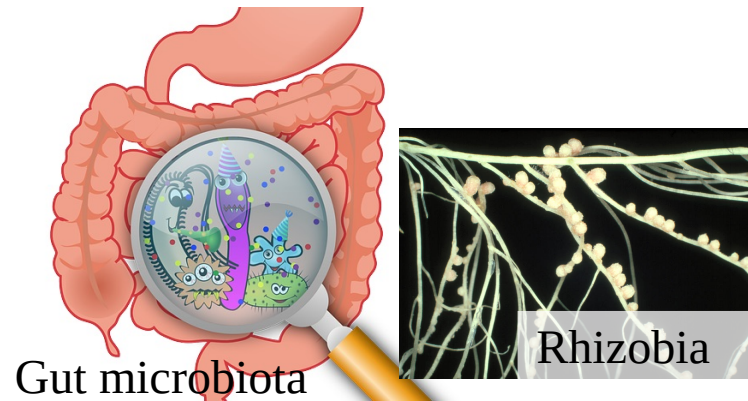


On the evolutionary transitions from free-living organisms to obligate symbioses

Linh-Phuong NGUYEN
Minus van Baalen

MMEE – Lyon, July 2019

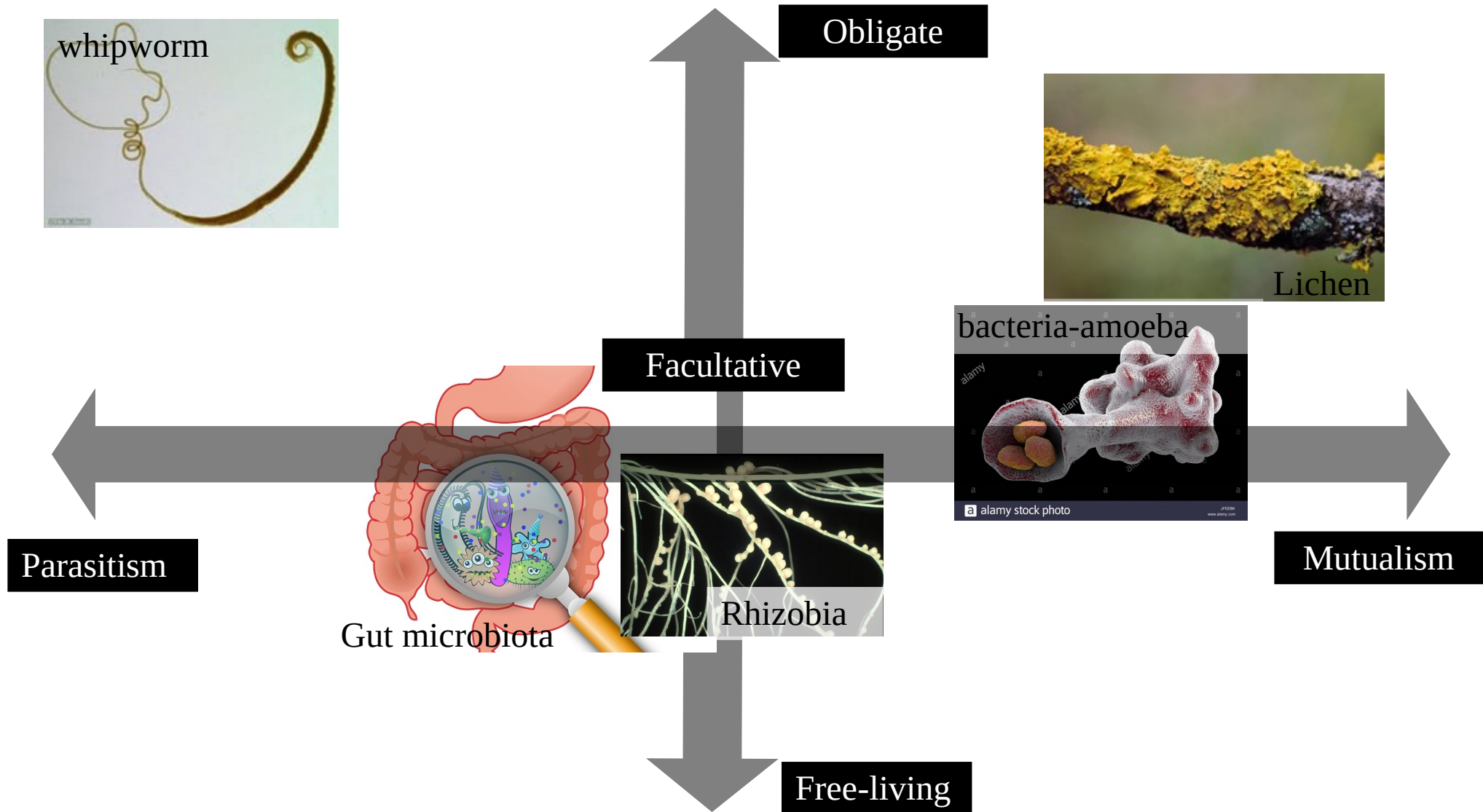
The diverse world of symbiosis



The diverse world of symbiosis

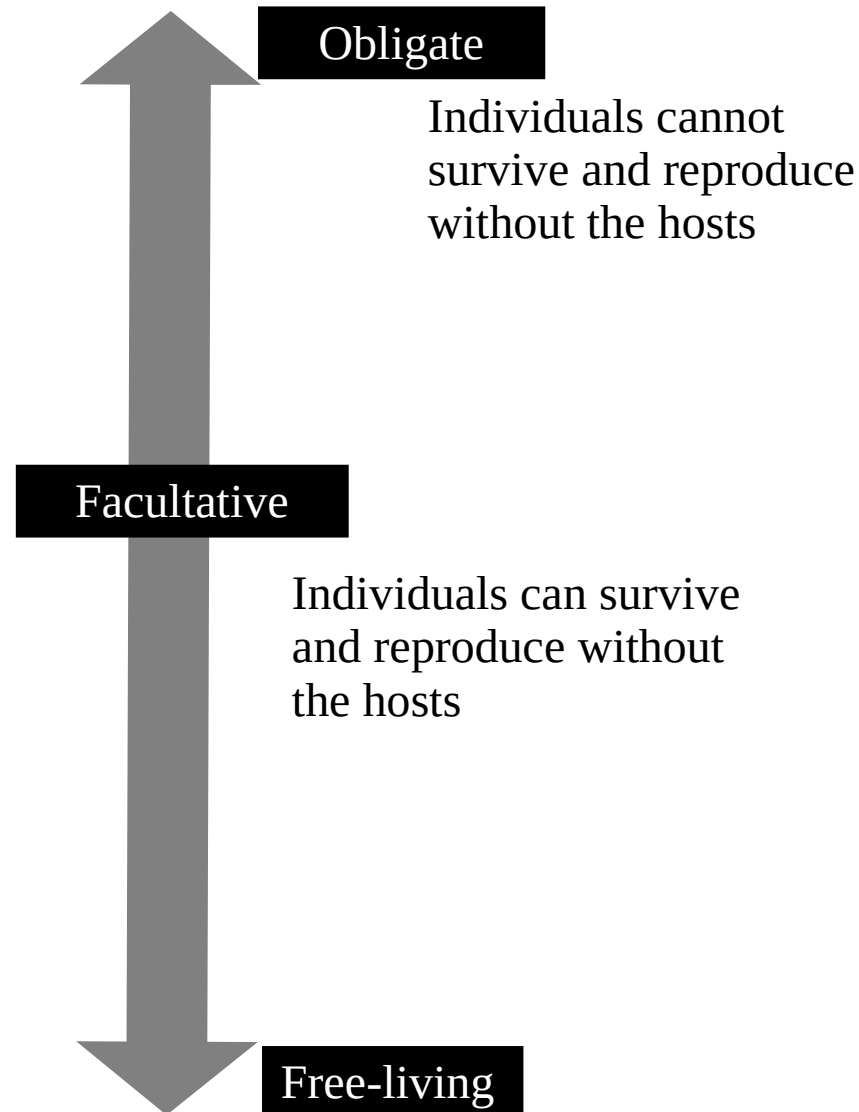


The diverse world of symbiosis

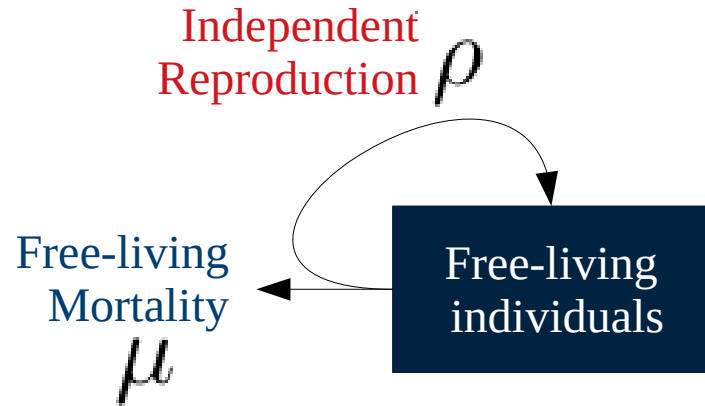


Transition from facultative to obligate symbiosis is an evolutionary riddle

- I will focus on the evolution of one partner (the SYMBIONT) given the ecological dynamics of the other partner (the HOST)
- I will use INDEPENDENT REPRODUCTION as indication of partner dependency

