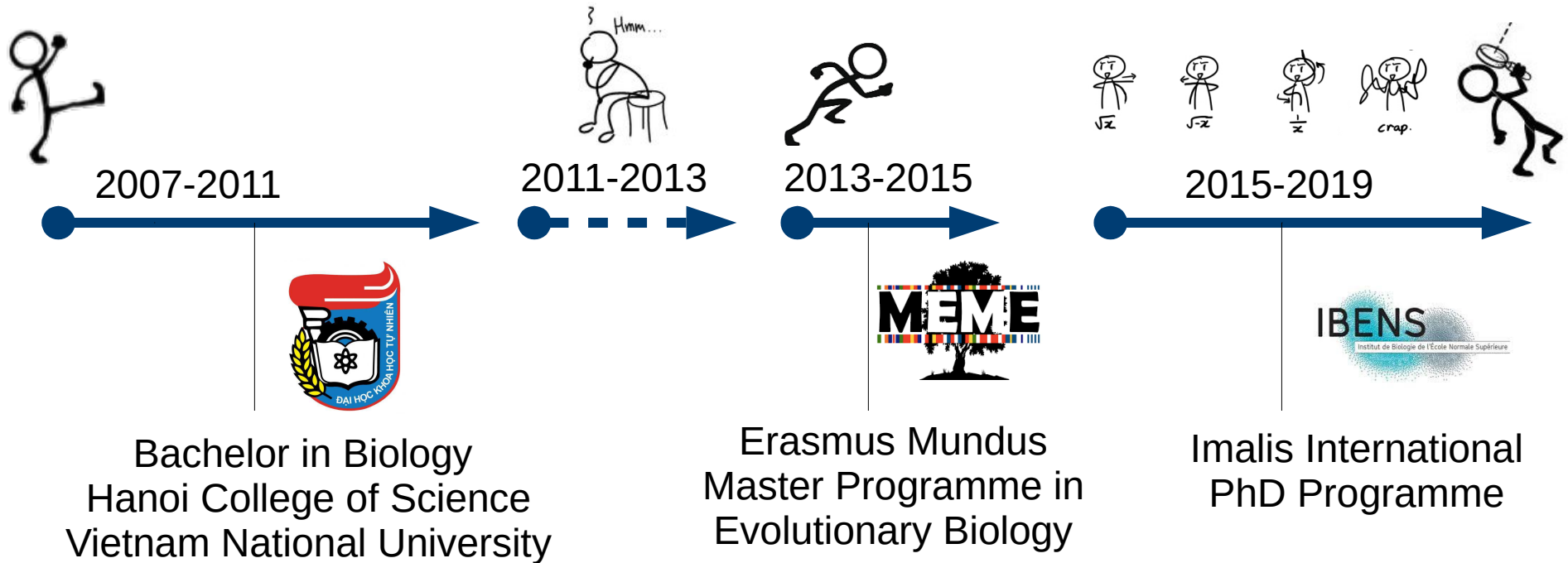


# **On the evolutionary transitions from free-living organisms to obligate symbioses**

Linh-Phuong NGUYEN

Supervised by: Minus van Baalen

# The story of my academic life



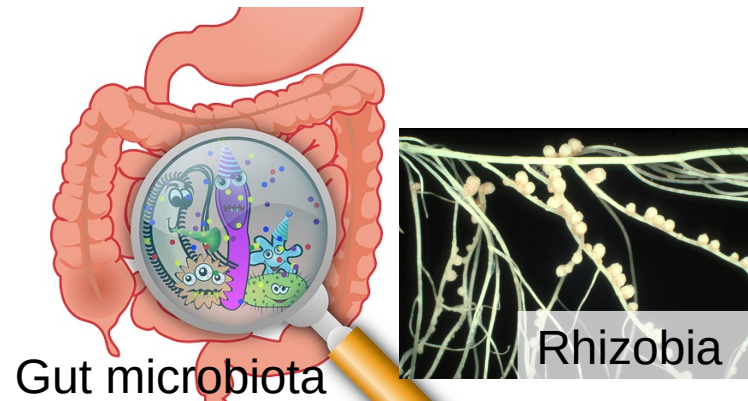
# The diverse world of symbiosis



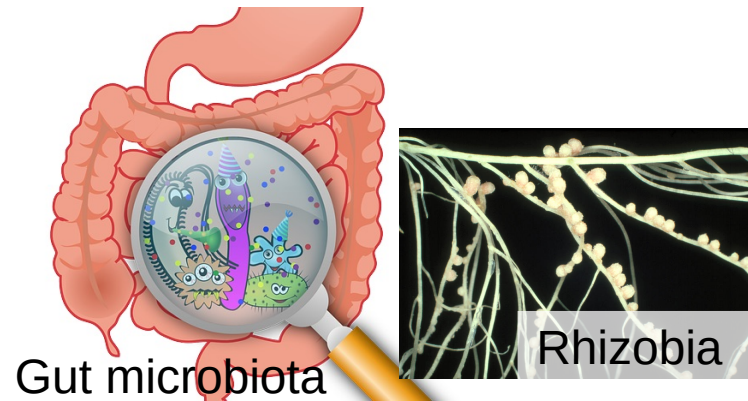
# The diverse world of symbiosis



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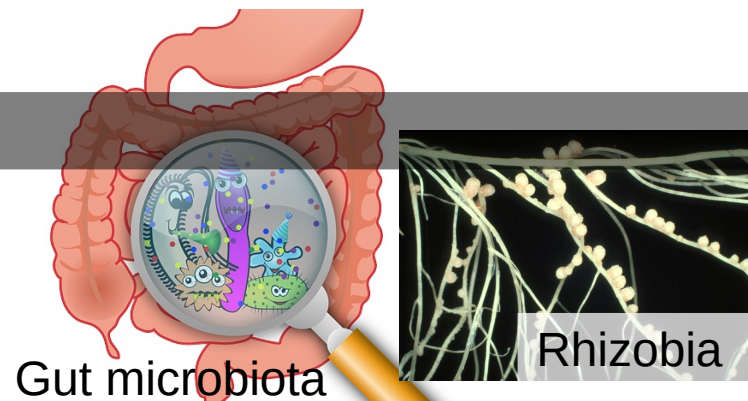
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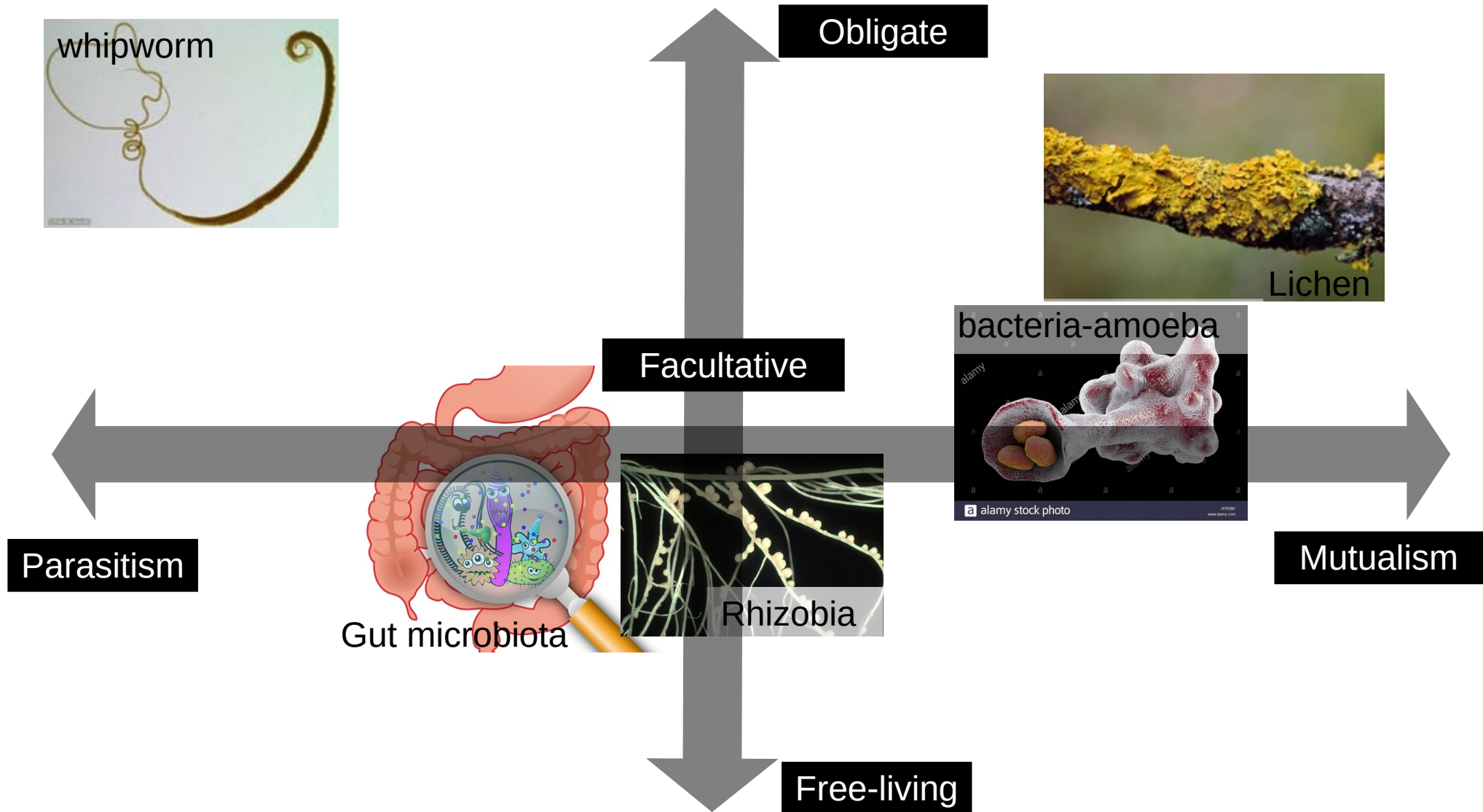


