## **A Recursive Example**

Another way to think of the *factorial* function is as a recurrence relation, which recursively defines a sequence; each further term is defined as a function of the preceding terms.

$$n! = n \times (n-1)!$$

Without qualification, this is a **circular definition**. The **qualification** is that **0! = 1**. We can translate this **recursive definition** into code as well:

```
int factorial(n)
{
   if (n == 0) { return 1; } // qualification
   return n * factorial(n - 1); // recursion
}
```

The condition (n == 0) is the simplest possible condition. It is called the **base case**. If n is not zero, then the function multiplies n times the result of (n - 1)!. It does this, by **calling itself** again to simplify the problem.

The solution to **any** recursive problem can be organized like this:

```
If the answer is known then return it // the base case
If not, then
Call the function with simpler inputs // recursive case
Return the combined simpler results
```

This **pattern** is called the **recursive paradigm**. You can apply this technique as long as:

- 1. You can identify simple cases for which the answer is known.
- 2. You can find a **recursive decomposition** breaking any complex instance of the problem into simpler problems **of the same form**.

Because this depends on dividing complex problems into simpler instances of the same problem, such recursive solutions are often called **divide-and-conquer algorithms**.



This course content is offered under a <u>CC Attribution Non-Commercial</u> license. Content in