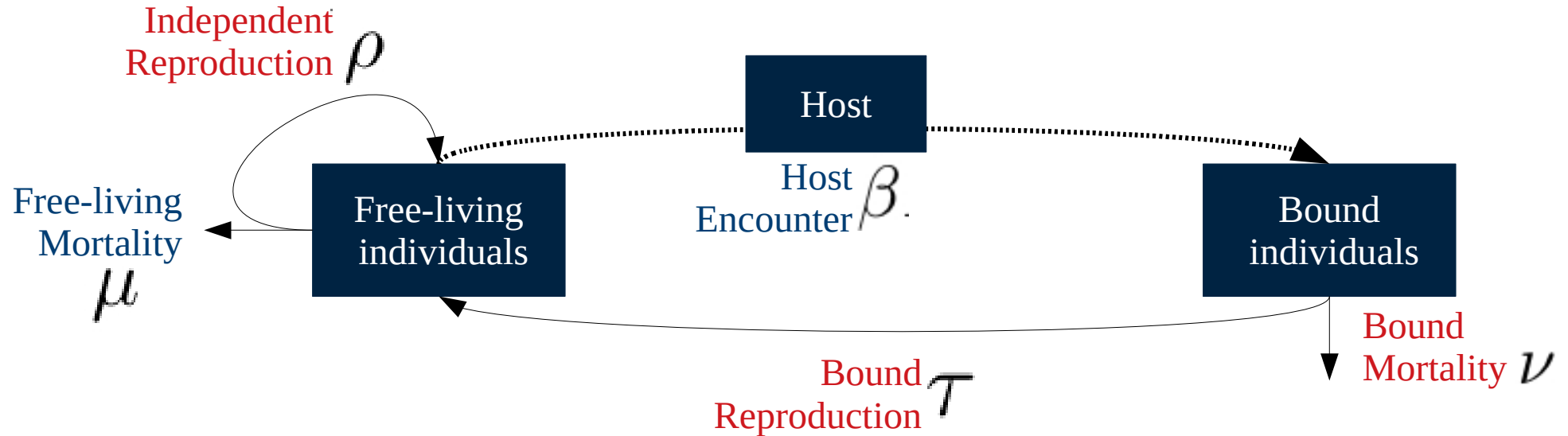


Ecological dynamics of a resident



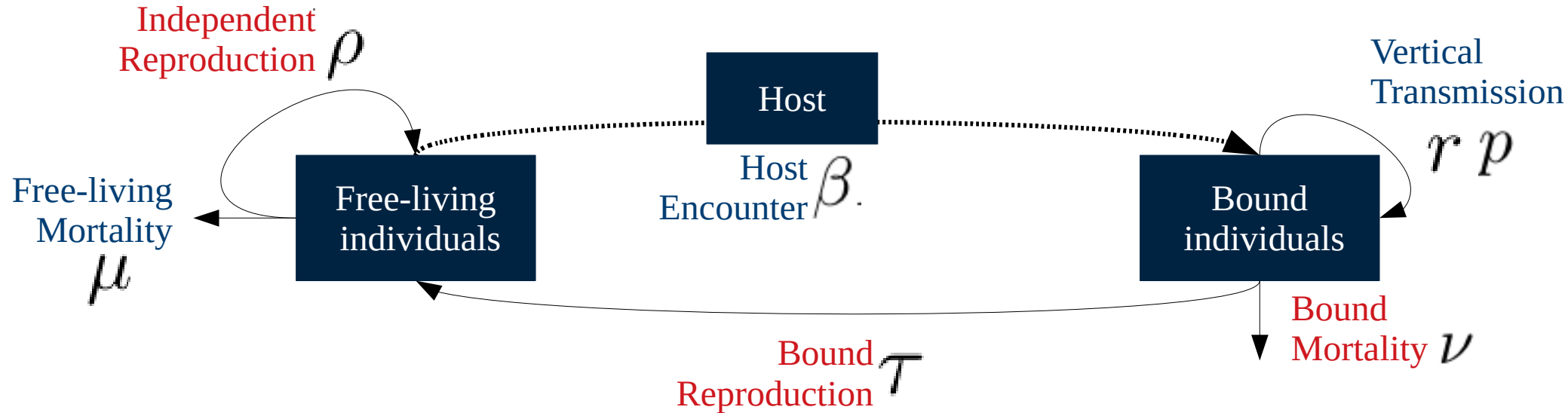
$$\frac{d}{dt} \begin{pmatrix} \mathcal{F} \\ \mathcal{A} \\ \mathcal{H} \end{pmatrix} = \begin{pmatrix} \rho K(\mathcal{F}) - \mu - \beta \mathcal{H} & \tau & 0 \\ \beta \mathcal{H} & p r - \nu N(\mathcal{A}, \mathcal{H}) & 0 \\ -\beta \mathcal{H} & r(1-p) & r - d D(\mathcal{H}, \mathcal{A}) \end{pmatrix} \begin{pmatrix} \mathcal{F} \\ \mathcal{A} \\ \mathcal{H} \end{pmatrix}$$

Ecological dynamics of a resident



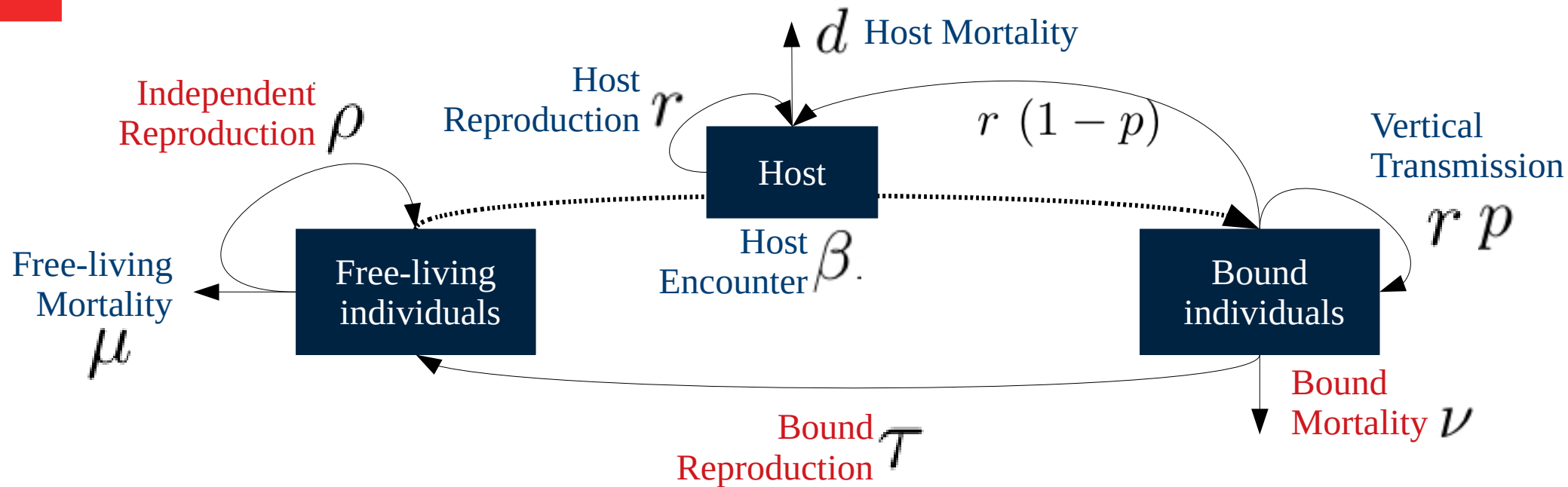
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Ecological dynamics of a resident