Parasitism



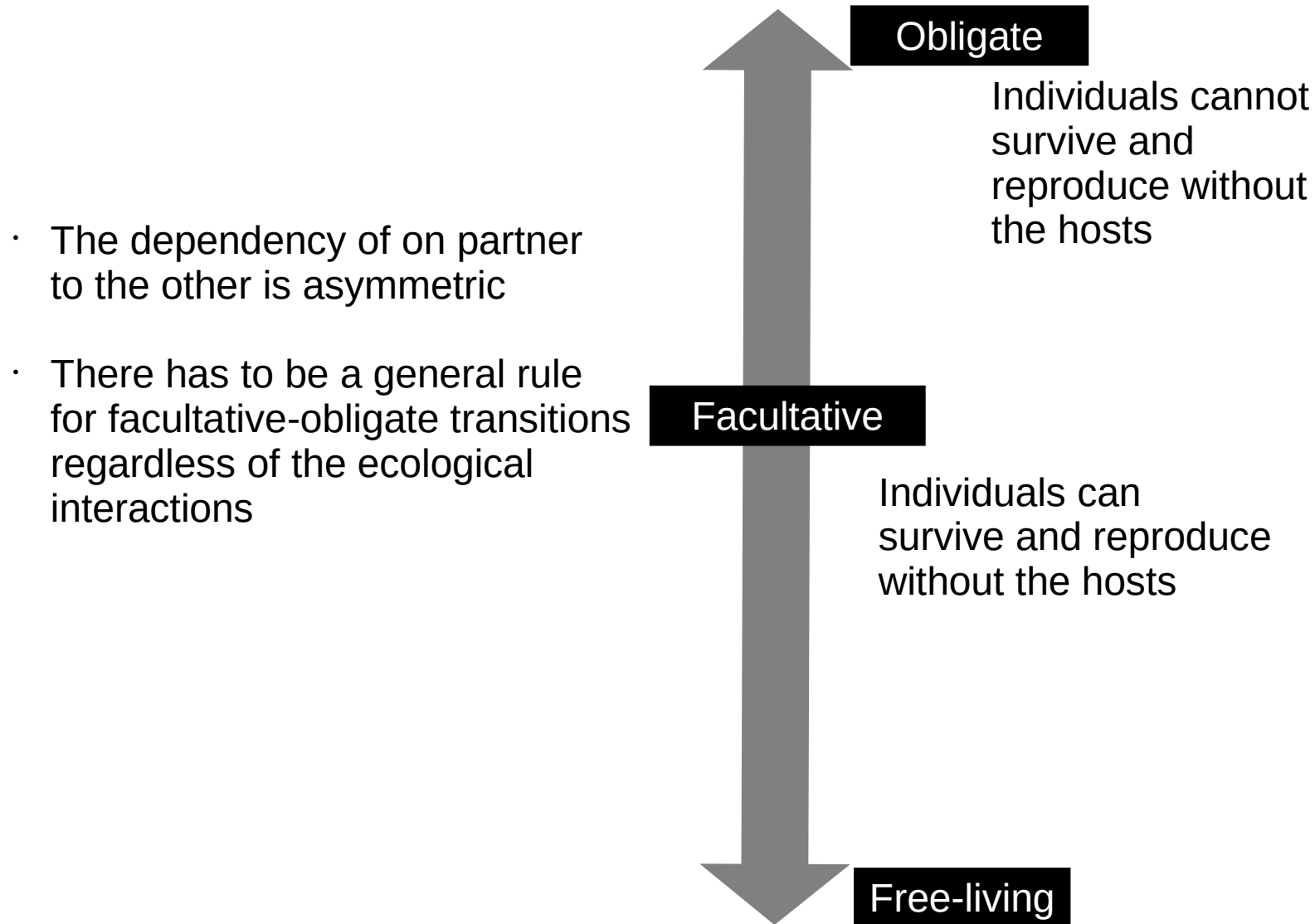
Mutualism

# The diverse world of symbiosis

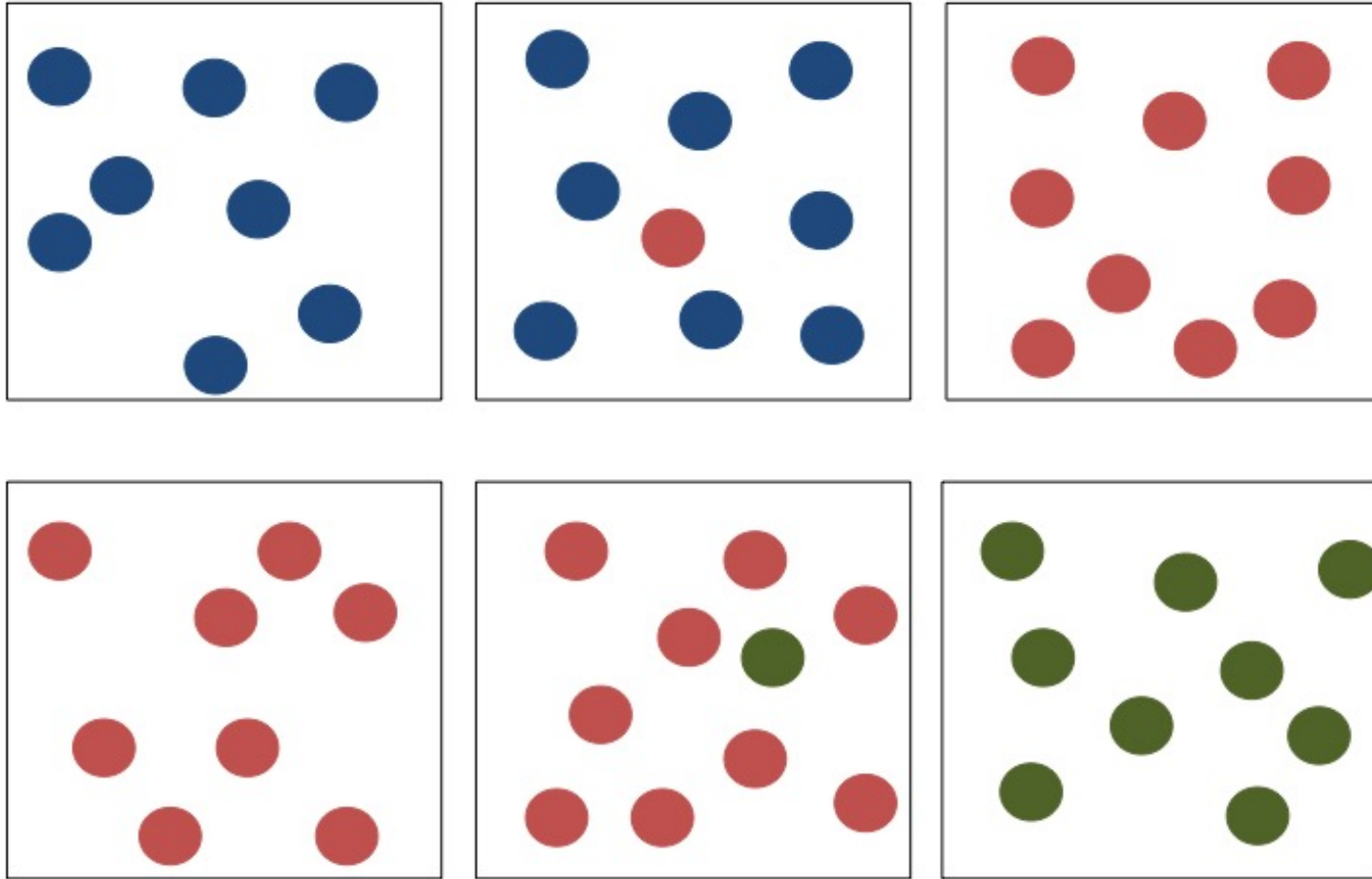




# Obligate symbiosis is an evolutionary riddle



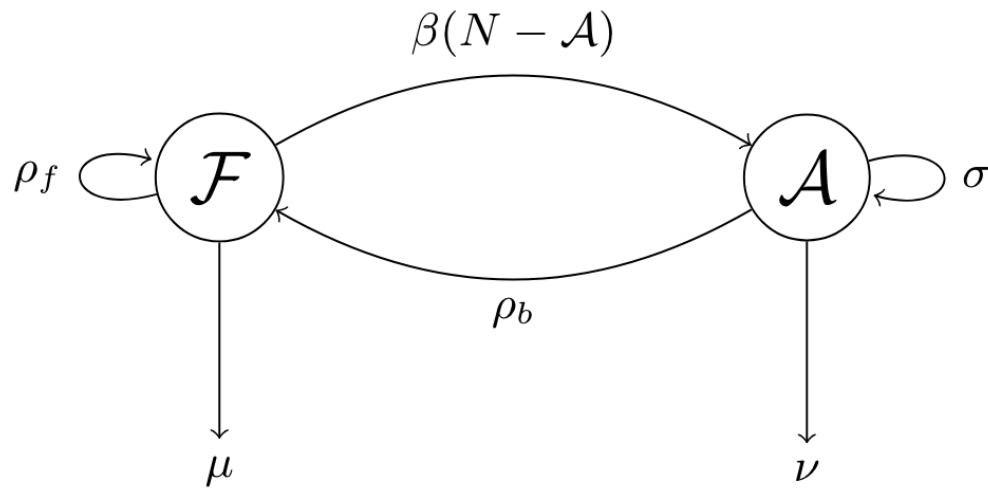
# Adaptive dynamics approach



Evolutionary stable strategy: the strategy once adopted by a resident cannot be invaded by any mutant

# Model with fixed host dynamics

Ecological dynamics

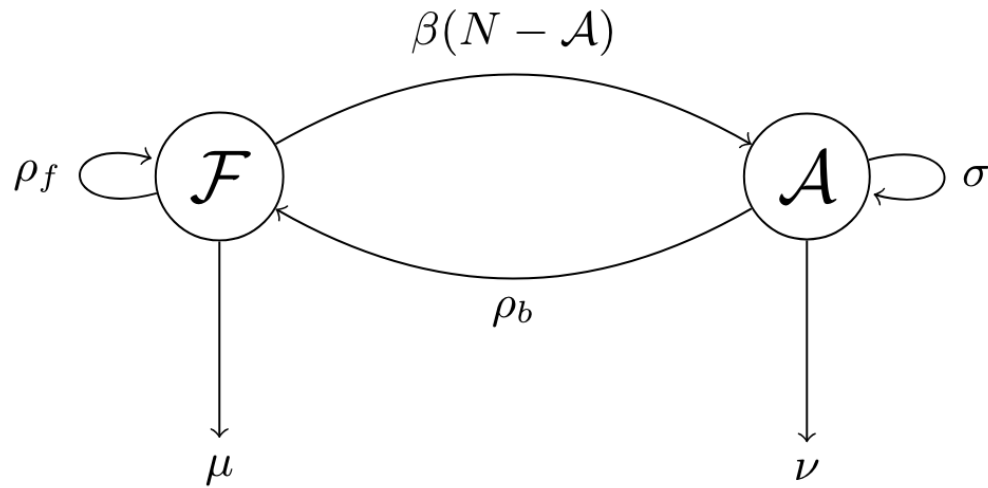


$$\frac{d\mathcal{F}}{dt} = \rho_f \mathcal{F} + \rho_b \mathcal{A} - \beta(N - \mathcal{A})\mathcal{F} - \mu(1 + c\mathcal{F})\mathcal{F}$$

$$\frac{d\mathcal{A}}{dt} = \beta(N - \mathcal{A})\mathcal{F} + \sigma \mathcal{A} - \nu \mathcal{A}$$

# Model with fixed host dynamics

Ecological dynamics



$$\frac{d\mathcal{F}}{dt} = \rho_f \mathcal{F} + \rho_b \mathcal{A} - \beta(N - \hat{\mathcal{A}}) \mathcal{F} - \mu(1 + c\mathcal{F}) \mathcal{F}$$

