HW 4: Response Time and Real-Time Scheduling

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Question 1: Cyclic Executive

Part A

A system's total utilization is given by:

$$\sum_{i=1}^{n} \frac{C_i}{T_i}$$

Plugging in the values from the problem yields:

$$\frac{1}{3} + \frac{1}{4} + \frac{2}{6} + \frac{1}{12}$$
$$\frac{4+3+4+1}{12} = \frac{12}{12} = 100\%$$

Part B

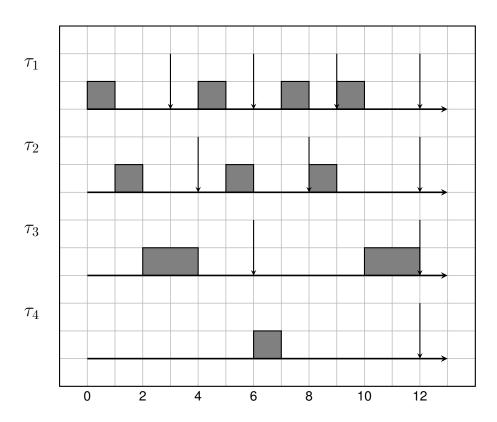


Figure 1: The downward arrow represents the deadline

Question 2: Interrupt Latency

Part A

$$ISRLatency_{2}^{0} = 12$$

$$ISRLatency_{2}^{1} = 12 + \left\lceil \frac{12}{30} \right\rceil 10 + \left\lceil \frac{12}{26} \right\rceil 4 = 12 + 10 + 4 = 26$$

$$ISRLatency_{2}^{2} = 12 + \left\lceil \frac{26}{30} \right\rceil 10 + \left\lceil \frac{26}{26} \right\rceil 4 = 12 + 10 + 4 = 26$$

Max latency is 26 ms.

Part B

$$ISRLatency_{2}^{0} = 24$$

$$ISRLatency_{2}^{1} = 24 + \left\lceil \frac{24}{30} \right\rceil 10 + \left\lceil \frac{24}{26} \right\rceil 4 = 24 + 10 + 4 = 38$$

$$ISRLatency_{2}^{2} = 24 + \left\lceil \frac{38}{30} \right\rceil 10 + \left\lceil \frac{38}{26} \right\rceil 4 = 24 + 20 + 8 = 52$$

Max latency is 52 ms.

Question 3: Preemptive Task Scheduling

Part A

In order to to determine schedulability we must see that $U \leq 1$.

$$U = \frac{13}{60} + \frac{8}{15} + \frac{5}{20}$$

$$U = \frac{13 + 32 + 15}{60}$$

$$U = \frac{60}{60} = 1$$

The system meets the EDF Schedulability Condition, therefore the system can be scheduled with EDF.

Part B

The system has a higher utilization then the bound (U(3) = 0.780). Need to apply RT test to determine schedulability.

$$\begin{aligned} Order: \tau_2, \tau_3, \tau_1 \\ R_1^0 &= C_1 = 13 \\ R_1^1 &= 13 + \left\lceil \frac{13}{15} \right\rceil 8 + \left\lceil \frac{13}{20} \right\rceil 5 = 13 + 8 + 5 = 26 \\ R_1^2 &= 13 + \left\lceil \frac{26}{15} \right\rceil 8 + \left\lceil \frac{26}{20} \right\rceil 5 = 13 + 16 + 10 = 39 \\ R_1^3 &= 13 + \left\lceil \frac{39}{15} \right\rceil 8 + \left\lceil \frac{39}{20} \right\rceil 5 = 13 + 24 + 10 = 47 \\ R_1^4 &= 13 + \left\lceil \frac{47}{15} \right\rceil 8 + \left\lceil \frac{47}{20} \right\rceil 5 = 13 + 32 + 15 = 60 \\ R_1^5 &= 13 + \left\lceil \frac{60}{15} \right\rceil 8 + \left\lceil \frac{60}{20} \right\rceil 5 = 13 + 32 + 15 = 60 \end{aligned}$$

Can be scheduled with rate monotonic scheduling.

Part C

 $15\ \mathrm{and}\ 20$ are not multiples of one another.

Part D

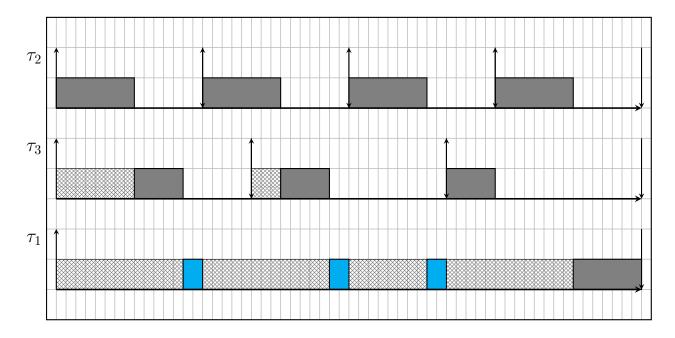


Figure 2: The downward arrow represents the deadline and the upward arrow represents the arrival of a task. If the box is blue it means the task was preempted.