

# LiTAMIN2 : Ultra Light LiDAR-based SLAM

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## Introduction

Ultra Light LiDAR-based SLAM using Geometric Approximation applied with KL-Divergence

### Abstract :

In this paper, a 3D light detection and ranging simultaneous localization and mapping (SLAM) method is proposed. It is available for operating upon 500~1000Hz with high accuracy (almost same as the state-of-the-art method - "SuMa"), for more precise result, it can still work on 200Hz.

TABLE IV: Absolute trajectory error for each SLAM method.

| Method<br>(Num. of frames) | Loop<br>closure | Seq. 00<br>(4541) | Seq. 01<br>(1101) | Seq. 02<br>(4661) | Seq. 03<br>(801) | Seq. 04<br>(271) | Seq. 05<br>(2761) | Seq. 06<br>(1101) | Seq. 07<br>(1101) | Seq. 08<br>(4071) | Seq. 09<br>(1591) | Seq. 10<br>(1201) | Avg. of all frames<br>[deg] / [m] |
|----------------------------|-----------------|-------------------|-------------------|-------------------|------------------|------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-----------------------------------|
| LiTAMIN2 (ICP+Cov)         | —               | 1.6/5.8           | 3.5/15.9          | 2.7/10.7          | 2.6/0.8          | 2.3/0.7          | 1.1/2.4           | 1.1/0.9           | 1.0/0.6           | 1.3/2.5           | 1.7/2.1           | 1.2/1.0           | 1.8 / 5.1                         |
| LiTAMIN2 (ICP+Cov)         | ✓               | 0.8/1.3           | 3.5/15.9          | 1.3/3.2           | 2.6/0.8          | 2.3/0.7          | 0.7/0.6           | 0.8/0.8           | 0.6/0.5           | 0.9/2.1           | 1.7/2.1           | 1.2/1.0           | 1.2 / 2.4                         |
| LiTAMIN2 (ICP)             | —               | 1.8/5.4           | 3.1/13.8          | 3.4/12.1          | 2.4/0.7          | 1.9/0.6          | 1.4/3.6           | 0.7/0.7           | 1.3/0.9           | 3.0/5.9           | 1.9/2.8           | 1.5/1.8           | 2.3 / 6.0                         |
| LiTAMIN2 (ICP)             | ✓               | 0.8/1.2           | 3.1/13.8          | 1.3/3.0           | 2.4/0.7          | 1.9/0.6          | 0.7/0.7           | 0.8/0.6           | 0.6/0.4           | 2.2/4.5           | 0.8/1.3           | 1.5/1.8           | 1.3 / 2.6                         |
| LiTAMIN                    | —               | 2.0/4.7           | 3.0/84.3          | 2.4/9.7           | 3.4/0.8          | 1.4/21.3         | 1.4/2.3           | 0.7/0.9           | 0.7/0.5           | 1.9/3.5           | 1.4/1.6           | 1.7/1.7           | 1.9 / 8.3                         |
| LiTAMIN                    | ✓               | 1.1/1.5           | 3.0/84.3          | 1.8/3.7           | 3.4/0.8          | 1.4/21.3         | 0.9/1.0           | 0.8/0.8           | 0.6/0.3           | 1.6/2.8           | 1.3/1.4           | 1.7/1.7           | 1.5 / 6.2                         |
| SuMa (Frame-to-Frame)      | —               | 6.4/19.7          | 8.2/34.9          | 5.4/21.3          | 4.1/1.2          | 3.4/13.4         | 2.9/5.1           | 1.5/2.0           | 2.1/2.9           | 6.2/15.9          | 2.4/5.0           | 2.4/3.4           | 4.8 / 14.1                        |
| SuMa (Frame-to-Model)      | —               | 1.0/2.9           | 3.2/13.8          | 2.2/8.4           | 1.5/0.9          | 1.8/0.4          | 0.7/1.2           | 0.4/0.4           | 0.7/0.5           | 1.5/2.8           | 1.1/2.9           | 0.8/1.3           | 1.4 / 3.9                         |
| SuMa (Frame-to-Model)      | ✓               | 0.7/1.0           | 3.2/13.8          | 1.7/7.1           | 1.5/0.9          | 1.8/0.4          | 0.5/0.6           | 0.7/0.6           | 1.1/1.0           | 1.2/3.4           | 0.8/1.1           | 0.8/1.3           | 1.1 / 3.2                         |
| LeGO-LOAM                  | —               | 2.8/6.3           | 3.8/119.4         | 4.1/14.7          | 4.1/0.9          | 3.3/0.8          | 1.9/2.8           | 1.4/0.8           | 1.5/0.7           | 2.5/3.5           | 2.2/2.1           | 1.9/1.8           | 2.8 / 11.1                        |
| hdl_graph_slam             | —               | 5.4/41.8          | 34.0/635.8        | 22.3/153.0        | 2.3/1.0          | 3.4/93.4         | 2.5/5.7           | 3.3/43.0          | 2.2/1.6           | 6.2/13.8          | 4.6/15.9          | 1.8/3.5           | 9.3 / 76.7                        |
| LOAM                       | —               | 5.8/19.4          | 6.1/21.0          | 21.7/111.6        | 3.3/1.0          | 2.2/0.5          | 2.2/4.6           | 0.9/1.1           | 1.2/1.3           | 3.0/6.7           | 1.9/5.3           | 1.5/1.9           | 7.0 / 29.7                        |