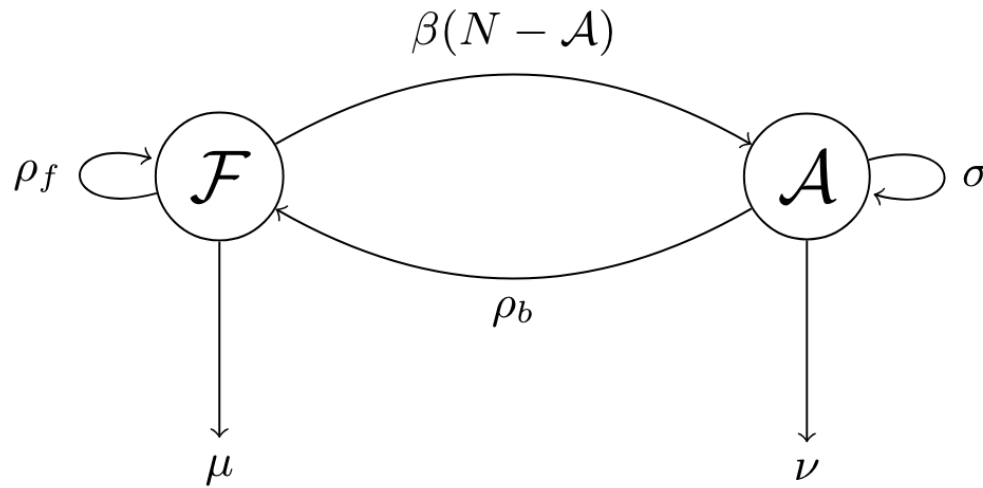
$$\frac{d\mathcal{A}}{dt} = \beta(N - \hat{\mathcal{A}}) \mathcal{F} + \sigma \mathcal{A} - \nu \mathcal{A}$$

Reproduction ratio

$$R_0 = \frac{1}{\beta(N - \hat{\mathcal{A}}) + (1 + c\hat{\mathcal{F}})\mu} \left( \rho_f + \beta \frac{\rho_b(N - \hat{\mathcal{A}})}{\nu - \sigma} \right)$$

# Model with fixed host dynamics

Ecological dynamics



$$\frac{d\mathcal{F}}{dt} = \rho_f \mathcal{F} + \rho_b \mathcal{A} - \beta(N - \hat{\mathcal{A}}) \mathcal{F} - \mu(1 + c\mathcal{F}) \mathcal{F}$$

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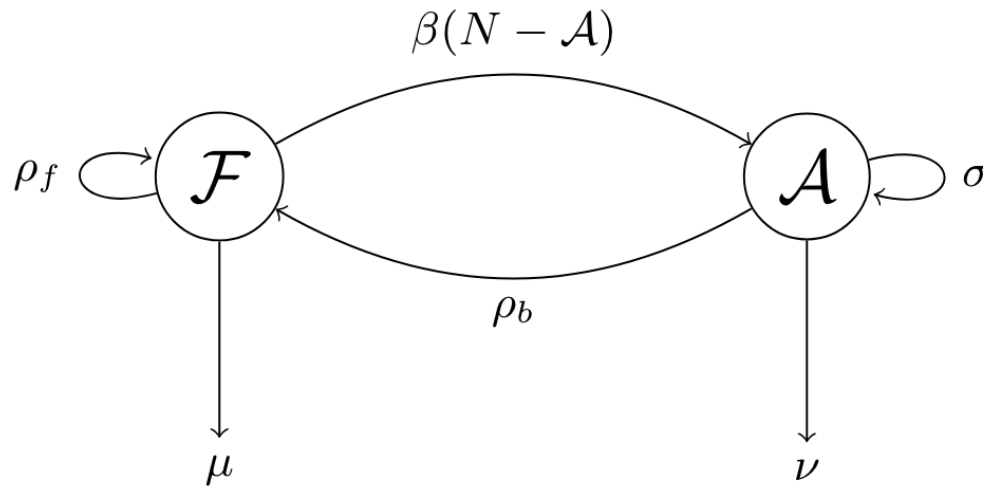
Duration in  
the free-living state

Bound  
component

Free  
component

# Model with fixed host dynamics

Ecological dynamics



$$\frac{d\mathcal{F}}{dt} = \rho_f \mathcal{F} + \rho_b \mathcal{A} - \beta(N - \hat{\mathcal{A}}) \mathcal{F} - \mu(1 + c\mathcal{F}) \mathcal{F}$$

