

Plane truss

Laboratory course Matlab

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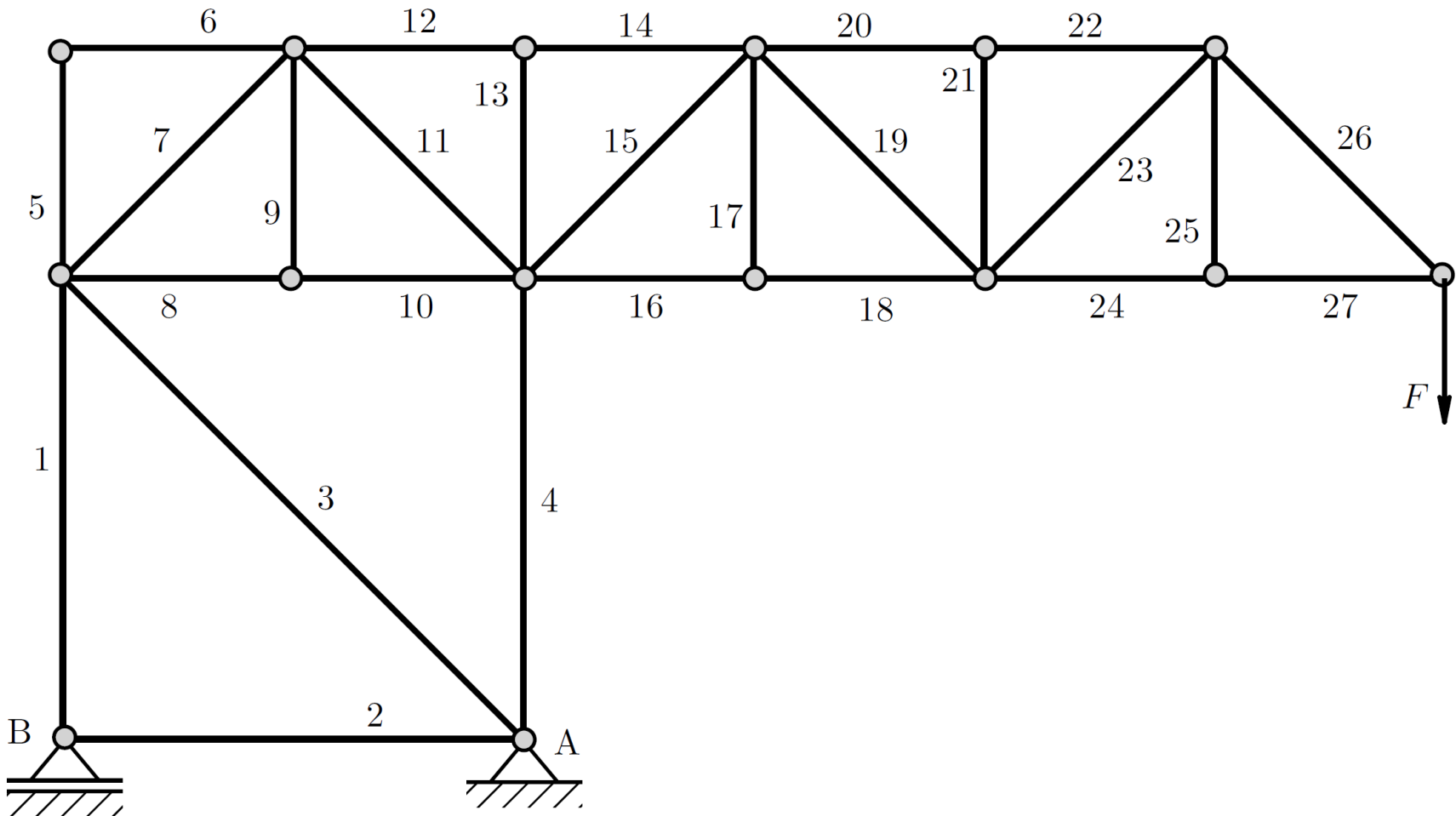
October 25th, 2024

Content:

1. Theory about plane trusses
2. Notes on the task

Task in the laboratory course

Plane trusses



Assumption of an **ideal truss**:

- i. The bar axes are straight.
- ii. The bar axes intersect in one point, the so-called **nodes**.
- iii. At the intersection, the bar axes are connected by frictionless joints.

Thus, **no moments** can be initiated in the bars.

- iv. The active forces only act on the nodes.