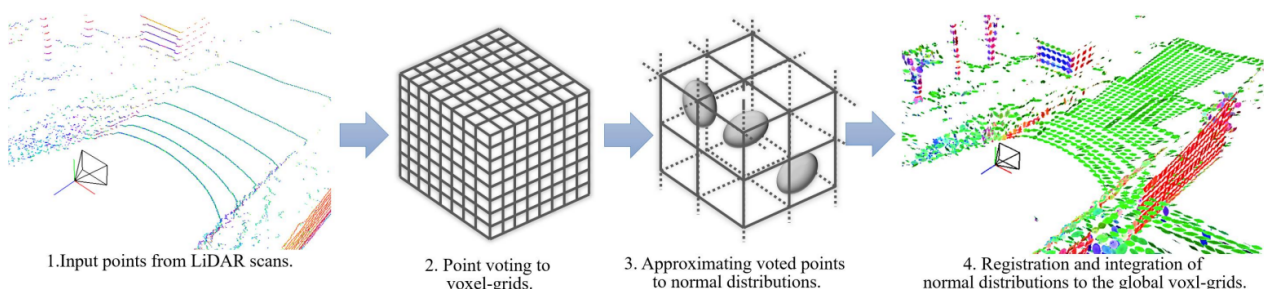
LiTAMIN2 used the size of voxel as 3 m from the best accuracy result of table II. The marks ✓ and — mean with (✓) and without (—) loop closure, respectively, for each method.

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This paper uses a novel ICP metric to speed up the registration process while maintaining accuracy. However, Reducing quantity of point cloud can drop the accuracy, to avoid this issue, symmetric KL-divergence is introduced to the ICP cost that reflects the difference between two probabilistic. The cost function includes not only the distance between points but also differences between distribution shapes.

### Main works

- Reduction of the number of points
  - Voted a group of input points into the voxel grids.
  - Aligned them using the means of the voting points.
  - Integrated the point clouds into voxel map.