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Reproduction ratio

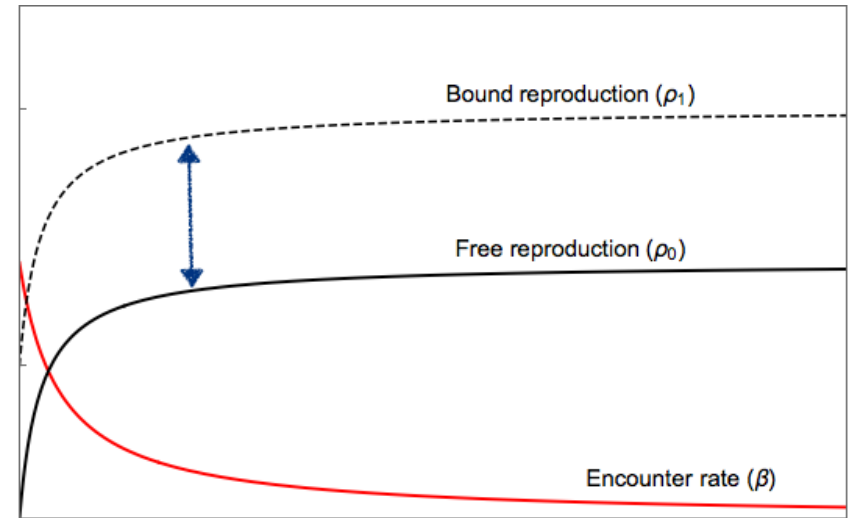
$$R_0 = \frac{1}{\beta(N - \hat{\mathcal{A}}) + (1 + c\hat{\mathcal{F}})\mu} \left( \rho_f + \beta \frac{\rho_b(N - \hat{\mathcal{A}})}{\nu - \sigma} \right)$$

Duration in the free-living state

Bound component

Free component

Trade-off



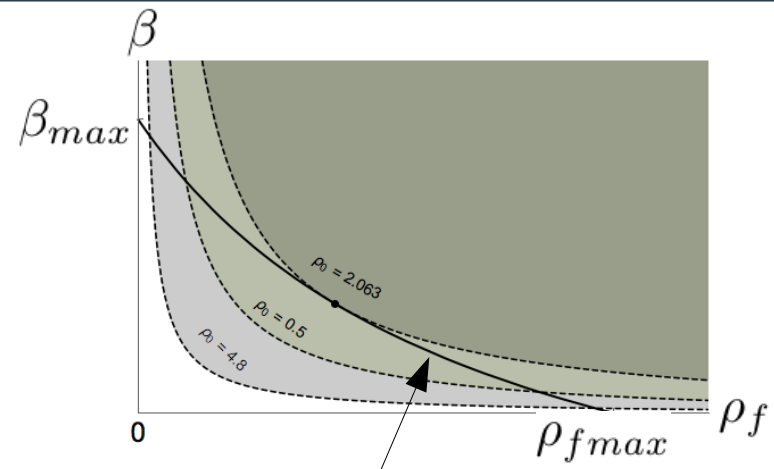
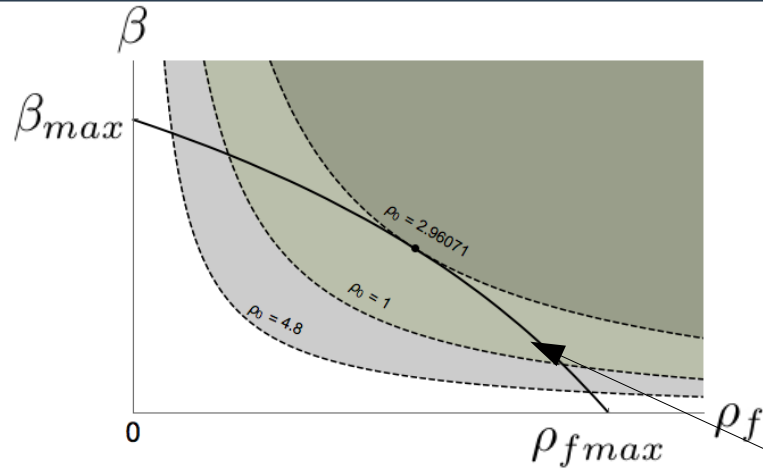
Underlying physiological trait

$$\rho_f(x) = \frac{\rho_{fmax}x}{\sigma x + 1}$$

$$\rho_b(x) = \rho_f(x) + b$$

$$\beta(x) = \frac{\beta_{max}}{\alpha x + 1}$$

# Model with fixed host dynamics



Underlying physiological trait

$$\frac{d\mathcal{F}}{dt} = \rho_f \mathcal{F} + \rho_b \mathcal{A} - \beta(N - \hat{\mathcal{A}})\mathcal{F} - \mu(1 + c\mathcal{F})\mathcal{F}$$

$$\frac{d\mathcal{A}}{dt} = \beta(N - \hat{\mathcal{A}})\mathcal{F} + \sigma \mathcal{A} - \nu \mathcal{A}$$

Reproduction ratio

$$R_0 = \frac{1}{\beta(N - \hat{\mathcal{A}}) + (1 + c\hat{\mathcal{F}})\mu} \left( \rho_f + \beta \frac{\rho_b(N - \hat{\mathcal{A}})}{\nu - \sigma} \right) > 1$$