Condition for static determination (1):

- Degree of freedom of the bounded system:

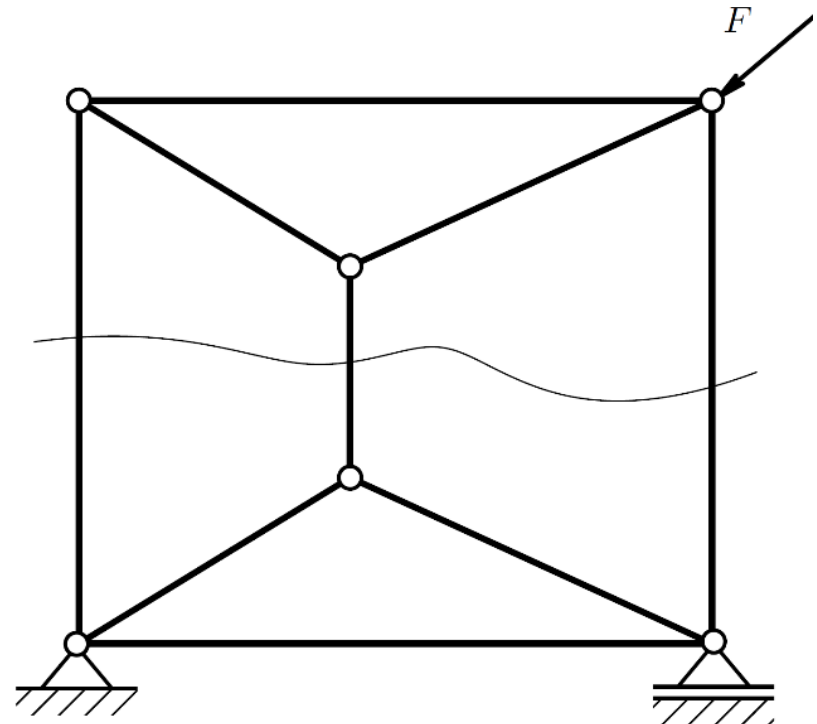
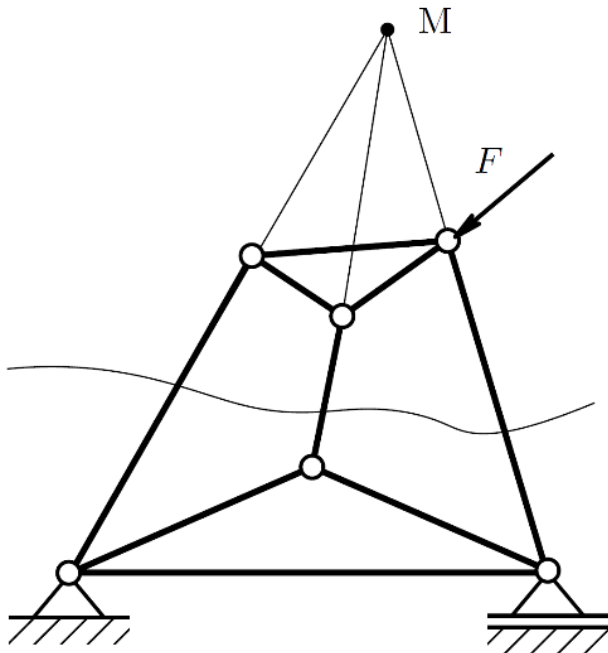
$$f = 2k - (a + s)$$

| | |
|-----|--------------------------------------|
| k | number of nodes |
| a | number of support connections |
| s | number of bars |

- External degree of freedom: $f_a = 3 - a$
- Internal degree of freedom: $f_i = f - f_a = 2k - (3 + s)$
- Necessary condition for the rigidity: $f \leq 0$

1. Theory about plane trusses

Condition for static determination(2): Exceptional cases



Condition for static determination (3):

- Necessary and sufficient condition for the rigidity and load-bearing capacity of the truss (no exceptional case)

$$f \leq 0 \quad \text{and} \quad f_a \leq 0$$

- $2k$ equilibrium conditions for the determination of the $(a + s)$ support connections and bar forces

$$f \begin{cases} > 0 & \text{movable (not stable)} \\ = 0 & \text{statically determined} \\ < 0 & \text{statically undetermined} \end{cases}$$

Method of joints (1):

