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# Weekly Report Aug 6,2018-Aug 12,2018

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## Abstract

In a nutshell, I continued the work of last week.

## 1 Tuesday

### 1.1 current state

1. I finished week 7 of Algorithm(graph searching)

### 1.2 The record of my Algorithms

#### 1.2.1 HEAP

1. Firstly, according to my buddy's advice, I learned about several data structures, namely lists, stacks, queues, heaps, search trees, hash tables, bloom filter and union-find,etc. First of all, is the HEAP structure mentioned by me last week.

HEAP is a container of objects that have keys, here are several common operations on a HEAP:

INSERT: add a new object to a HEAP running time:  $O(\log n)$

EXTRACT-MIN(MAX): remove an object in a HEAP with a minimum (or maximum) key value running time:  $O(\log n)$

HEAPIFY:  $n$  batch insert in  $O(n)$  time

DELETE: from a middle running time:  $O(\log n)$

2. Then I learned about the first application of heap— sorting, which is used as a fast way to do repeated recall for the minimum

HEAP SORT:

1. insert into the heap

2. extract one by one

The running time can be  $2n \log n$

MEDIUM MAINTENANCE:

$X_1, X_2, \dots, X_m$  divided into  $H_{low}$  and  $H_{high}$  and the medium is just between them

SPEEDING UP DIJKSTRA:

By using heaps, we can do the graph search with the running time of  $O(m \log n)$

3. Then I learned about the HEAP property, it's conceptionally a rooted binary complete tree, at every node  $X$ ,  $key[X] \leq$  all children's keys, Thus we say that the root is the minimum

NOTE:

$parent(i) = \frac{i}{2}$  if  $i$  is even

$parent(i) = \lceil \frac{i}{2} \rceil$  if  $i$  is odd

children of  $i = 2i, 2i+1$

054 4. Then I went through the INSERTION AND BUBBLING UP of HEAP:  
 055 INSERTION:  
 056 step1: stick k at the end of the last leave  
 057 step2:swap key ( if violate the rule then bubble up k until it's properly stored)  
 058 EXTRACT:  
 059 step1: delete root  
 060 step2:move last leaf to be the new root  
 061 step3:swap the smaller child  
 062  
 063 **1.2.2 BINARY SEARCH TREE**  
 064  
 065 Here is a comparison of the traditional sorted array and BINARY SEARCH TREE:  
 066 SORTED ARRAY:  
 067 SEARCH  $O(\log n)$   
 068 SELECT  $O(1)$   
 069 MIN/MAX  $O(1)$   
 070 PRED/SUCC  $O(1)$   
 071 RANK  $O(\log n)$   
 072 OUTPUT  $O(n)$   
 073 BINARY SEARCH TREE:  
 074 SEARCH  $O(\log n)$   
 075 SELECT  $O(\log n)$   
 076 MIN/MAX  $O(\log n)$   
 077 PRED/SUCC  $O(\log n)$   
 078 RANK  $O(\log n)$   
 079 OUTPUT  $O(n)$   
 080 INSERT  $O(\log n)$   
 081 DELETE  $O(\log n)$   
 082  
 083 5. Then I learned about the BST structure  
 084 -exactly one node per key  
 085 -each node has three nodes:  
 086 1.left child  
 087 2.right child  
 088 3.parent  
 089  
 090 6. Then I learned about its property:  
 091 the key left is less and the key right is bigger  
 092 The Print procedure is a recursive tricky call:  
 093 -let r = root of search tree, with subtrees Tl,Tr  
 094 -recurse on Tl  
 095 -print out r  
 096 -recurse on Tr  
 097 The running time is  $O(n)$   
 098  
 099 7. Then I learned about its deletion  
 100 EASY (k has no children) delete directly  
 101 MEDIUM (k has one child) delete k and swap  
 102 DIFFICULT (k has two children)  
 103 compute k's PRES L  
 104 swap k and L  
 105 delete k  
 106  
 107 8. Then I learned about the select and rank:  
 SELECT  
 -start at x ,with children y and z  
 -let a =size(y)

108            -if a=i-1, return x's key  
109            -if a  $\leq$  i-1, recurse on Y  
110            -if a  $\geq$  i-1, recurse on z  
111

### 112            **1.2.3 RED BLACK TREE**

114            9. how to balance the tree to make it as complete as possible? We here use the RED BLACK  
115            TREE, we can ensure that the height is always  $O(\log n)$   
116            The principle of it is actually quite simple:  
117            - each node is red or black  
118            - the root is black  
119            - no two red in one row  
120

## 121            **2 Tuesday**

### 122            **2.1 current state**

123  
124            1. I finished week 8 of Algorithm(graph searching)  
125

### 126            **2.2 records of my algorithm**

#### 127            **2.2.1 HASH TABLE**

128            1. The purpose of hash table is to maintain a set of stuff, we use a key to insert, delete and  
129            look up, these operations all run in a  $O(1)$  constant time and there are some applications of  
130            the HASH TABLE:  
131

132            2. DE-DUPLICATION a given stream of objects, we linear scan the objects, the goal is to  
133            remove the duplicates, the solution is as follows:  
134            - look up in hash table  
135            - if not found, insert x  
136