Duration in the free-living state

Bound component

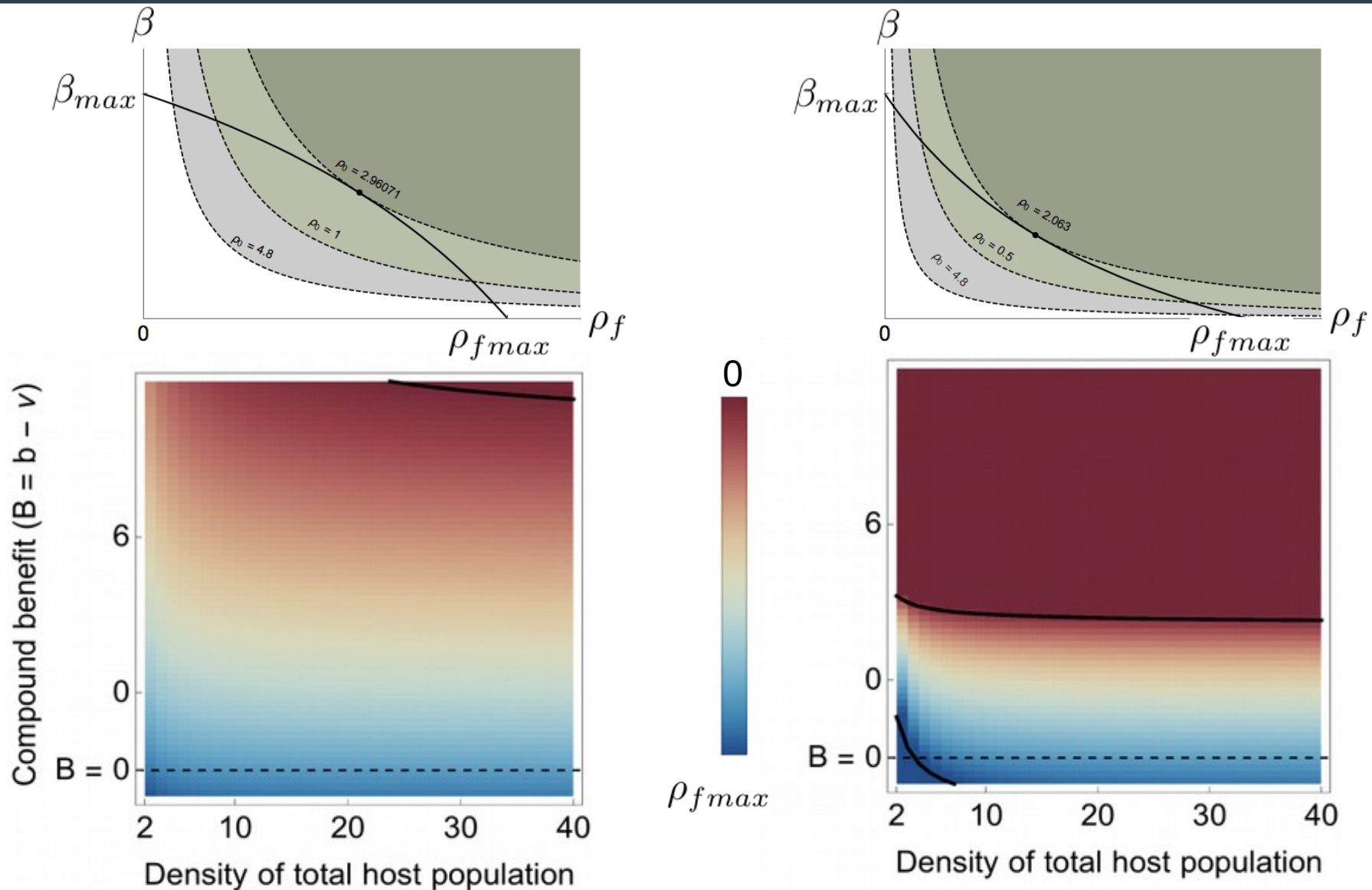
Free component

$$\rho_f(x) = \frac{\rho_{fmax}x}{\sigma x + 1}$$

$$\rho_b(x) = \rho_f(x) + b$$

$$\beta(x) = \frac{\beta_{max}}{\alpha x + 1}$$

# On the difficult transitions from free-living organisms to obligate symbiosis





# Simplicity: the pros and cons

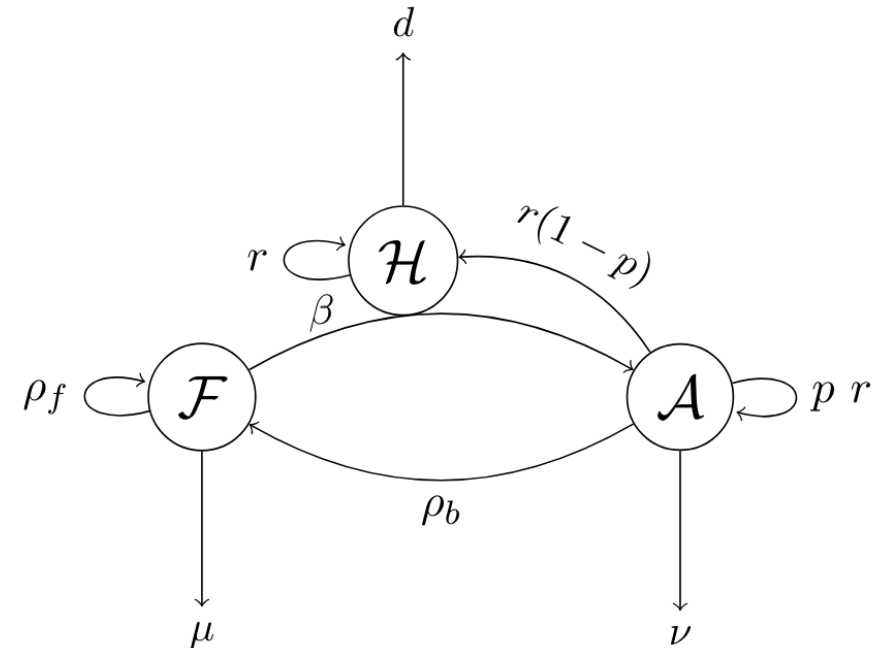
- **What I find exciting about this model:**
  - The effects of the trade-off and the ecological feedback are disentangled
  - Simple model but interesting and useful biological insights
- **Limitations:**
  - Host dynamics are not taken into account
  - Analysis using specific and simple trade-off
  - The evolution toward obligate symbiosis is not only about losing independent reproduction but also about gaining adaptation.

# Building on the simple model

$$\frac{d\mathcal{F}}{dt} = \rho_f \frac{\kappa}{1 + \phi\mathcal{F}} \mathcal{F} + \rho_b \mathcal{A} - \beta \mathcal{F} \mathcal{H} - \mu \mathcal{F}$$

$$\frac{d\mathcal{A}}{dt} = \beta \mathcal{F} \mathcal{H} - \nu(1 + (\mathcal{A} + \mathcal{H})\gamma) \mathcal{A} + rp\mathcal{A}$$

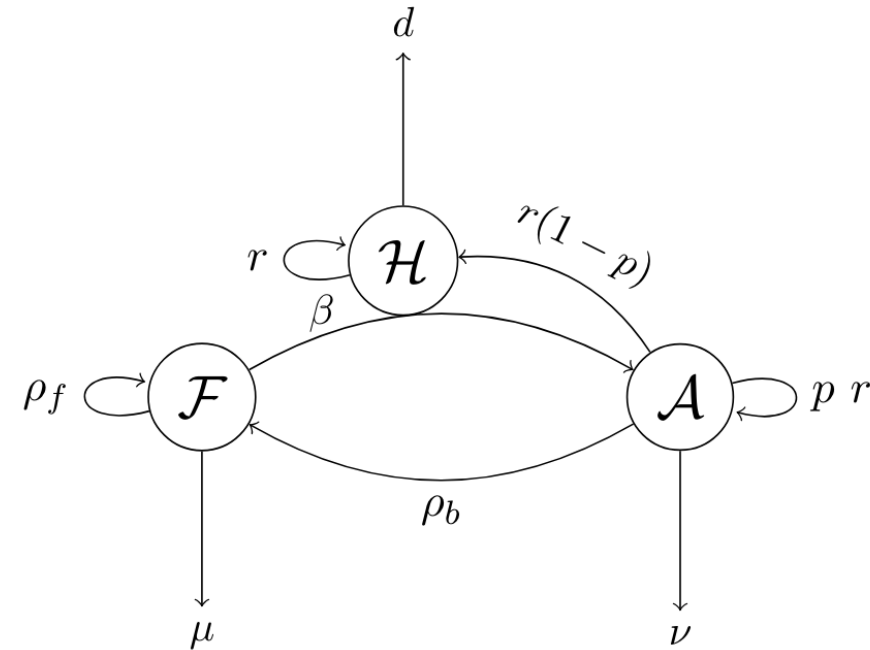
$$\frac{d\mathcal{H}}{dt} = r(1 - p)\mathcal{A} + r\mathcal{H} - \beta \mathcal{F} \mathcal{H} - d(1 + (\mathcal{H} + \mathcal{A})\zeta) \mathcal{H}$$



# Building on the simple model

$$\frac{d\mathcal{F}}{dt} = \rho_f \frac{\kappa}{1 + \phi \hat{\mathcal{F}}} \mathcal{F} + \rho_b \mathcal{A} - \beta \mathcal{F} \hat{\mathcal{H}} - \mu \mathcal{F}$$

$$\frac{d\mathcal{A}}{dt} = \beta \mathcal{F} \hat{\mathcal{H}} - \nu (1 + (\hat{\mathcal{A}} + \hat{\mathcal{H}}) \gamma) \mathcal{A} + r p \mathcal{A}$$



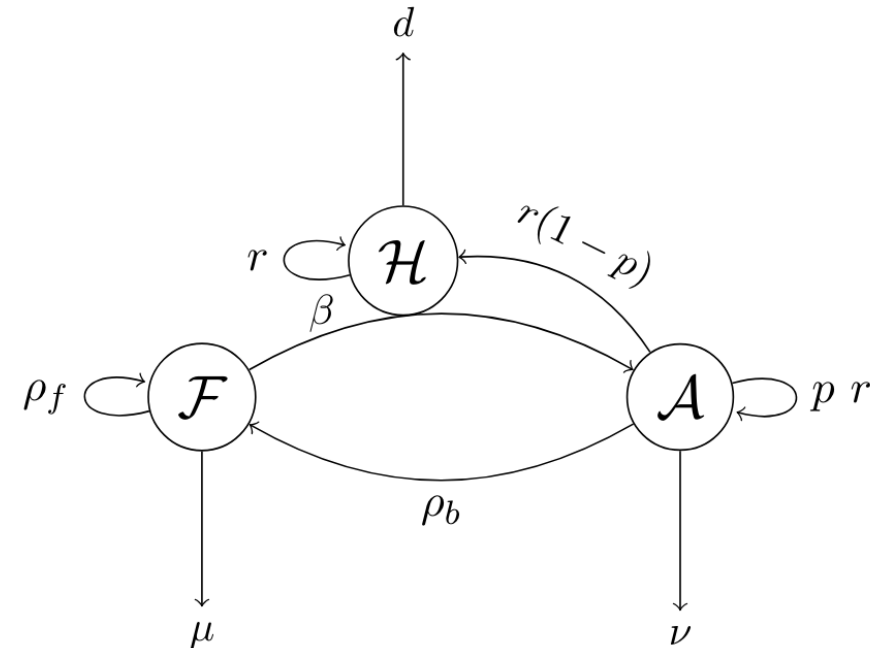
Neutral mutant has zero invasion fitness

$$\left( \frac{\kappa \rho_f}{(1 + \phi \hat{\mathcal{F}}) \mu} - 1 \right) \left( \frac{r p}{(1 + \gamma (\hat{\mathcal{A}} + \hat{\mathcal{H}})) \nu} - 1 \right) = \left( \frac{r p}{(1 + (\hat{\mathcal{A}} + \hat{\mathcal{H}}) \gamma) \nu} + \frac{\rho_b}{(1 + (\hat{\mathcal{A}} + \hat{\mathcal{H}}) \gamma) \nu} - 1 \right) \frac{\hat{\mathcal{H}} \beta}{\mu}$$

# Building on the simple model

$$\frac{d\mathcal{F}}{dt} = \rho_f \frac{\kappa}{1 + \phi \hat{\mathcal{F}}} \mathcal{F} + \rho_b \mathcal{A} - \beta \mathcal{F} \mathcal{H} - \mu \mathcal{F}$$

$$\frac{d\mathcal{A}}{dt} = \beta \mathcal{F} \mathcal{H} - \nu (1 + (\hat{\mathcal{A}} + \hat{\mathcal{H}}) \gamma) \mathcal{A} + r p \mathcal{A}$$



Neutral mutant has zero invasion fitness

$$\left( R_{ff}^{-1} \right) \left( R_{aa}^{-1} \right) = \left( R_{aa} + R_{af}^{-1} \right) \mathcal{T}$$

Reproduction ratio of  
free-living individual

Reproduction ratio of  
vertically transmitted individual

Reproduction ratio of  
horizontally transmitted  
individual

Effective number  
of host encounter

# Insights from analysing invasion fitness

1. When can a mutant with small adaptation  $x_{mut} \approx 0$  to the symbiotic lifestyle invade a resident population without any adaptation  $x_{res} = 0$ , hence  $R_{ff}(x_{res}) = 0$  ?
2. If a singular strategy exists where adaptation to the symbiotic lifestyle is sufficient  $R_{af}(x_{ss}) > 0$ , is such a strategy at the minimum or maximum of the fitness landscape?
3. What are the effects of the ecological interactions on the evolution of the adaptation to the symbiotic lifestyle?