1. Cutting all nodes free
2. Setting up the equilibrium of forces at all nodes:

- equilibrium of forces in x-direction
- equilibrium of forces in y-direction
- equilibrium of moments is not necessary,
since no moments are initiated in the bars

$$\sum F_x \doteq 0$$

$$\sum F_y \doteq 0$$

$$\sum M_n = 0$$

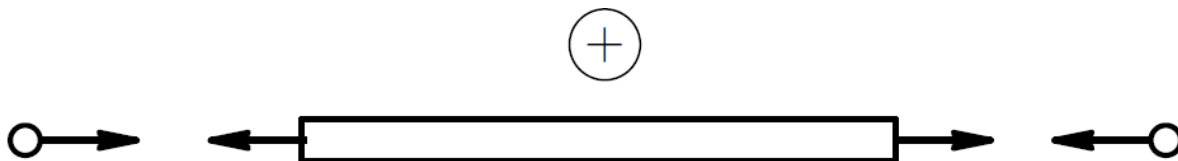
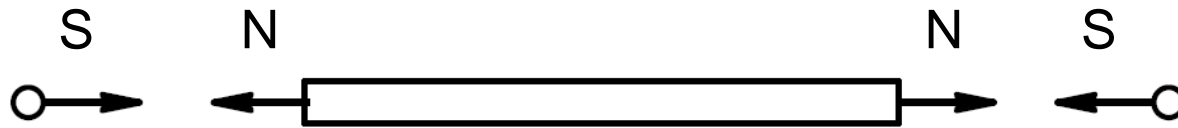
3. Summarising the equilibrium conditions in a linear and inhomogeneous system of equations with the dimension:

$$2k \times (a + s)$$

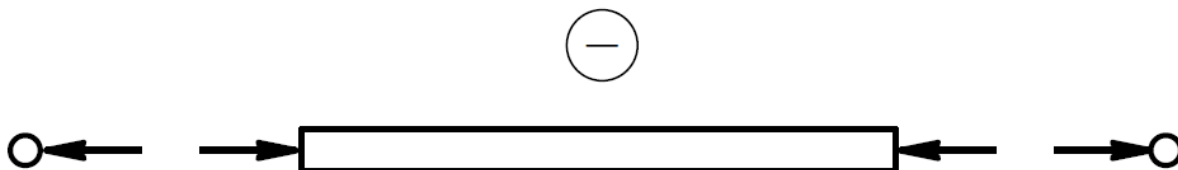
Alternative: Method of sections

1. Theory about plane trusses

Sign convention:



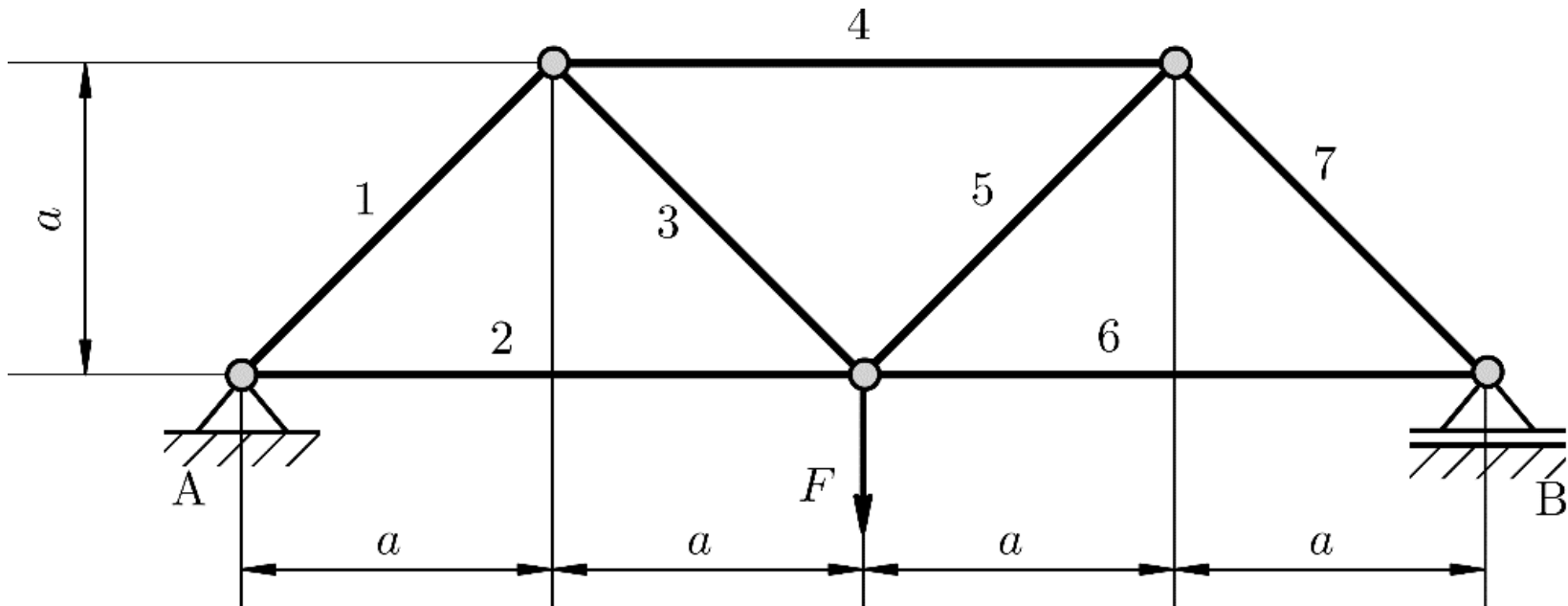
Tension bar
($S > 0 \text{ N}$)