137            3. 2-sum problem, we input an unsorted array of n integers, target sum t, we want to figure  
138            out whether or not there are 2 numbers x, y that  $x+y=t$   
139

140            NAIVE:  
141            -  $O(n^2)$  running time exhaustive search  
142

143            BETTER:  
144            - sort A  $O(n \log n)$   
145            - for each x in A, look for  $t-x$  in A with  $O(n \log n)$   
146

147            AMAZING:  
148            - insert elements of A  
149            - for each x in A, look up  $t-x$  in H  
150

151            HISTORICAL APPLICATION:  
152            - symbol tables in compilers  
153            - blocking network traffic  
154            - speed up search algorithm  
155

156            4. Then I learned about the high level idea:  
157            - pick n = number of buckets  
158            - choose a hash function  $h(x)$   
159            - use array A of length n, store x in  $A(h(x))$   
160            but in a hash function, sometimes the different elements collide in a same bucket, there are  
161            two solutions:  
162

              CHAINING:  
              - keep linked lists in each bucket  
              - given a key (object x, perform insert delete look up) in the list in  $A(h(x))$   
              OPEN ADDRESSING

162 -hash funtion now specifies probe sequence  $h_1(x)$ ,  $h_2(x)$  (keep trying until find a open slot)  
163 -linear probing (look consecutively)  
164

## 165 5. HASH FUNTIONS

166 1. It should be easy to store and be very fast to evaluate

167 2.It should lead to good performance

168 Beacuse all of the hash functions has there disadvantages, so we should design it accoring  
169 to the problem, one of the method is the QUICK AND DIRTY HASH FUNCTION, which  
170 links the objects with integers and integers with buckets  
171

172 6. Then I learned how to choose na s buckets

173 -n should be a prime

174 -not too close to the power of 2

175 -not too close to the power of 10  
176

### 177 2.2.2 BLOOM FILTER

178  
179 7. Then I learned about the use of bloom filter, it has some advantages and disadvantages

180 ADVANTAGE:

181 -move space efficiently

182 DISADVANTAGE:

183 -can not store an associated object

184 -no deletions

185 -small false positives

186 Then we can look up if the elements exists in the list easily!  
187

## 188 3 summary

189  
190 These days there are too many other trifles, spoiling the learning procedure.  
191  
192

## 193 4 Saturday

### 194 4.1 current state

195  
196 1. I finished week 9 of Algorithm(greedy algorithm)  
197  
198

### 199 4.2 records of my algorithm

#### 200 4.2.1 APPLICATION of the GREEDY ALGORITHM

201  
202 1.1. internet-graph, we take the vertices as end hosts and router

203 1.2.web-graph, we take edges as hyperlinks

204 we use BELL-Ford algorithm to calculate the shortest path

205 2.1 sequence alignment, we use two strings over the alphabet , to check out how similar they are( in  
206 gene similarity)  
207  
208

#### 209 4.2.2 Paradigms of design algorithm

210 -divide and conquer

211 -randomized algorithm

212 -greedy algorithm

213 -dynamic algorithm  
214  
215

### 4.2.3 Greedy algorithm

-DEF: we take myopic decision, hope everything work at the end  
-EXAMPLE: the Dijkstra's shortest path algorithm, it's processed once on each step irrevocably  
what kind of problems can be solved by greedy algorithm? for an example, we can solve the  
caching problem ,using the BELADY(1960's) theorem "the furthest-in-future", as guideline for  
practical algorithm ,and such problem can be extended to a new stage-scheduling problem

### 4.2.4 scheduling problem

we assume the job  $j$  has weight  $w_j$ , and length  $l_j$ , we want the minimum of the completion time  $C_j$ ,  
obviously:  
-if the jobs has equal length and different weight, we put heavier ahead  
-if the jobs has equal weight and different length, we put shorter ahead  
we assume the score in two forms:  $W_j \cdot L_j$  and  $\frac{W_j}{L_j}$ , by using examples we find that the former is  
wrong, then we use the induction method to prove that the score can be expressed as the later form.  
-we sort the jobs in the order 1, 2, ...,  $n$  as  $\frac{W_1}{L_1} > \frac{W_2}{L_2} > \dots > \frac{W_n}{L_n}$   
-if there is a better way than the greedy method, there should be  $i < j$ , if we exchange  $i$  and  $j$ , the cost  
is  $W_i L_j$ , and the benefit is  $W_j L_i$ , obviously benefit is bigger than cost ,if we exchange like this for at  
most  $C^n 2$  times ,the score can be proved right.

### 4.2.5 PRIM's MST ALGORITHM

INPUT: undirected graph  $G(V, E)$   
-assume adjacency list representation  
-negative is ok  
OUTPUT: minimum cost tree that spans all vertices  
the operations are as follows:  
-initialize  $X = \{s\}$   
- $T =$   
-while  $X \neq T$   
let  $e(u, v)$  = the cheapest edge  
add  $e$  to  $T$   
add  $v$  to  $X$   
if we use the HEAP structure, the running time can be easily  $O(m \log n)$