# 1. Evolution of small symbiotic adaptation

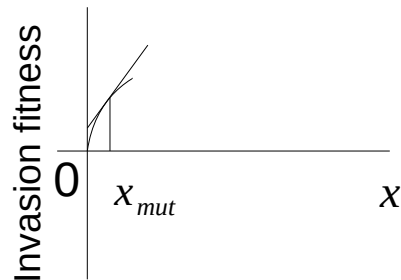
- A mutant with small adaptation to the symbiotic lifestyle invades a resident population without any adaptation when the selection gradient is positive

$$\left. \frac{1}{R_{ff} - 1} \frac{\partial R_{ff}}{\partial x_{mut}} - \left( \frac{1}{R_{af} + R_{aa} - 1} \frac{\partial R_{af}}{\partial x_{mut}} \right) \right|_{\substack{x_{res}=0 \\ x_{mut} \approx 0}} > 0$$

Assumptions:

$$- \frac{\partial R_{aa}}{\partial x_{mut}} = 0; \frac{\partial T}{\partial x_{mut}} = 0$$

- Very small vertical transmission

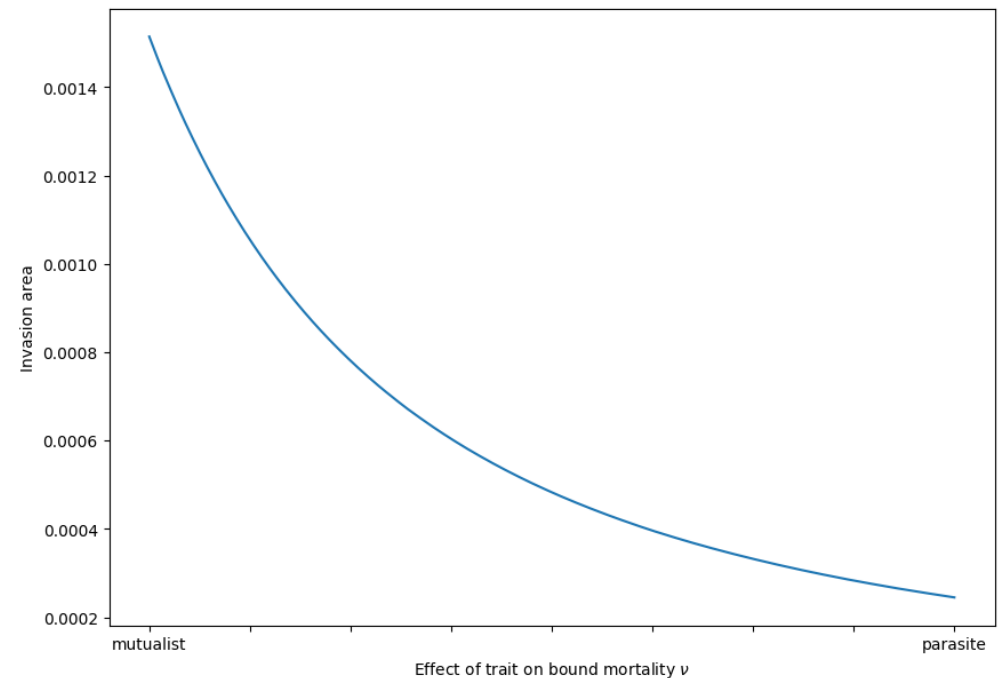
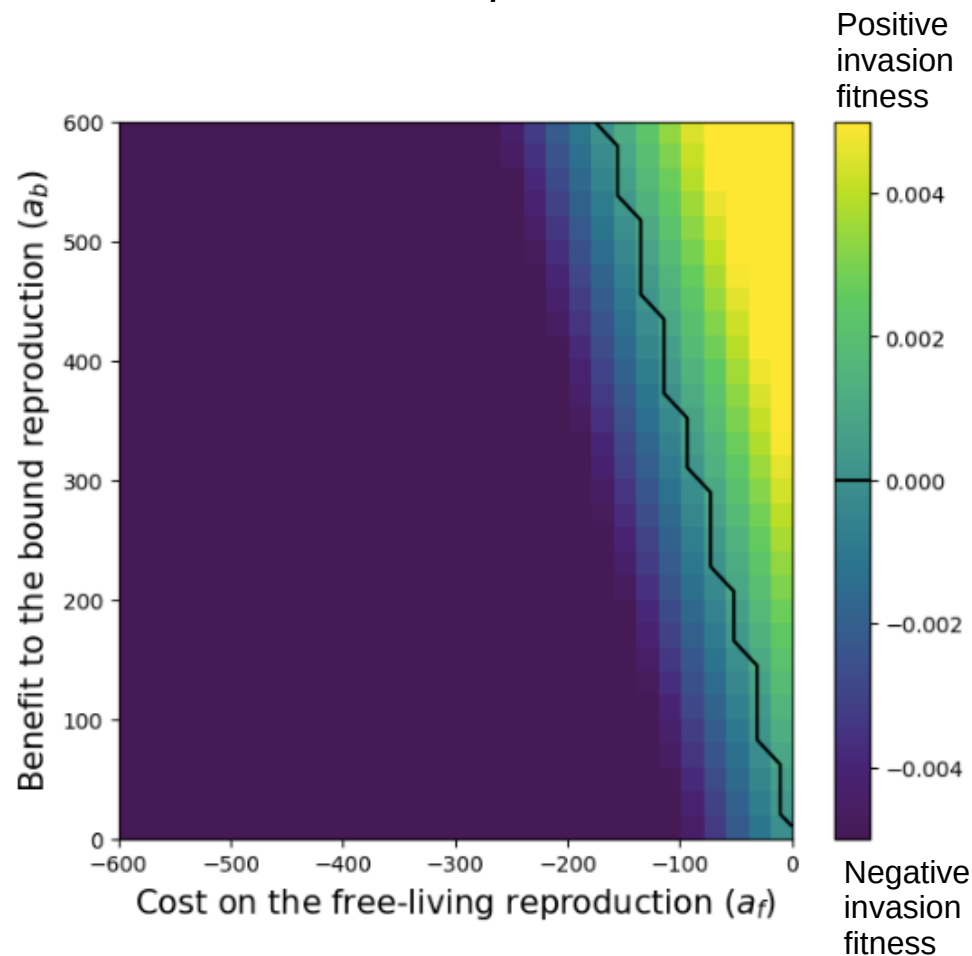


- With local analysis around the resident value, any function can be linearised. What matters is the coefficients.

# Evolution of small symbiotic adaptation

$a_f$  Coefficient for  $R_{ff}$  linearised function  $< 0$

$a_b$  Coefficient for  $R_{af}$  linearised function  $> 0$



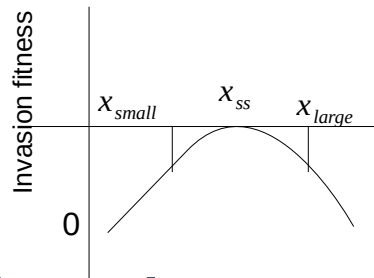
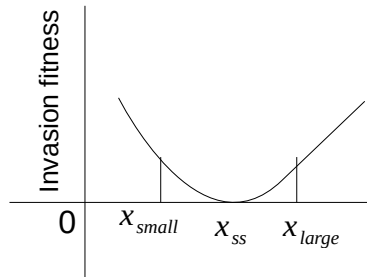
## 2. The singular strategy has to satisfy

- Selection gradient is zero

$$\left( \frac{1}{R_{ff} - 1} \frac{\partial R_{ff}}{\partial x_{mut}} = \frac{1}{R_{aa} + R_{af} - 1} \frac{\partial R_{af}}{\partial x_{mut}} \right) \Big|_{x_{mut}=x_{res}=x_{ss}}$$

Assumptions:

- $\frac{\partial R_{aa}}{\partial x_{mut}} = 0; \frac{\partial T}{\partial x_{mut}} = 0$
- Very small vertical transmission



- Condition for minimum and maximum

- ♦ ~~Second derivative of the fitness function~~ Selection gradients on neighbour mutants
- ♦ Minimum singular strategy  $\rightarrow$  polymorphism
- ♦ Maximum singular strategy  $\rightarrow$  monomorphism