Compression bar
($S < 0 \text{ N}$)

2. Notes on the task

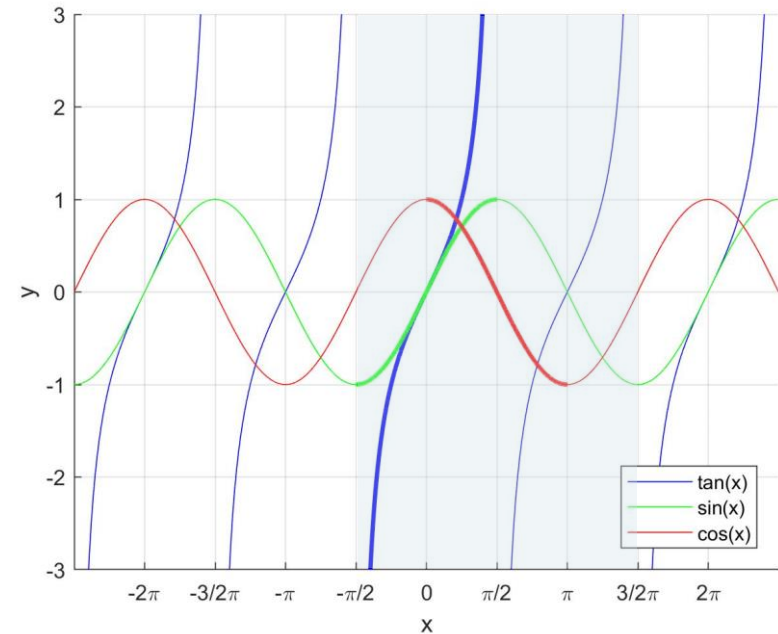
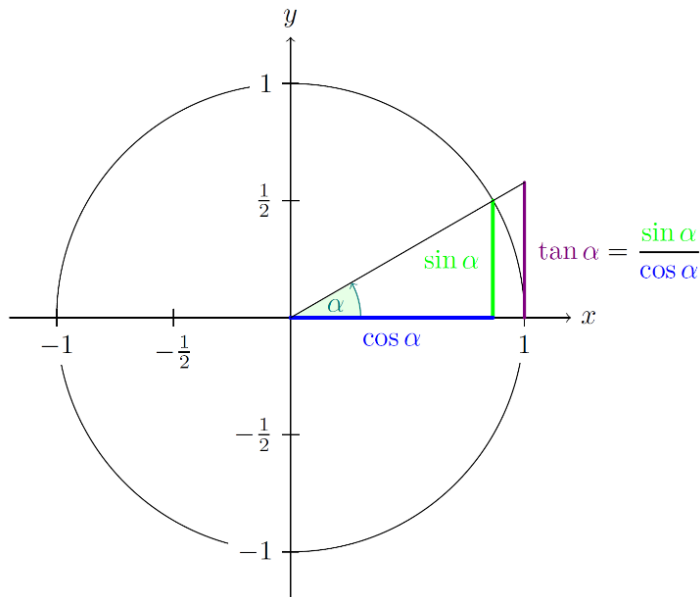
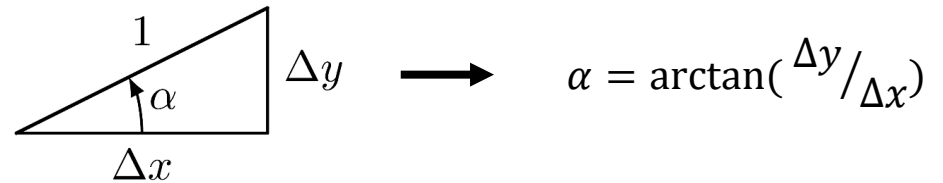
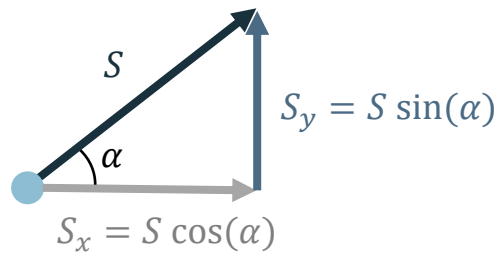
Method of joints (2) - **Task 1** in the script as preparation for the programming task:



➡ Cutting free and setting up the linear system of equations

2. Notes on the task

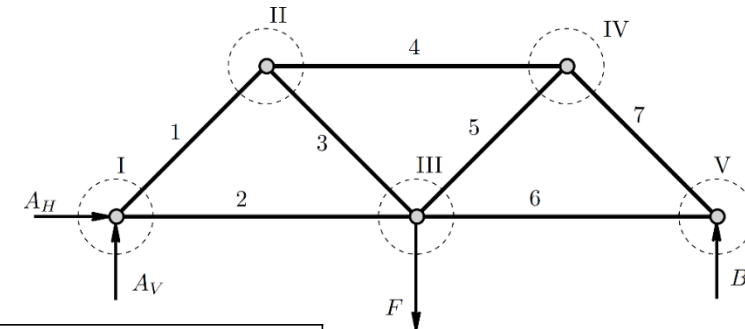
Arctangent:



2. Notes on the task

Method of joints (3) - Task 1 in the script:

Result $\mathbf{A}\mathbf{r} = -\mathbf{f} \longrightarrow \mathbf{r} = -\mathbf{A}^{-1}\mathbf{f}$



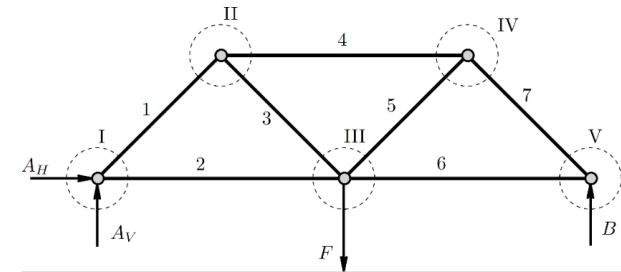
| Kn. | A_H | A_V | B | S_1 | S_2 | S_3 | S_4 | S_5 | S_6 | S_7 | | |
|-----|-------|-------|-----|---------------|-------|---------------|-------|---------------|-------|---------------|-------|-----|
| I | 1 | 0 | 0 | $\sqrt{2}/2$ | 1 | 0 | 0 | 0 | 0 | 0 | A_H | 0 |
| | 0 | 1 | 0 | $\sqrt{2}/2$ | 0 | 0 | 0 | 0 | 0 | 0 | A_V | 0 |
| | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| II | 0 | 0 | 0 | $-\sqrt{2}/2$ | 0 | $\sqrt{2}/2$ | 1 | 0 | 0 | 0 | B | 0 |
| | 0 | 0 | 0 | $-\sqrt{2}/2$ | 0 | $-\sqrt{2}/2$ | 0 | 0 | 0 | 0 | S_1 | 0 |
| | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| III | 0 | 0 | 0 | 0 | -1 | $-\sqrt{2}/2$ | 0 | $\sqrt{2}/2$ | 1 | 0 | S_2 | 0 |
| | 0 | 0 | 0 | 0 | 0 | $\sqrt{2}/2$ | 0 | $\sqrt{2}/2$ | 0 | 0 | S_3 | F |
| | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| IV | 0 | 0 | 0 | 0 | 0 | 0 | -1 | $-\sqrt{2}/2$ | 0 | $\sqrt{2}/2$ | S_4 | 0 |
| | 0 | 0 | 0 | 0 | 0 | 0 | 0 | $-\sqrt{2}/2$ | 0 | $-\sqrt{2}/2$ | S_5 | 0 |
| | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | ... |
| V | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | -1 | $-\sqrt{2}/2$ | S_6 | 0 |
| | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | $\sqrt{2}/2$ | S_7 | 0 |