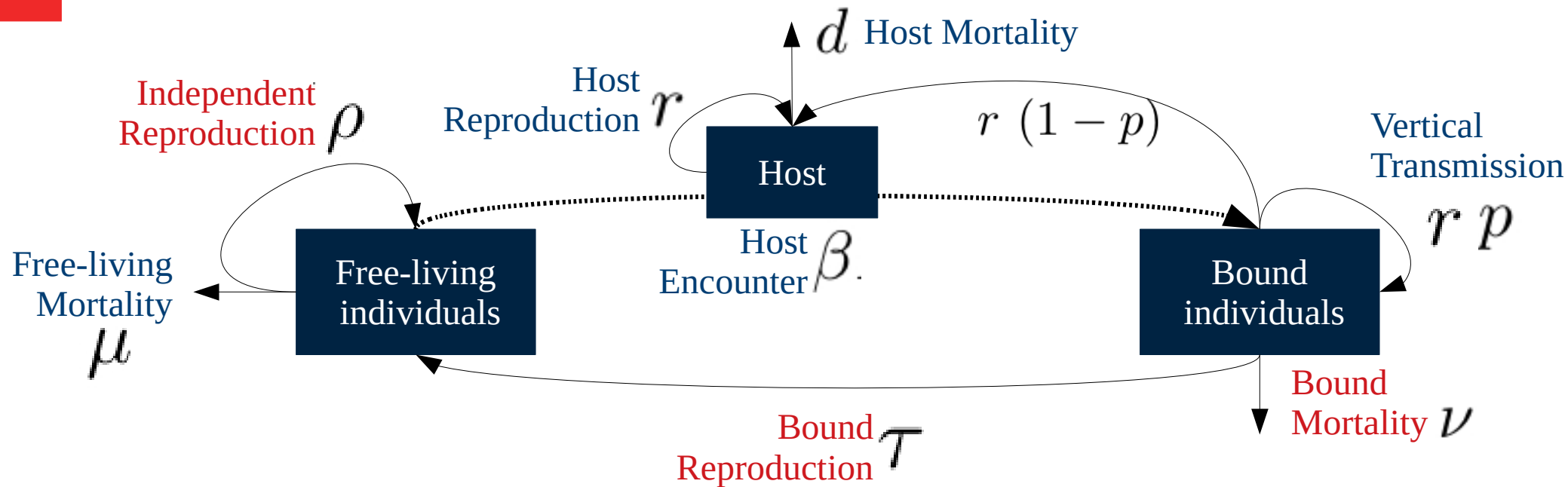
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Ecological dynamics of a resident



$$\frac{d}{dt} \begin{pmatrix} \mathcal{F} \\ \mathcal{A} \\ \mathcal{H} \end{pmatrix} = \begin{pmatrix} \rho K(\mathcal{F}) - \mu - \beta \mathcal{H} & \tau & 0 \\ \beta \mathcal{H} & p r - \nu & 0 \\ -\beta \mathcal{H} & r(1-p) & r - d \end{pmatrix} \begin{pmatrix} \mathcal{F} \\ \mathcal{A} \\ \mathcal{H} \end{pmatrix}$$

Invasion fitness of a mutant



$$\left(\frac{\rho_m}{\mu} K(\hat{\mathcal{F}}) - 1 \right) \left(\frac{p}{\nu_m} \frac{r}{N(\hat{\mathcal{A}}, \hat{\mathcal{H}})} - 1 \right) = \left(\frac{p}{\nu_m} \frac{r}{N(\hat{\mathcal{A}}, \hat{\mathcal{H}})} + \frac{\tau_m}{\nu_m} \frac{1}{N(\hat{\mathcal{A}}, \hat{\mathcal{H}})} - 1 \right) \left(\frac{\beta}{\mu} \hat{\mathcal{H}} \right) < 0$$

R_{ff}
 Free-living
reproduction
ratio

R_{aa}
 Bound
reproduction
ratio
(vertical
transmission)

R_{af}
 Bound
reproduction
ratio
(horizontal
transmission)

\mathcal{T}
 Effective host
encounters

Trade-off among bound reproduction, independent reproduction and bound mortality rate

$$\tau = \theta - \rho^h + \eta(\nu - \nu_0)^g$$

Adaptation to the symbiotic lifestyle imposes a cost on the independent reproduction

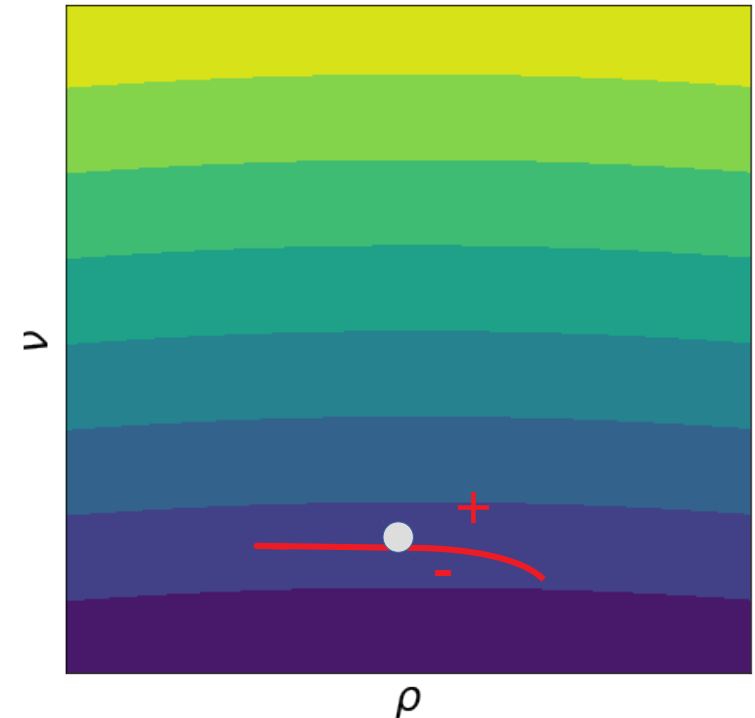
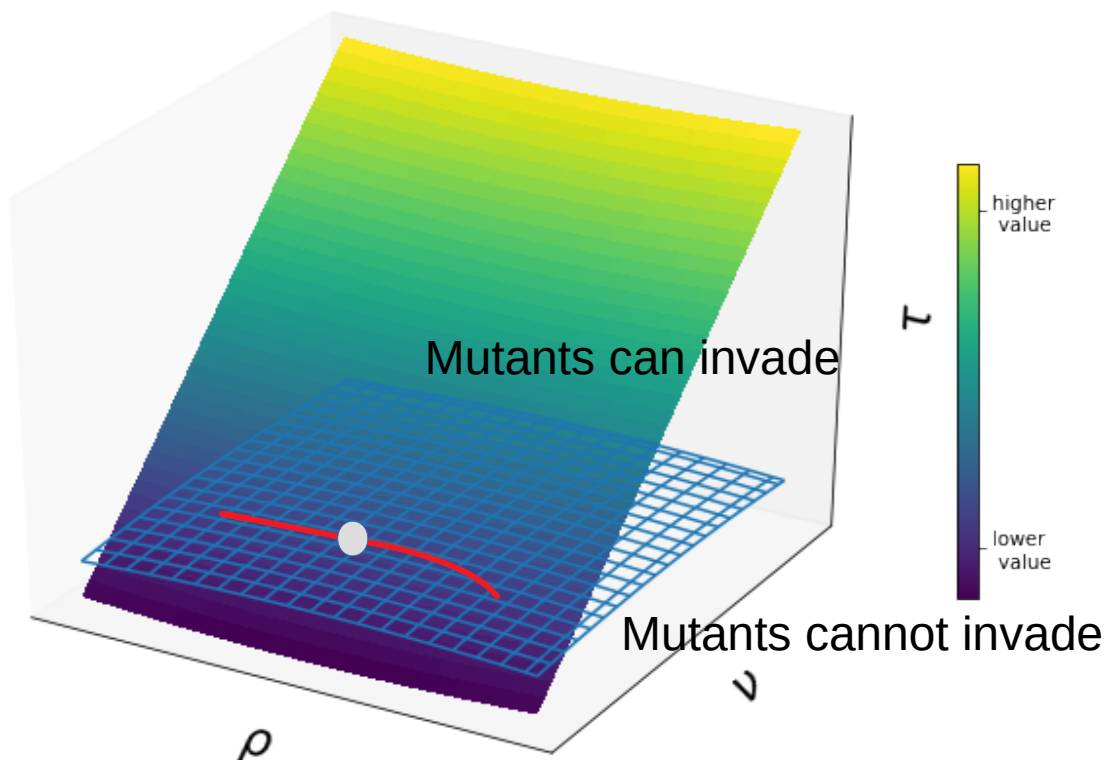
$\eta > 0$: The adaptation increases host mortality rate (parasitic relationship)

$\eta < 0$: The adaptation reduce host mortality rate
(mutualistic relationship via host protection)