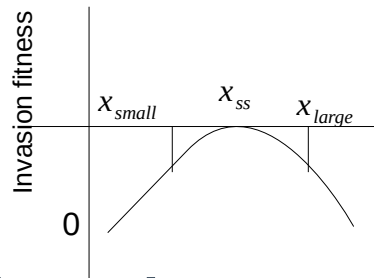
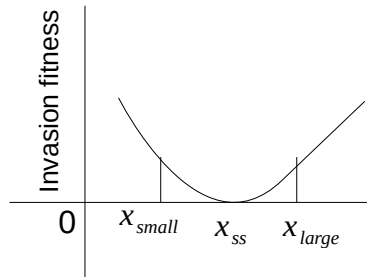
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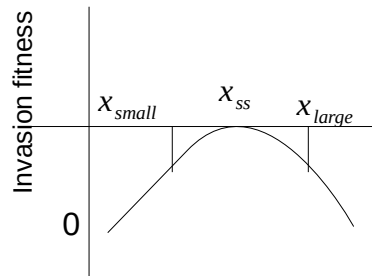
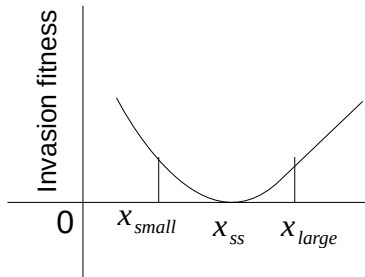
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- Selection gradient is zero

$$\left( \frac{1}{R_{ff} - 1} \frac{\partial R_{ff}}{\partial x_{mut}} = \frac{1}{R_{aa} + R_{af} - 1} \frac{\partial R_{af}}{\partial x_{mut}} \right) \Big|_{x_{mut}=x_{res}=x_{ss}}$$

Assumptions:

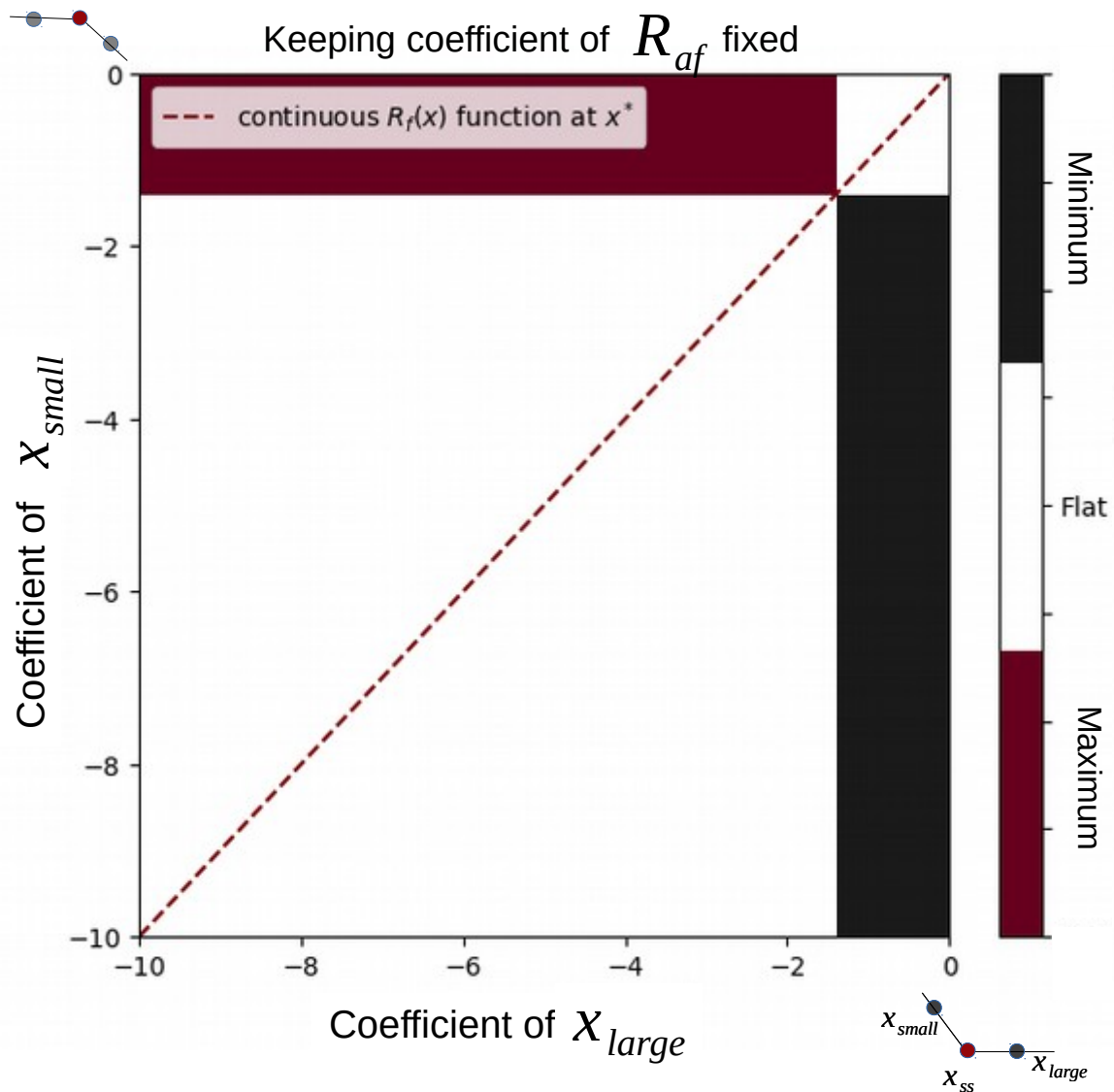
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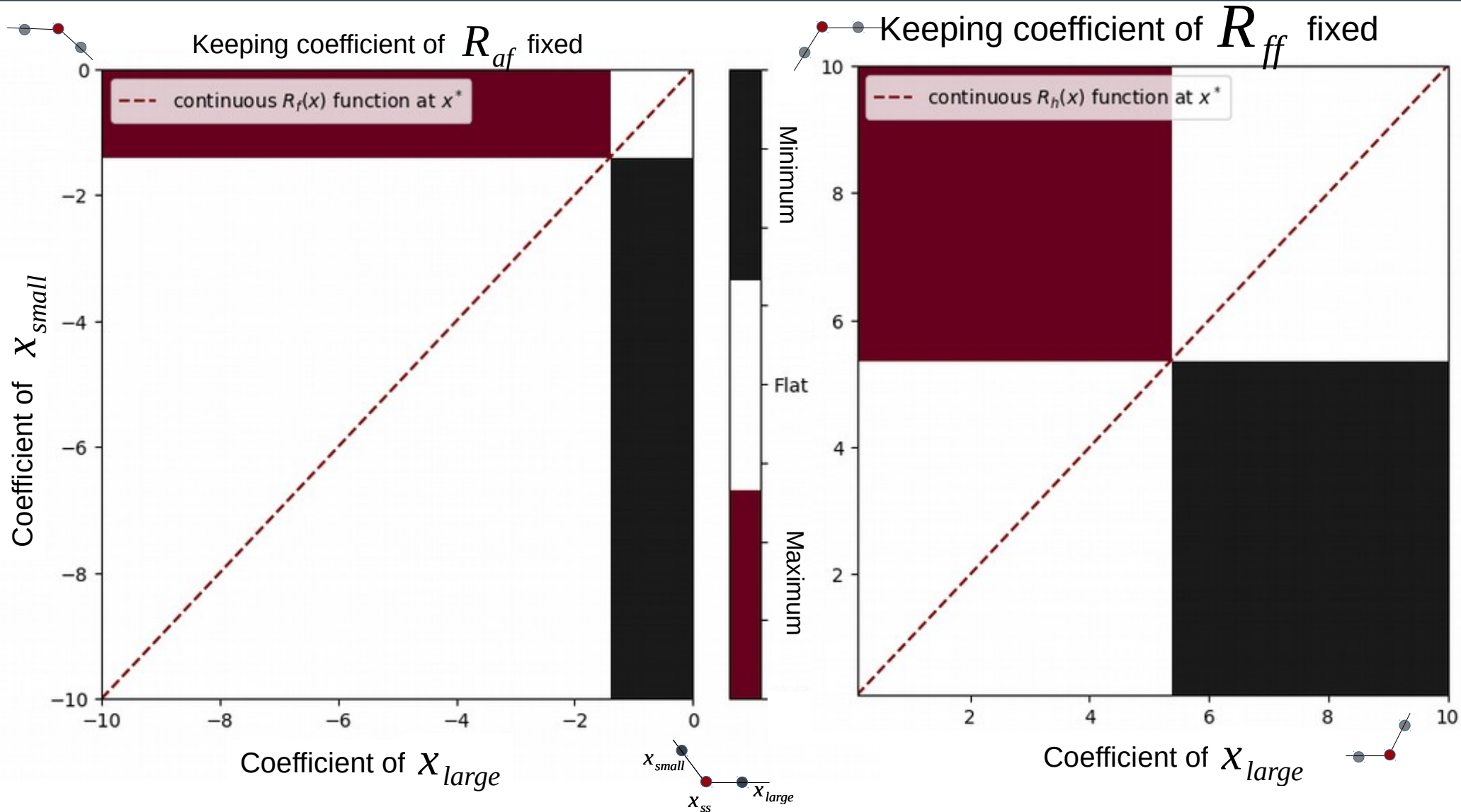
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## 2. Condition for minimum and maximum