\mathbf{A}

\mathbf{r}
 $=$
 $-\mathbf{f}$

2. Notes on the task

Data structure (e.g. `truss_3.mat`)



Connectivity
(`conn`)

| local node 1 | local node 2 |
|--------------|--------------|
| 1 | 2 |
| 1 | 3 |
| 2 | 3 |
| 2 | 4 |
| 3 | 4 |
| 3 | 5 |
| 4 | 5 |

Coordinates
(`coord`)

| x | y |
|---|---|
| 0 | 0 |
| 2 | 2 |
| 4 | 0 |
| 6 | 2 |
| 8 | 0 |

Bearing
(`bearing`)

| node | dof |
|------|-----|
| 1 | 1 |
| 1 | 2 |
| 5 | 2 |

External loading
(`F`)

| node | F_x | F_y |
|------|-------|-------|
| 3 | 0 | -1.5 |

Reading and saving variables

- `[filename , pathname] = uigetfile`
opens a graphic dialog box to select a file that, for example, can subsequently be loaded with the `load` function. The `uigetfile` function gives back two output-variables: the `filename` and the `pathname` to the folder that contains the file
- **concatenation:** `filepath = [pathname, filename]`
- `input = load(filepath)`
loads variables of a `.mat`-file in the Matlab workspace
- `save(`results.mat`)`
saves the entire workspace in a `.mat`-file called `results`

Access to data in structure arrays

- `s = struct(field1, value1 , field2, value2, ...)`
summarises different field arrays, denoted by `field1` and `field2`, with the values `value1` and `value2` in one structure `s`.
The same can be obtained by using

```
s.field1 = value1;  
s.field2 = value2;
```

- Access to the values of a structure field via a dot `.`

```
input = load(filename);  
forces = input.F;
```

Access to data in matrices

- Saving data in principle by a matrix or multidimensional array, e.g.

$$A = [1, 2; 3, 4] \longrightarrow A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

- Access and assignment via indices $A(i, j)$ (row i und column j)

$$A(1, 2) = 5 \longrightarrow A = \begin{bmatrix} 1 & 5 \\ 3 & 4 \end{bmatrix}$$

- $l = \text{length}(v)$ or $[m, n] = \text{size}(A)$
query the length l of a vector v or the number of rows m and columns n of a $[m \times n]$ matrix A .

Using $\text{length}(A)$ returns the maximum value of m and n .

Generating graphs (1)

- `figure`
generates a new window to plot graphs;
plotting multiple graphs is only possible with the command
`hold on`
- `p1 = plot([x1 , x2] , [y1 , y2])`
draws a 2D line plot from point $(x1, y1)$ to point $(x2, y2)$
- `legend([p1 , p2] , `bar`, `force`)`
creates legend of the line plots of the current window

Generating graphs (2)

- `text(x1, y1, `node 1`)`
adds the text `node 1` to the data point `(x1, y1)`
- `quiver(x2, y2, force(1), force(2))`
draws the vector `force` at point `(x2, y2)`
- Uniform arrow size with the additional option
`quiver(x2, y2, force(1), force(2), ...`
``MaxHeadSize`, 1/norm(force))`

Angle calculation and solving the linear system of equation

- `atan(dy/dx)`
Arctangent in rad for the value range $[-\frac{\pi}{2}, +\frac{\pi}{2}]$
→ Function with **only one** input parameter
- `atan2(dy, dx)`
Arctangent in rad for the value range $[-\pi, +\pi]$
→ Function with **two** input parameters
- `x = A\b`
solves the linear system of equations $\mathbf{Ax} = \mathbf{b}$ for the vector \mathbf{x}

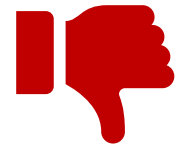
Hard vs. generic coding for plane truss code

- **Hard coding:**

The script is explicitly coded for the trusses given in the input files, e.g. for truss 3:

```
Nnodes = 5;
```

```
...
```



- **Generic coding:**

The script is coded in a general way, such that any input file defining a truss can be evaluated

```
Nnodes = size(coords,1);
```

```
...
```



Thank you for your attention!

If you have any questions on the lecture, please use the forum „Forum: experiment LTM“ on StudOn.

You can also contact me via email emely.schaller@fau.de.

LTM-task

on November 8th (group A)

on November 15th (group B)

from 10 am to 4 pm

in the MB & CBI CIP-Pool