Trade-off and invasion fitness can be represented as manifolds

$$\tau = \theta - \rho^h + \eta(\nu - \nu_0)^g$$

$$\tau_m > \frac{N(\hat{\mathcal{A}}, \hat{\mathcal{H}})\nu_m - pr}{\beta\hat{\mathcal{H}}} \left(\beta\hat{\mathcal{H}} + \mu - K(\hat{\mathcal{F}})\rho_m \right)$$

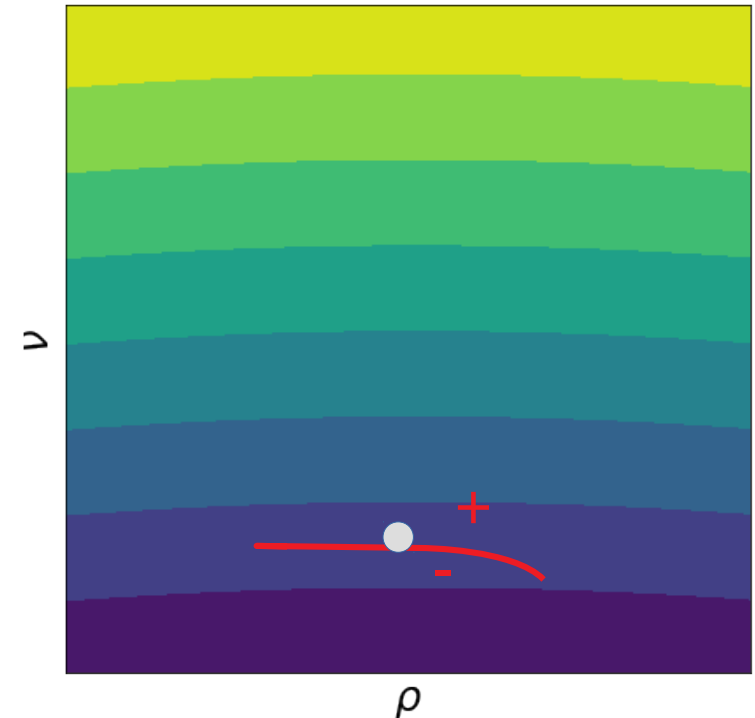
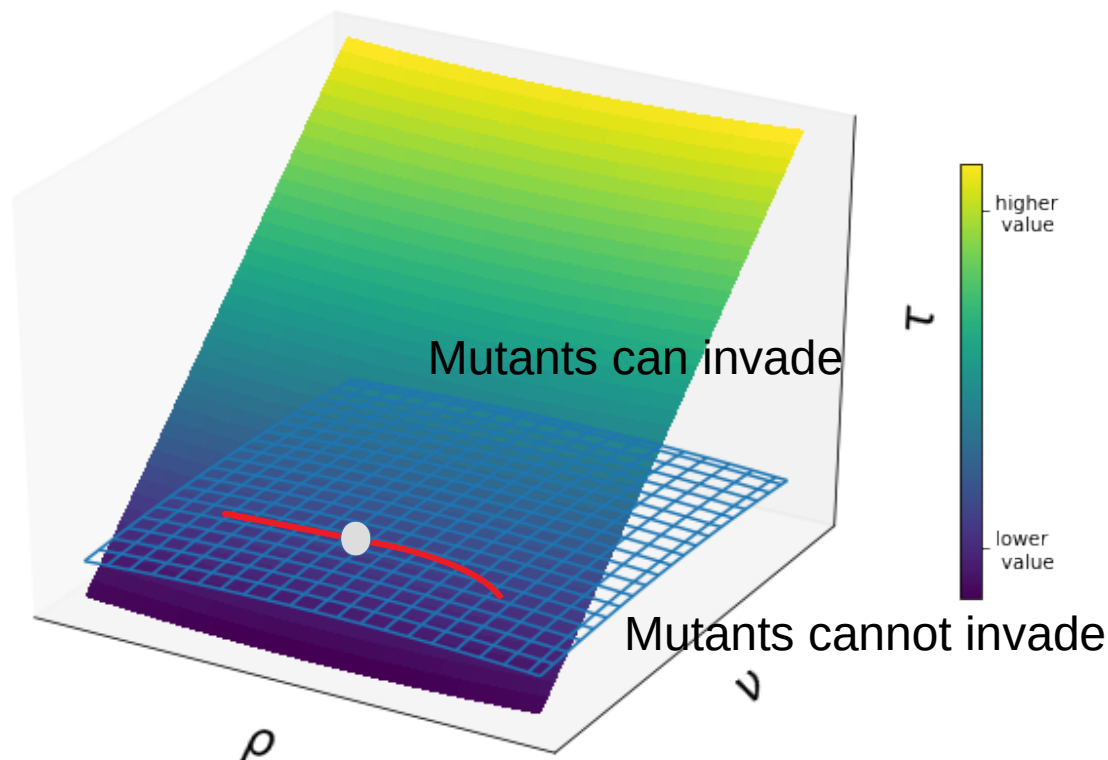


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Invasion boundary



Trade-off and invasion fitness can be represented as manifolds

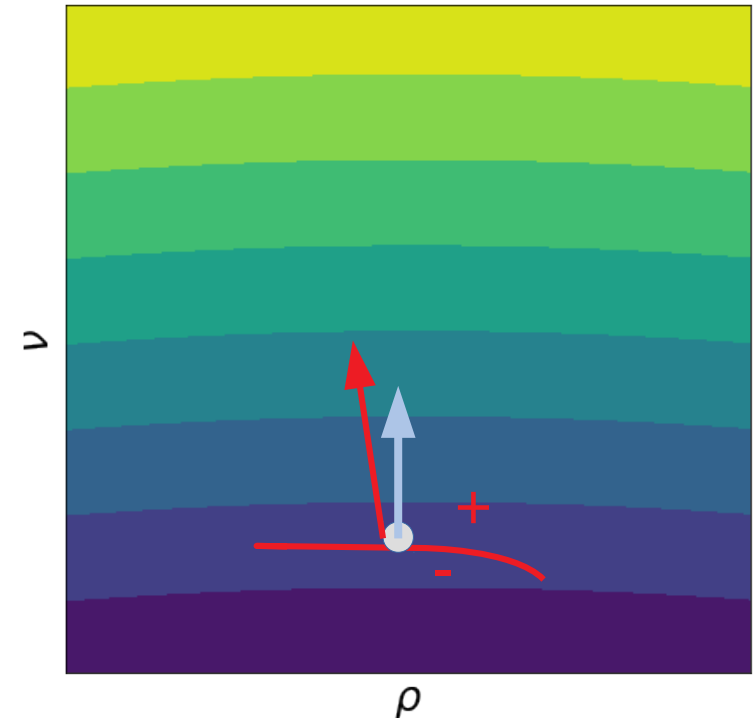
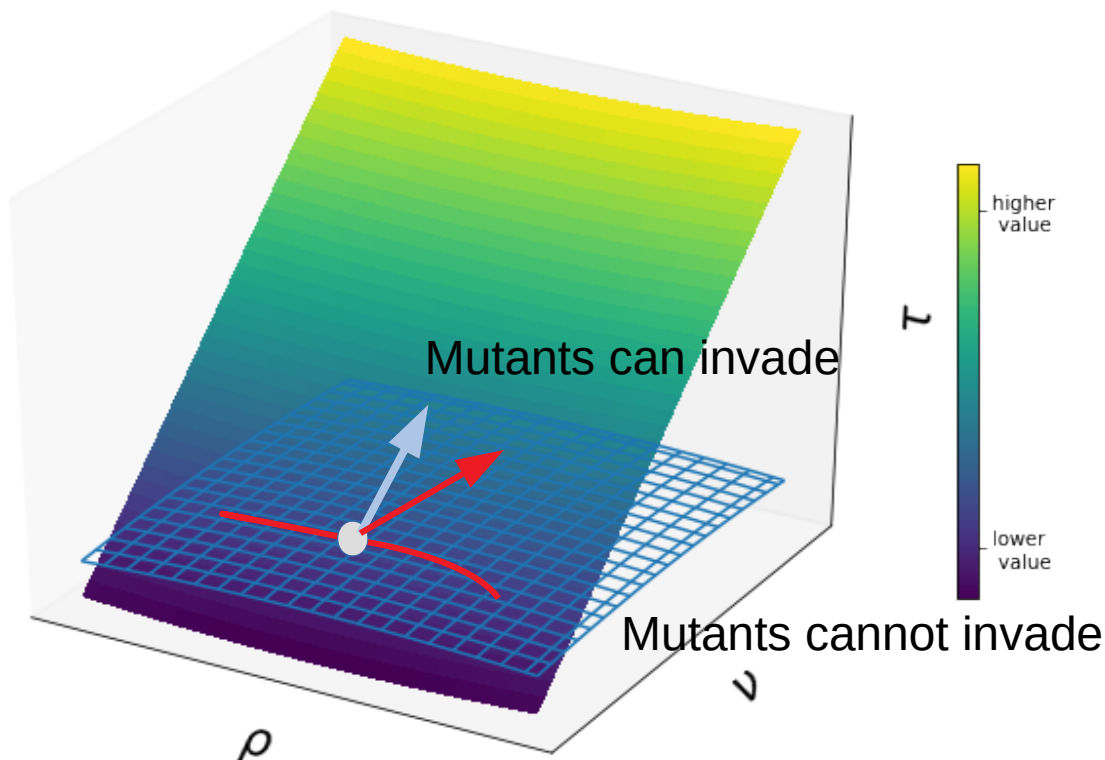
$$\tau = \theta - \rho^h + \eta(\nu - \nu_0)^g$$