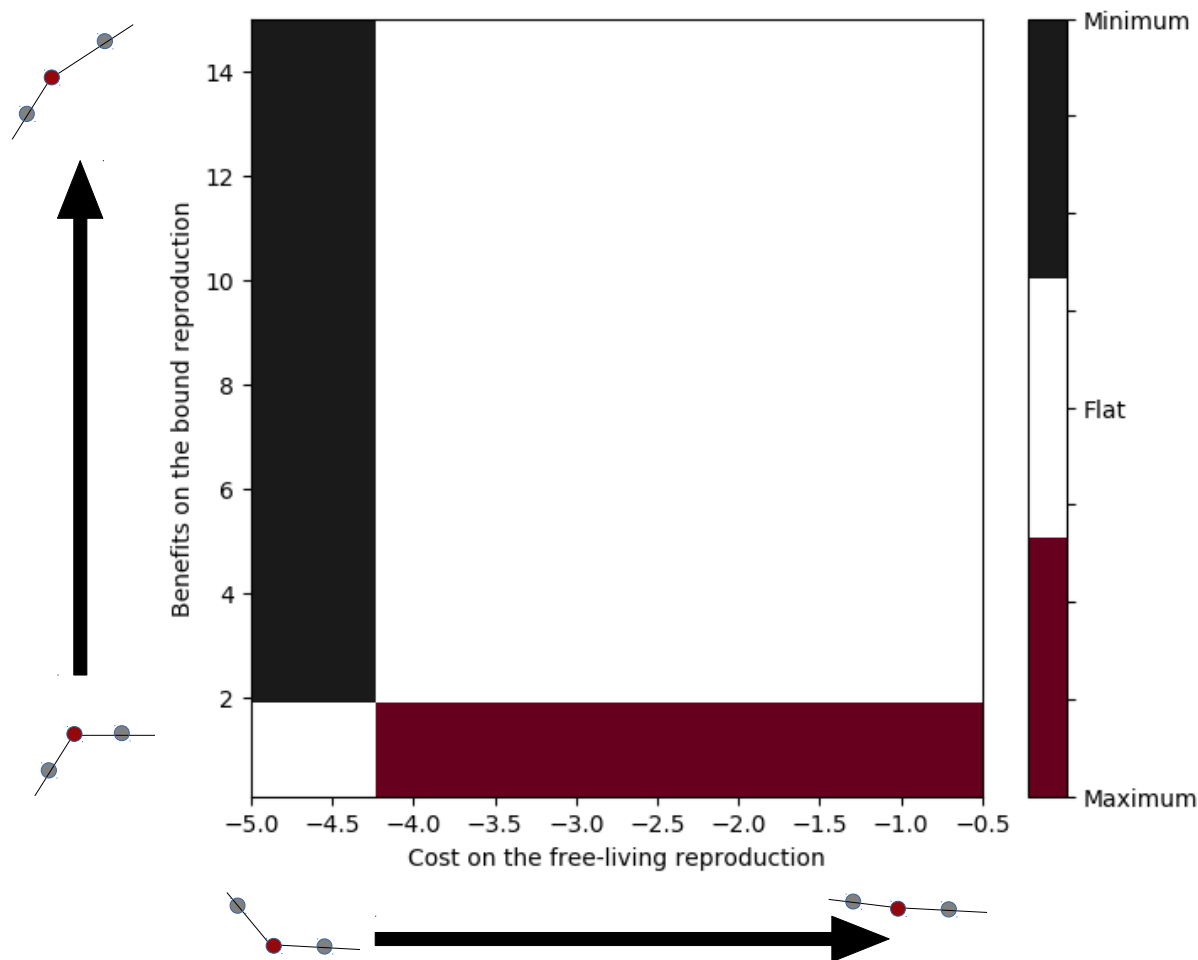
## 2. Condition for minimum and maximum



## 2. Condition for minimum and maximum

A saturated to continuously increasing benefit

A saturated to continuously decreasing benefit

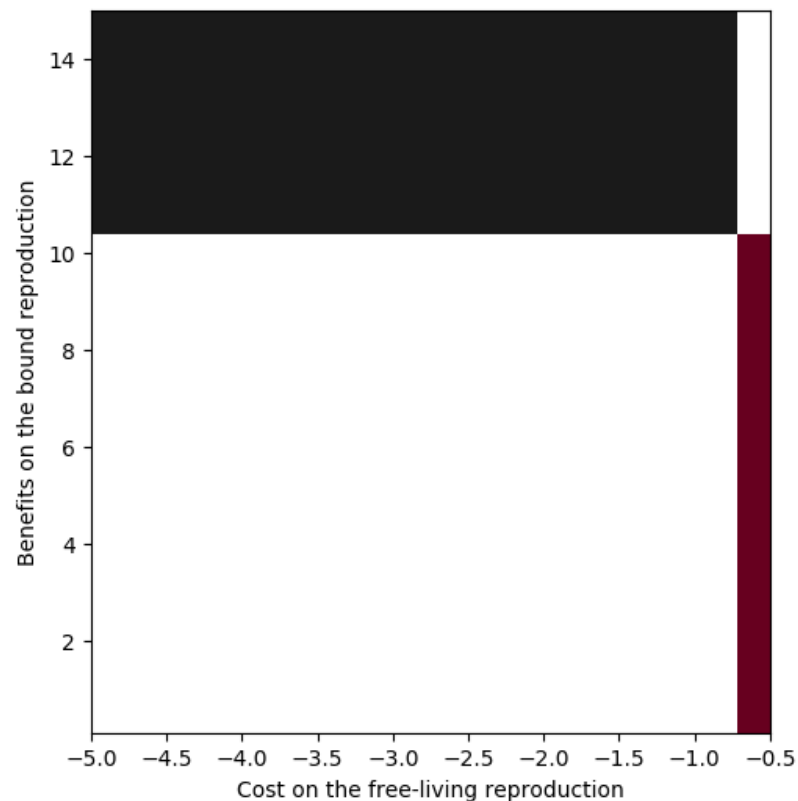


# 3. Effect of ecological interactions

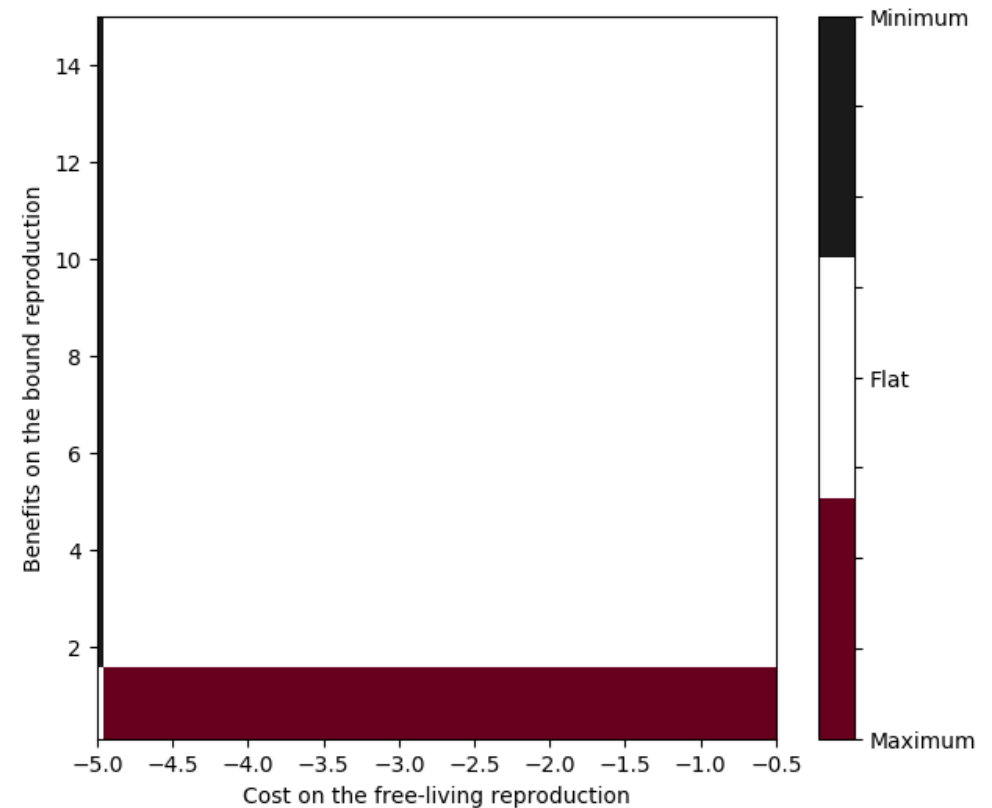
A saturated to continuously increasing benefit

A saturated to continuously decreasing benefit

Parasitism



Mutualism



# Exciting results

- Different production ratios for different reproduction strategies are disentangled
- Useful insights can be obtained from the analysis of invasion at the boundary and the local singular strategy
- Effect of the ecological interactions can be observed without specifying trade-off functions
- Understand the limit of analysis when specific trade-off is not stated

Thank you for your attention!