

## Observance of Hund's Rules in the Same Setting: Coexistence of Intra-Atomic and Inter-Atomic Exchanges in Cellular Automata

**Rule 1:** Maximization of total spin  $S$   
Reduces Coulomb repulsion  
Weak Ferromagnetic coupling  
Long-range dipolar interactions

**Rule 2:** Maximization of total orbital  
angular momentum  $L$   
Reduces Coulomb repulsion

**Rule 3:** Minimization of spin-orbit energy  
Save kinetic energy  
Antiferromagnetic coupling<sup>1</sup>

**Goktug Islamoglu**

Independent Researcher, M.Sc

[goktu.github.io/ADama/](https://goktu.github.io/ADama/)

1. Paolasini, Luigi. Lectures on Magnetism, Lecture 4 «Magnetic Interactions». ESRF

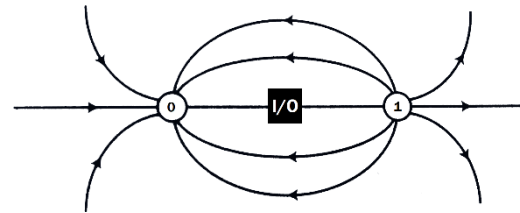
## Significance of Hund's Rule Determination of the ground states

**Aim:** To bridge between ferromagnetism and antiferromagnetism, through paramagnetic and ferrimagnetic spin magnetic moments

Antiferromagnetic materials is one of the most popular areas of memory research.

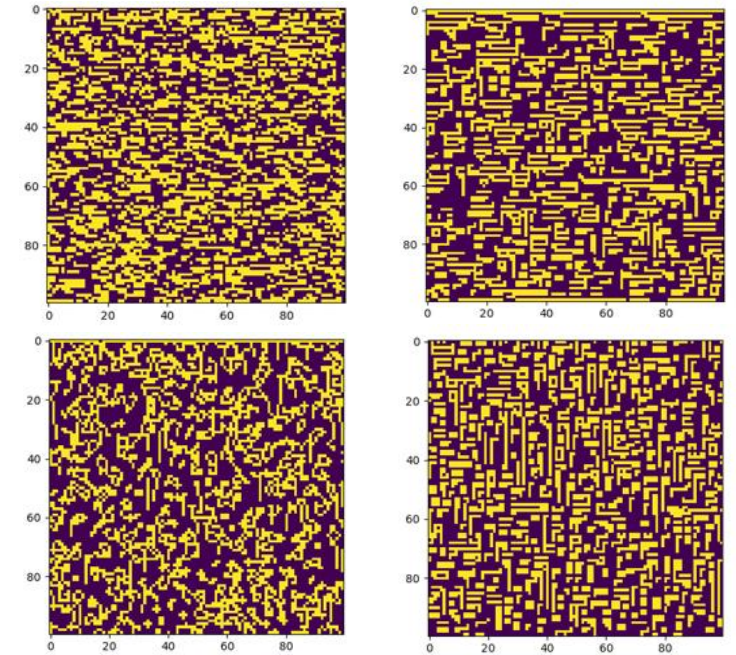
Finding materials generating a 0/1 switch is the current challenge for antiferromagnets.

In this research, the author proposes a framework by a cellular automaton model. A switch between **strained ferromagnetic** state and **antiferromagnetic ground state** is hypothesized as **ferrimagnetic polarization**.

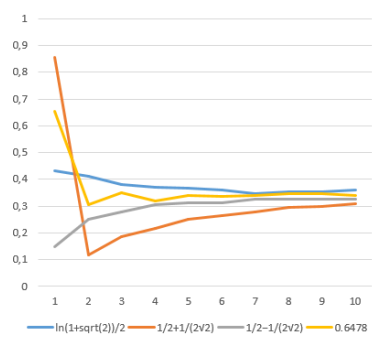


**Fig. 1** Strained Model

Top Right, Clockwise  
**a.** Ferromagnet  
**b.** Ferrimagnet  
**c.** Antiferromagnet  
**d.** No drive, coupling  
**e.** No coupling, drive



**4-4 NEIGHBOR TUNING RESPONSE**



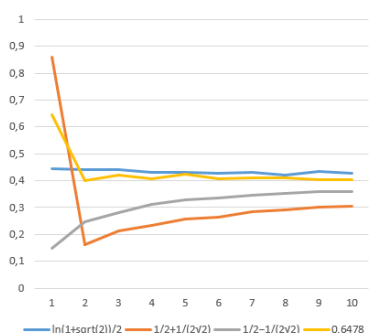
**Fig. 2** Neighbor Tuning

**Top-Middle Left:** State 1 cell counts of 4/9 or 5/9, inverse Ising critical temp. local max, paramagnetic

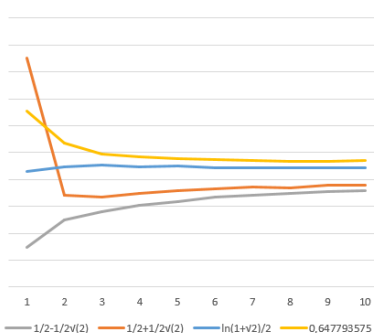
**Middle Right:** Count 6/9, global max, spontaneous ferromagnetic transition.