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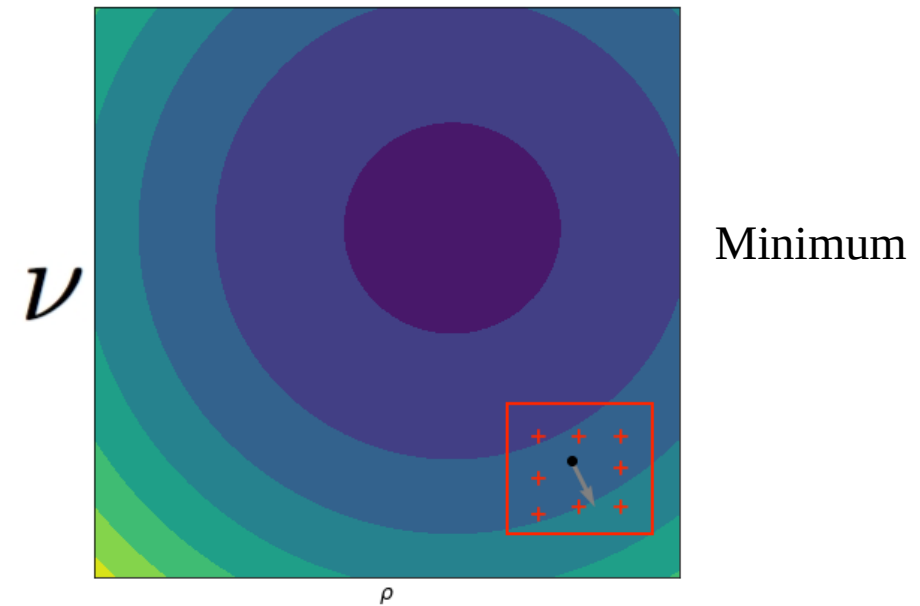
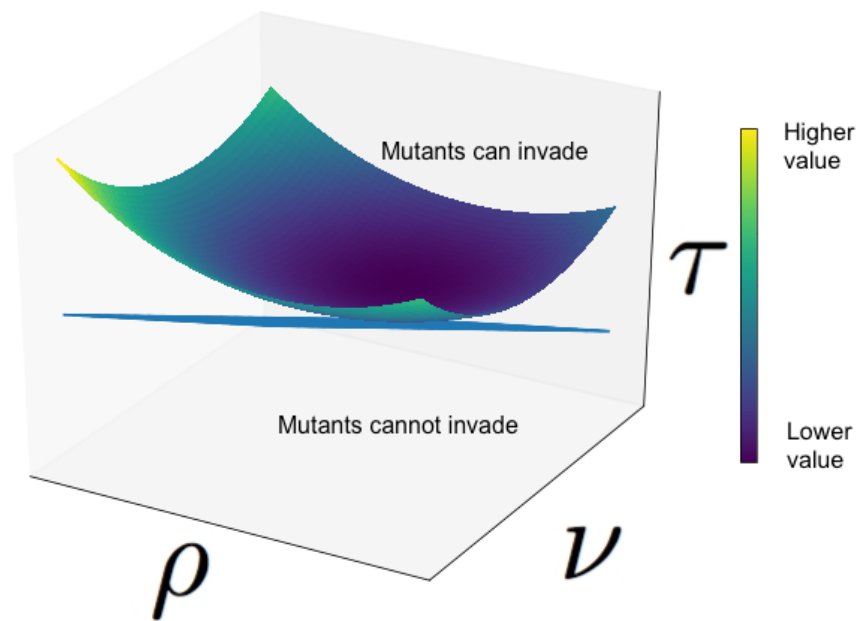
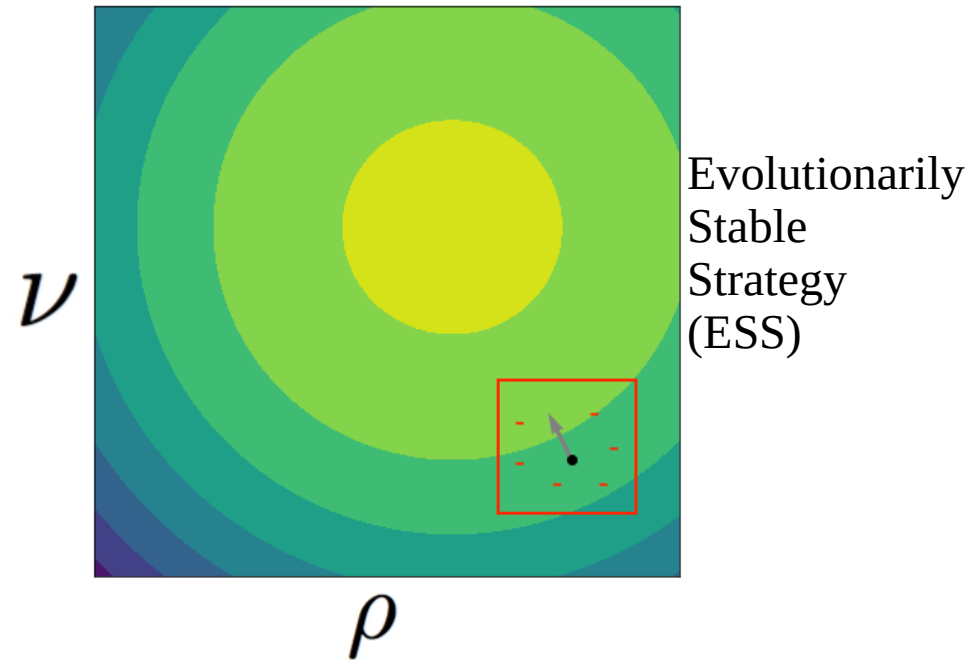
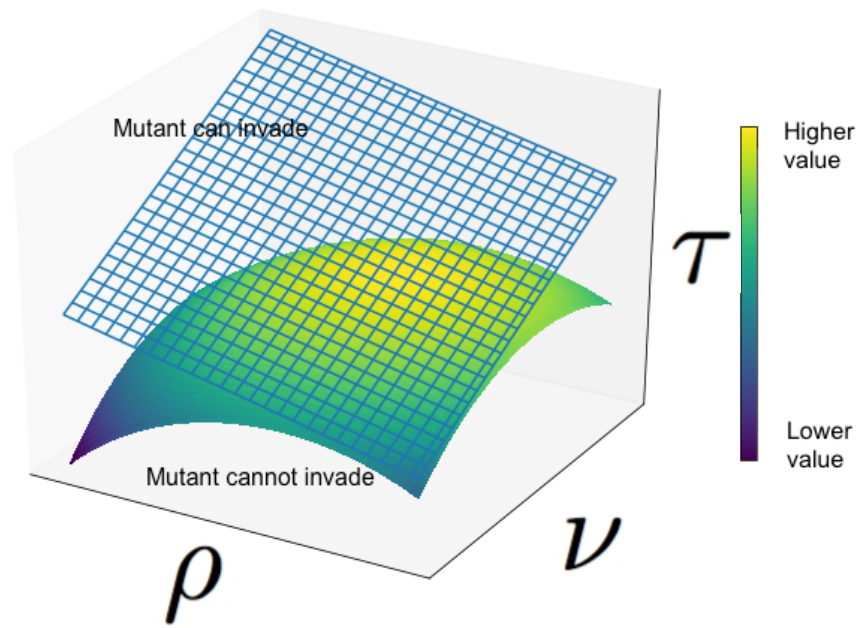
Invasion boundary

