$$\tau_1^N = \sum_{k=1}^{N-1} \sum_{l=1}^k \phi_l^N \frac{1}{T_l^+} \prod_{m=l+1}^k \frac{T_m^-}{T_m^+}$$