**Bottom:** Transition model

**5-5 NEIGHBOR TUNING RESPONSE**



**6-6 NEIGHBOR TUNING RESPONSE**

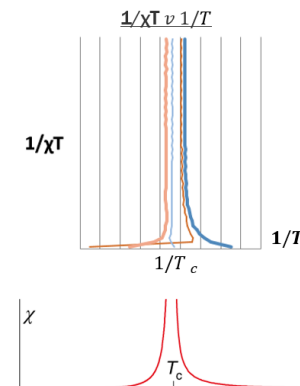
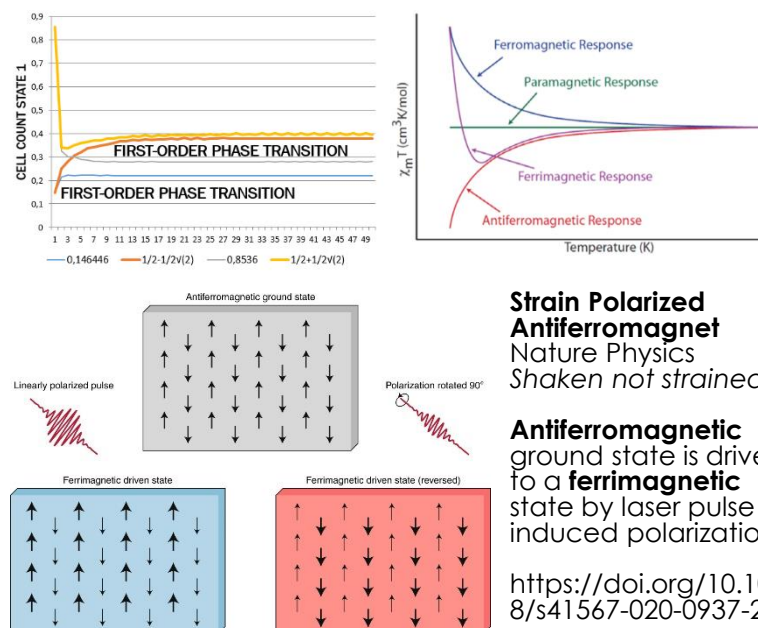


**Fig. 3** Types of Transitions

**Top:** Second-order phase transition at Ising critical temp. is ferromagnetic.

**Middle:** First-order phase transition at the reversed ferrimagnetic polarization to the AFM ground state.

**Bottom:** Commentary



**Strain Polarized Antiferromagnet**  
Nature Physics  
Shaken not strained

**Antiferromagnetic** ground state is driven to a **ferrimagnetic** state by laser pulse induced polarization.

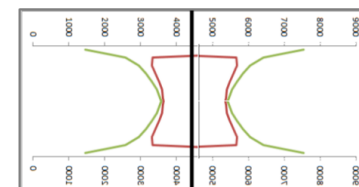
<https://doi.org/10.1038/s41567-020-0937-2>

## Results

Exact analytical solutions of transition geometries: First-order (Hund's Rule 3) & second-order (H's R 1)

**Presented:**  
NECSI ICCS 2020  
NERCCS 2021

**2D Ising model map onto 1D quantum spin chain<sup>1</sup>**



Polarization: Catenoid around  $p = 1/2$

**FIRST-ORDER PHASE TRANSITION**

Step 1

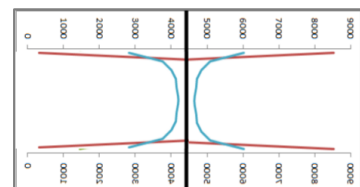
1	1	1
0	1	1
1	1	1

Step 2

1	1	1
0	0	1
1	1	1

Step 3

1	1	1
0	0	0
1	1	1



Ising critically: Pseudosphere around  $p = \ln(1+1/2)/2$

**SECOND-ORDER PHASE TRANSITION**

Underlying evolution function suggests a mode of switching between two types of phase transitions. An I/O (1st rule) that is also a data storage (3rd rule).

This feedback loop is a **dipole state machine**.

1. Wei, BB., Chen, SW., Po, HC. et al. Phase transitions in the complex plane of physical parameters. Sci Rep 4, 5202 (2014). <https://doi.org/10.1038/srep05202>