Steepest ascent of tradeoff surface

Steepest ascent of invasion surface

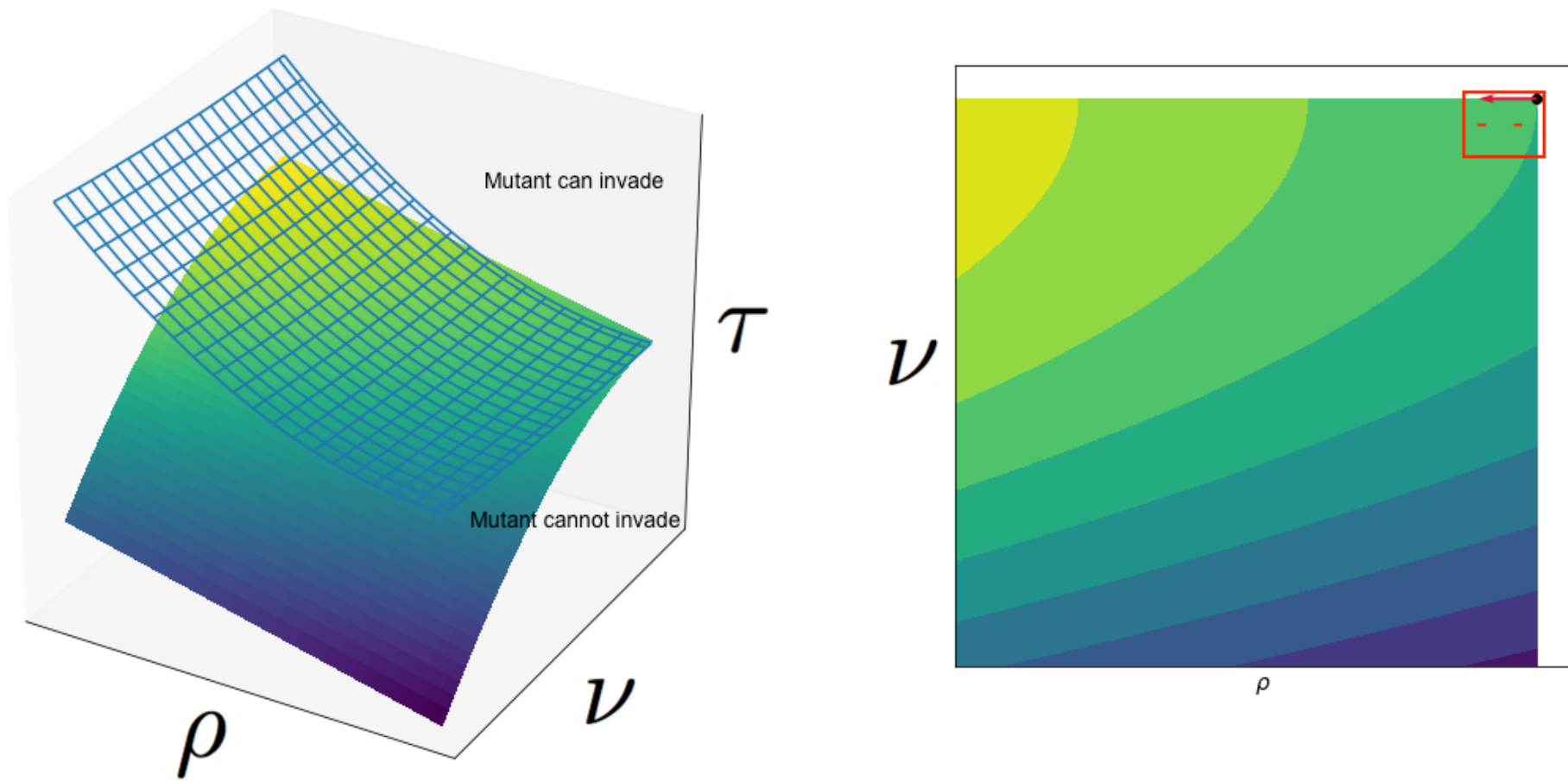


Singular strategy is the tangent point of the two manifolds



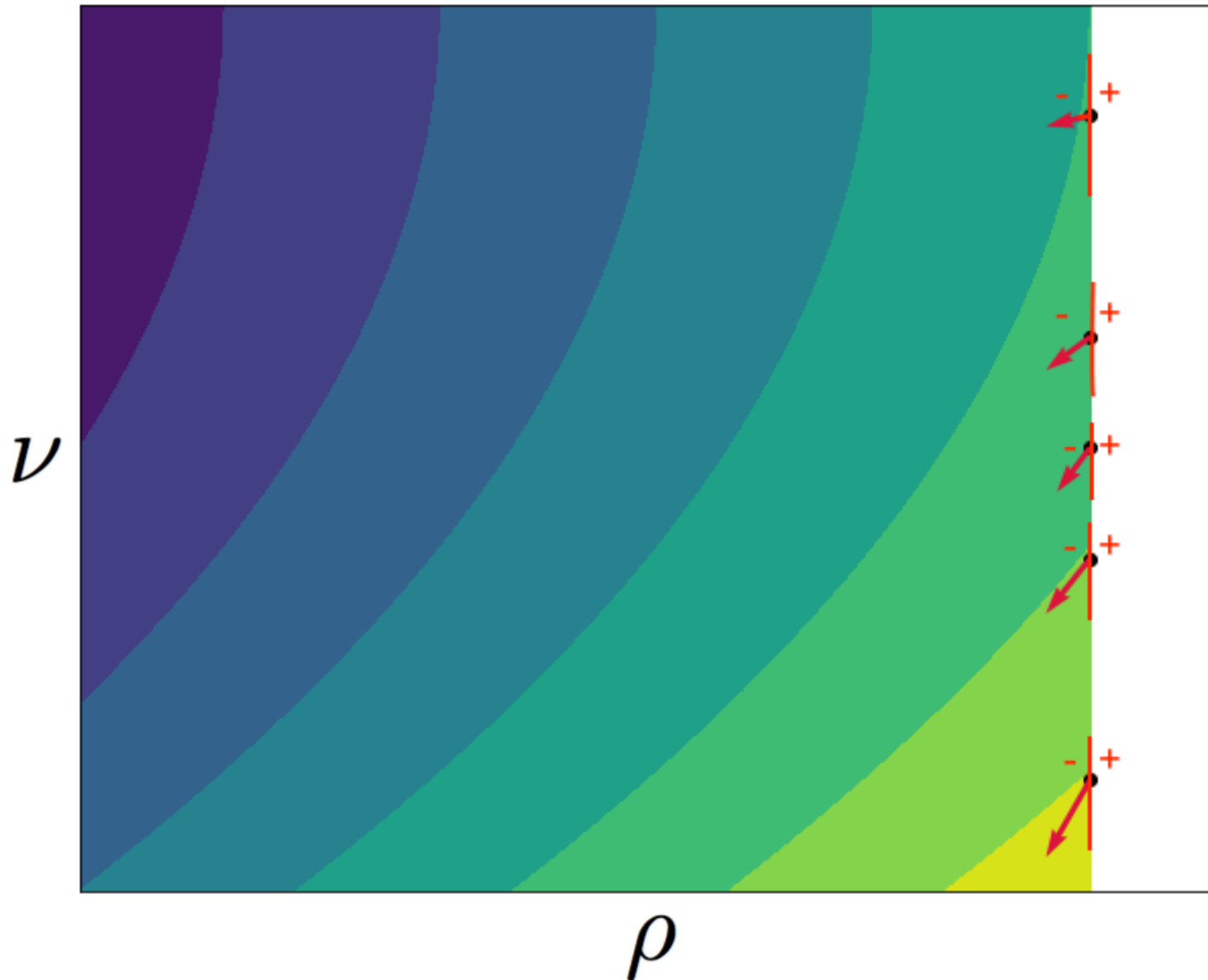
Boundary ESS

The **steepest ascent** of the invasion surface lies on the negative area



Multiple ESSs

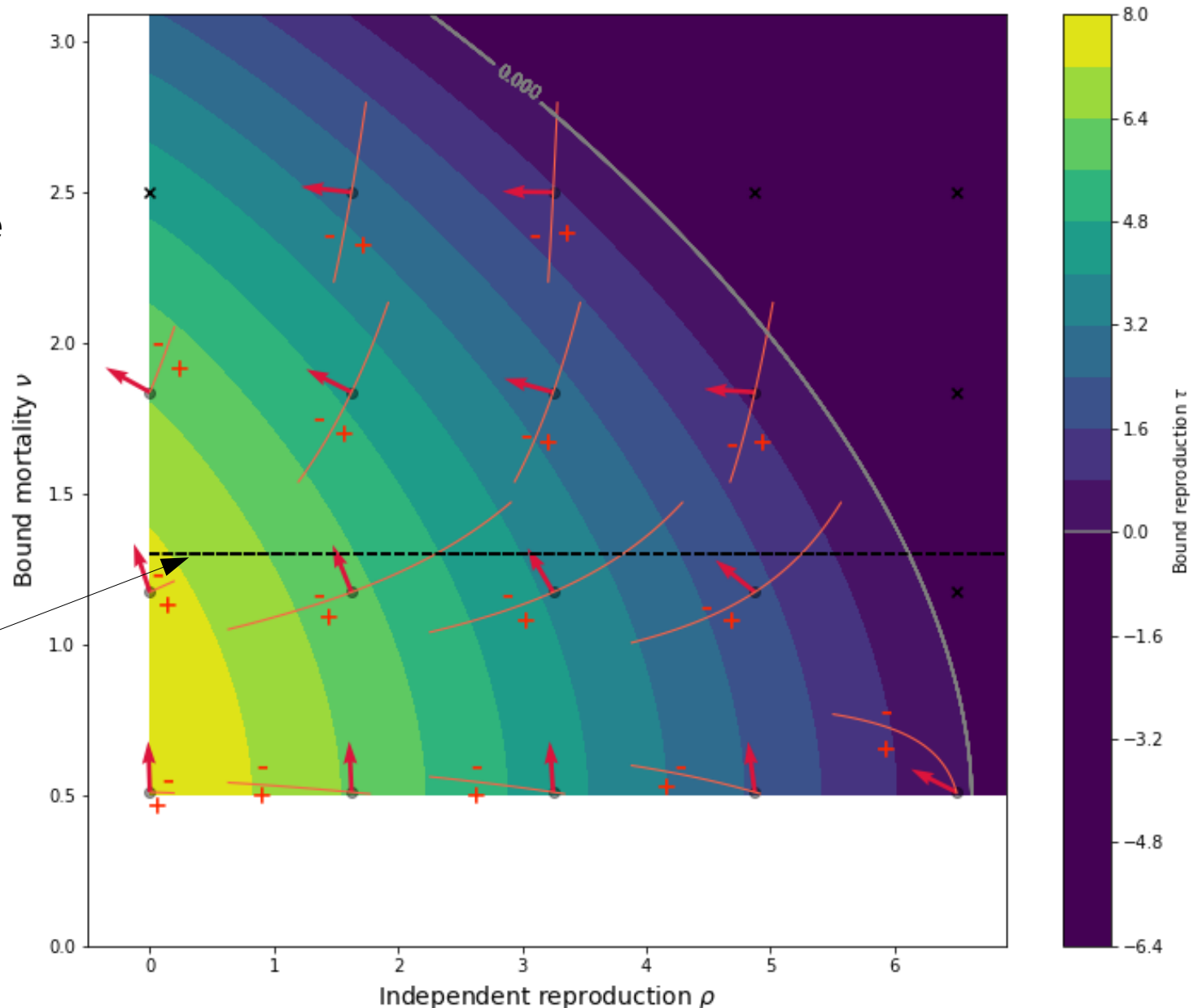