- ICP cost function applied with symmetric KL-divergence

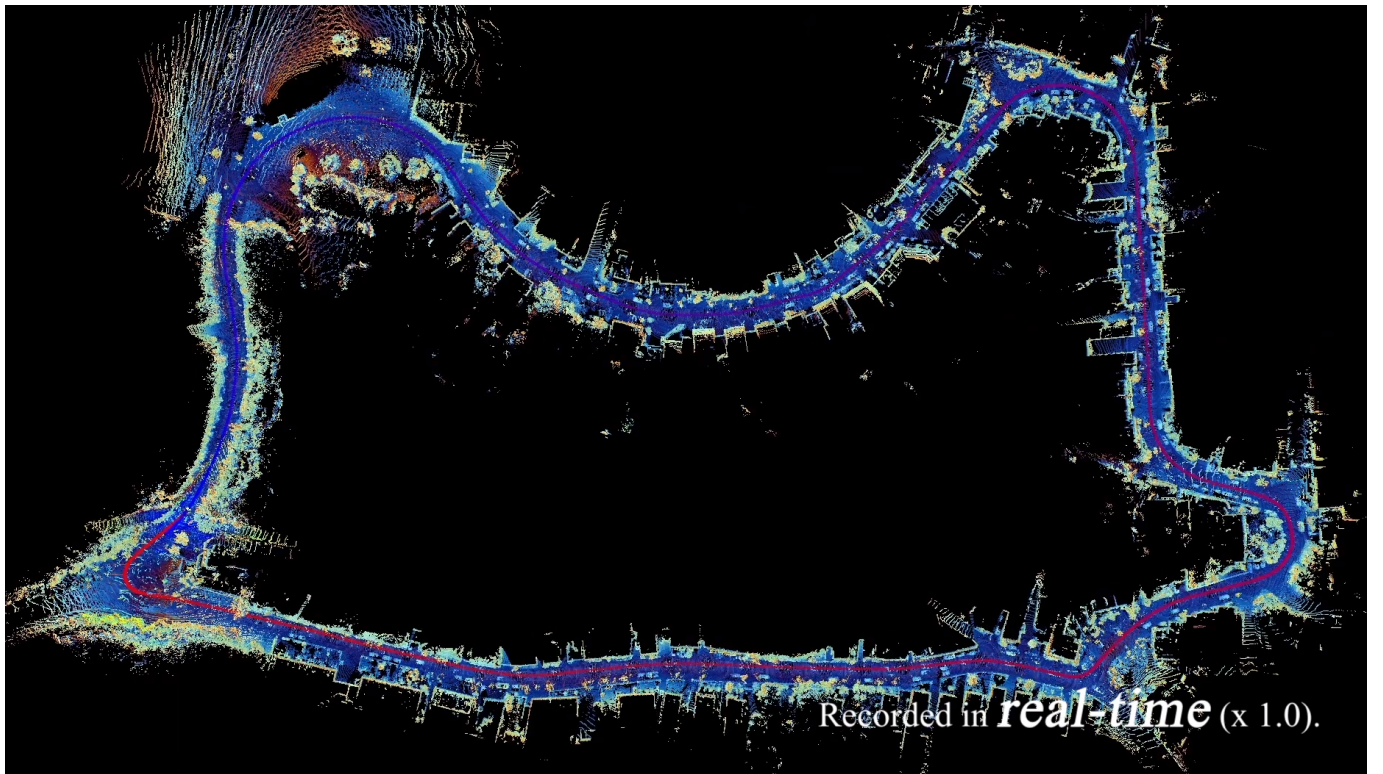
TABLE I: Comparison of the ICP cost functions for local approximation with a cluster of normal distributions.

| Method                     | ICP cost function per point-association  |
|----------------------------|--|
| Standard ICP               | $(q - (Rp + t))^T (q - (Rp + t))$  |
| NDT                        | $(q - (Rp + t))^T C^{-1} (q - (Rp + t))$   |
| Generalized ICP            | $(q - (Rp + t))^T (C_q + RC_p R^T)^{-1} (q - (Rp + t))$  |
| LiTAMIN                    | $(q - (Rp + t))^T \frac{w(C + \lambda I)^{-1}}{\ (C + \lambda I)^{-1}\ _F} (q - (Rp + t))$   |
| LiTAMIN2 (proposed method) | $w_{ICP} \left[ (q - (Rp + t))^T \frac{(C_q + RC_p R^T + \lambda I)^{-1}}{\ (C_q + RC_p R^T + \lambda I)^{-1}\ _F} (q - (Rp + t)) \right] + w_{Cov} [\text{Tr}(RC_p^{-1} R^T C_q) + \text{Tr}(C_q^{-1} RC_p R^T) - 6]$ |

## Reference :

### Video

- [LiTAMIN2 \(ICRA 2021\) Youtube](#)



### Links

- [MR2T lab official web](#)
- [LiTAMIN2: Ultra Light LiDAR-based SLAM using Geometric Approximation applied with KL-Divergence](#)
- [LiTAMIN2 introduction](#)
- [ICRA2021 LiTAMIN2の復現](#)