies \forall p[p = \mathbf{rev}(h)] \\ (0) \end{array}$$

Let's start by proving

$$\begin{array}{l} \forall h \forall l p \forall hp [(hp = \\ (d, s, f, d, :, k, f, o, A, :, :, i, y, e, w, r, k, l, d, J, K, D, H, S, U, B, s, g, v, c, a, 6, 9, 8, 3, 4, n, c, x, v), \\ 0 < lp < 16, \\ h_0 = 0, \\ h_1 = 8, \end{array}$$

$$\begin{aligned}
h = & \\
\Sigma_{i=2}^{lp} & \begin{cases} ((p_i \oplus hp_{8+i}) \ggg 4) + 0x30, & \text{if } (p_i \oplus hp_{i+8} \wedge 0xffffffff0 < 0xa0) \text{ and if } i \equiv 0 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \ggg 4) + 0x37, & \text{if } (p_i \oplus hp_{i+8} \wedge 0xffffffff0 \geq 0xa0) \text{ and if } i \equiv 0 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \wedge 0xf) + 0x30, & \text{if } (p_i \oplus hp_{i+8} \wedge 0xf < 0xa) \text{ and if } i \equiv 1 \pmod{2} \\ ((p_i \oplus hp_{8+i}) \wedge 0xf) + 0x37, & \text{if } (p_i \oplus hp_{i+8} \wedge 0xf \geq 0xa) \text{ and if } i \equiv 1 \pmod{2} \end{cases} \\
) \implies & \#p[p = \mathbf{rev}(h)] \\
(0) &
\end{aligned}$$

I/ substraction to reverse the addition

$\forall x[(x = y + z) \implies (y = ez)]$  then it follow that as the previous part of the function contains:  $h = x + 0x30$ , then  $h - 0x30 = x$  so

$\exists rev(h)[rev(H(p)) = p - 0x30]$

II/ exclusive or

According to the Karnaught table at: [https://fr.wikipedia.org/wiki/Table\\_de\\_v](https://fr.wikipedia.org/wiki/Table_de_v)

*Thenas*

$xlat \oplus xlat = 0$ , and as  $p \oplus 0 = p$ , we know that the original password  
 $p = xlat \oplus h$ .

III/ rotating 4 first to 4 last bits

$\forall x[(x \ggg y) \implies (x \lll y = x)]$ .

*Thenas*

$z = (x \ggg y) = (x \lll y)$ , we know that the original password  $p = H(p) \lll 4$ .

IV/ unmasking different signatures (recurrent marks) in the hash

In the previous chapter one 'I/ substraction to reverse the addition', we told we can reverse the previous addition. We still need to guess which addition/substraction has been done previously.

As both addition values are made depending of:

“ if (password[left] 0xfffff0 ; 0xa0) -; password[left] + 0x30 or else  
password[left] + 0x37 if (password[right] 0x000000f ; 0x0a) -; password[right]  
0x0f + 0x30 or else password[right] 0x0f + 0x37 “

Then we have proven that:

$hp =$

$(d, s, f, d, , , k, f, o, A, , , ., i, y, e, w, r, k, l, d, J, K, D, H, S, U, B, s, g, v, c, a, 6, 9, 8, 3, 4, n, c, x, v) \implies$   
 $(\forall x \in hp[0 \geq x0 \geq 256 \implies x \in hp])$

then:

Let p be the password that the user types.

Let hp be the hardcoded password in the code of Packet Tracer.

Let lp be the length of the user input password.

Let h be the hash value obtained from the custom algorithm.

So that:

$$\begin{aligned} & \forall h \forall lp \forall hp [(hp \in N \wedge 0 \geq hp, \\ & 0 < lp < 16, \\ & h_0 = 0, \\ & h_1 = 8, \\ & h = \\ & \Sigma_{i=2}^{lp} \begin{cases} (((p_i \oplus hp_{i+8}) \lll 4) - 0x30), & \text{if } p_i < 0xa0 \text{ and if } i \equiv 0 \pmod{2} \\ (((p_i \oplus hp_{i+8}) \lll 4) - 0x37), & \text{if } p_i \geq 0xa0 \text{ and if } i \equiv 0 \pmod{2} \\ (((p_i \oplus hp_{i+8}) \wedge 0xfffffffff0) - 0x30), & \text{if } p_i < 0xa0 \text{ and if } i \equiv 1 \pmod{2} \\ (((p_i \oplus hp_{i+8}) \wedge 0xfffffffff0) - 0x37), & \text{if } p_i \geq 0xa0 \text{ and if } i \equiv 1 \pmod{2} \end{cases} \\ & ) \implies \forall p [p = \mathbf{rev}(h)] \end{aligned}$$