Multiple residents with invasion boundaries parallel to one axis



Benefits from adaptation to symbiosis impose a small cost on independent reproduction

When adapting to the symbiotic lifestyle also provide host protection

Mortality rate of free host

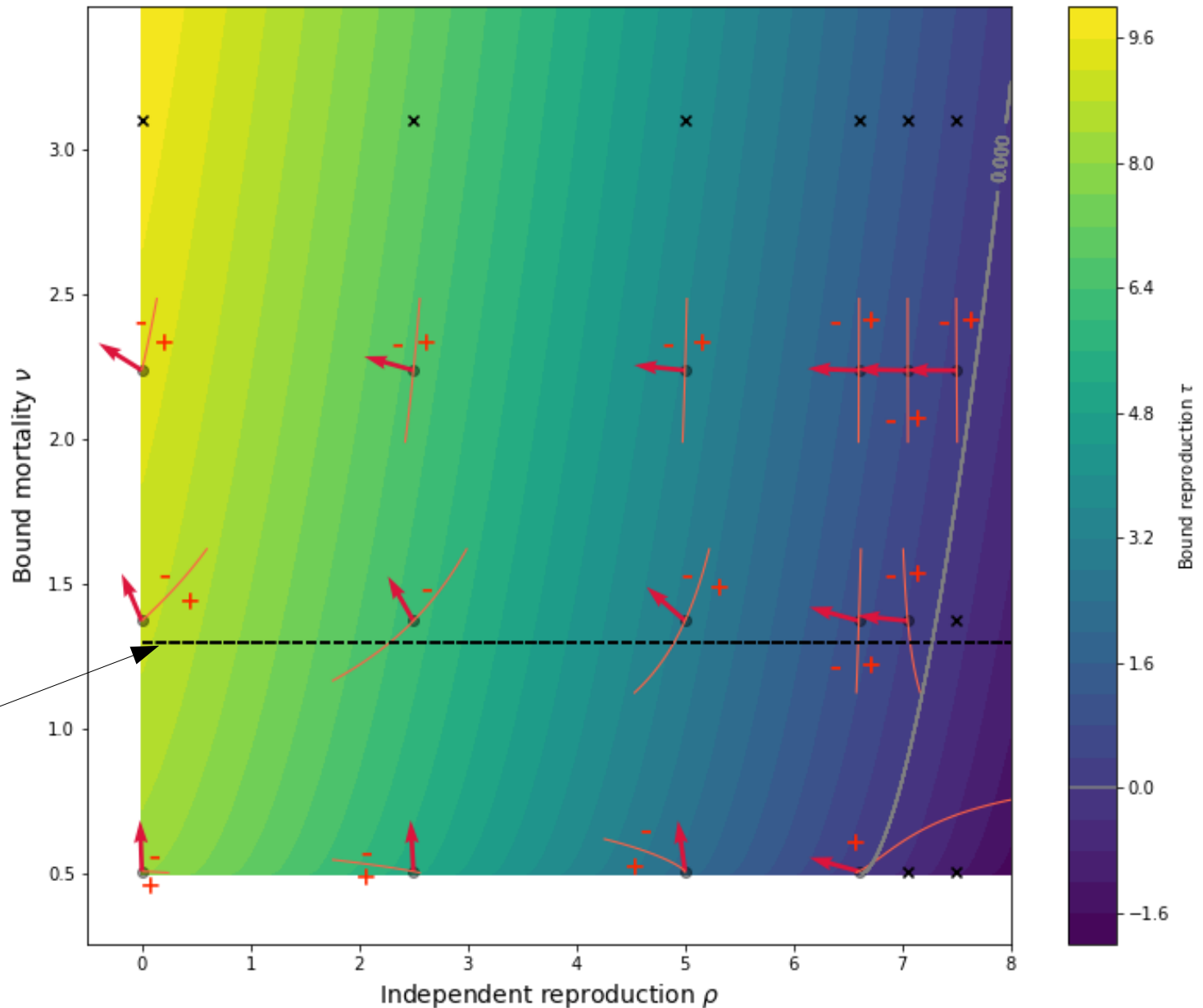


Benefits from adaptation to symbiosis impose a small cost on independent reproduction

When adapting to the symbiotic lifestyle is virulent

Parasites are incapable of inducing high virulence

Mortality rate of free host

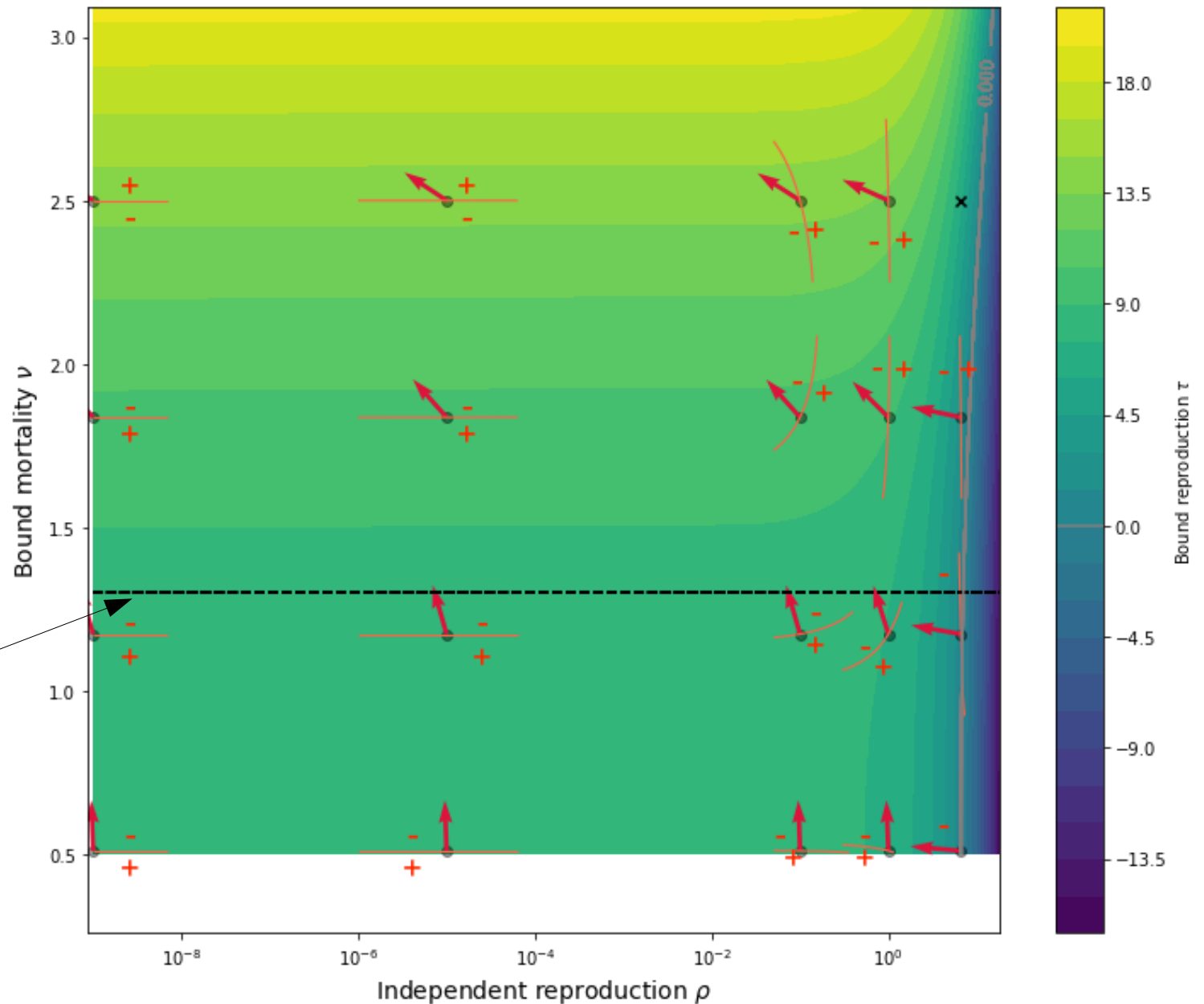


Benefits from adaptation to symbiosis impose a low cost on independent reproduction

When adapting to the symbiotic lifestyle is virulent

Parasites are capable of inducing high virulence

Mortality rate of free host





Conclusions

When benefits from the adaptation to the symbiosis impose a low cost on the independent reproduction:

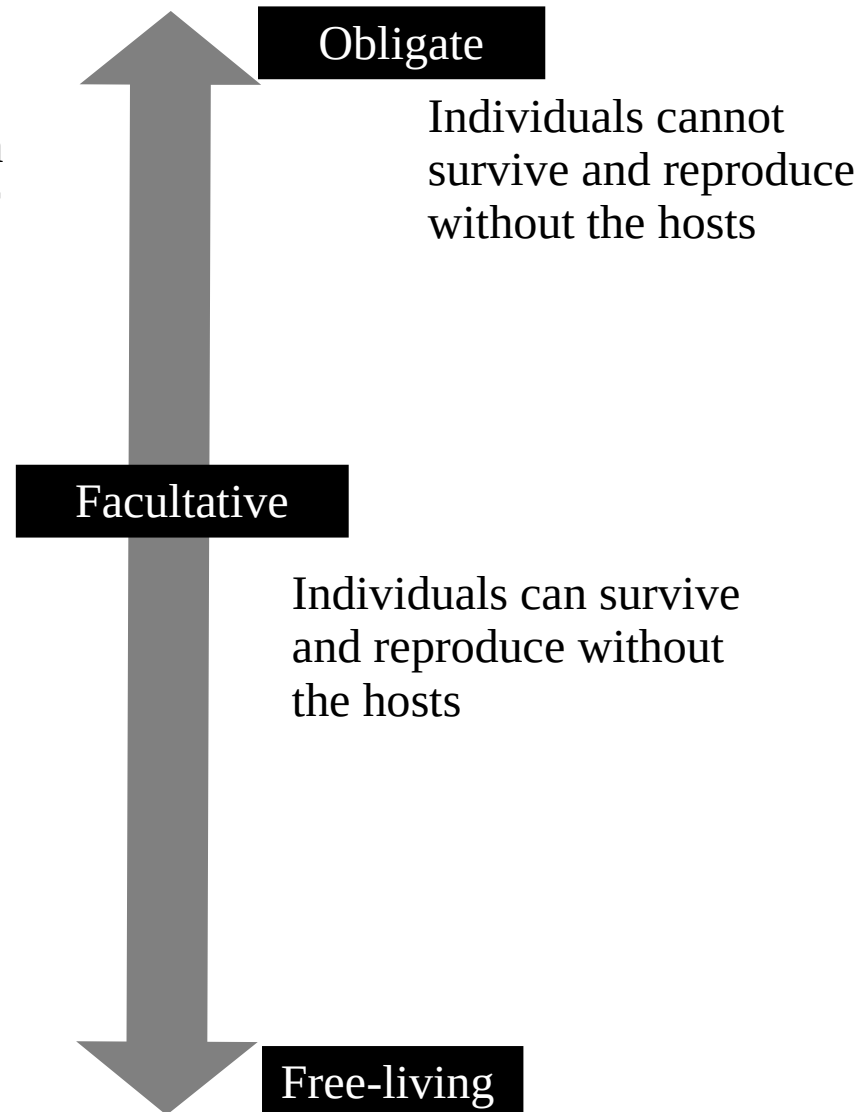
- Obligate mutualism can evolve via small mutations
- Parasitism incapable of inducing high virulence never evolve dependency on the host
- Parasitism capable of inducing high virulence results in various scenarios



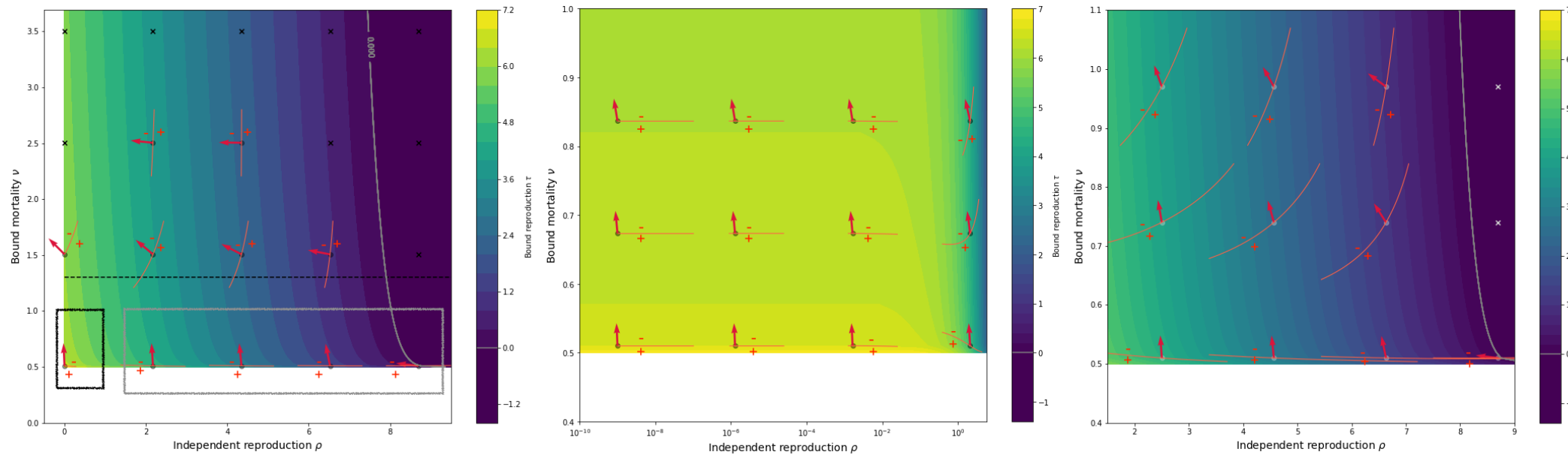
Questions?

Transition from facultative to obligate symbiosis is an evolutionary riddle

- We will focus on the evolution of one partner (the SYMBIONT) given the ecological dynamics of the other partner (the HOST)
- We will use INDEPENDENT REPRODUCTION as indication of partner dependency



Benefits from adaptation imposes a high cost on the independent reproduction



Benefits from adaptation imposes a high cost on the independent reproduction

