# BLG 335E Analysis of Algorithms 1 Project 1

<u>Lecturer:</u> Hazım Kemal Ekenel

> Student: Göktürk GÖK 150110029

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### A. Asymptotic Upper Bound

There are 3 main situation as worst-case, average-case and best case of algorithms. And each of them is described as <a href="big O">big O</a> notation which specify the upper bound for the worst-case, <a href="big D">big Theta Notation</a> which is located between upper and lower bound for the average-case and <a href="big O">big Omega Notation</a> that specify the lower bound for the best-case.

#### 1. Linear Search

my implementation: Normally there would be a key then you can search the list item by item until the key matches the element of an array. But in our project there is a temporary array( temp) which keeps K-closest warehouses instead of just a key. My implementation includes two nested loops which the inner loop is K times and outer loop is N-K times. So N\*K is the upper bound of linear search in this project instead of finding a key in an array has just N.

**best case:** 1 (big omega notation) **worst case:** n (big O notation)

#### 2. Insertion Sort

 $\label{eq:my-implementation:} \begin{tabular}{ll} my implementation: There are two nested loops which both are run N (range) times. So <math display="block"> \hline upper-bound\ of\ my\ insertion\_sorter\ is\ N^2\ . \\ \begin{tabular}{ll} Here\ N\ is\ the\ number\ of\ warehouses\ which\ is\ taken\ as\ an\ argument\ from\ terminal. \end{tabular}$ 

**best case:** n (big omega notation) **average case:** n<sup>2</sup> (big theta notation) **worst case:** n<sup>2</sup> (big O notation)

#### 3. Merge Sort

my implementation: There is a <u>divide and conquer algorithm</u> here using merge sort algorithm. Asymptotic <u>upper bound of Merge Sort</u> Algorithm is **O(n\*log(n))**. So when the number of warehouses is taken as N, execution time will be multiplied by **N\*(log(N))**.

best case: nlogn (big omega notation) average case: nlogn (big theta notation)

worst case: nlogn (big O notation)

## **B.** Execution Time (sec)

#### 1. Linear Search

	K = 1	K = 2	K = 10	K = N/2
N = 10	0	0	0	0
N = 100	0	0	0	0
N = 1000	0	0	0.0001	0.004
N = 1 000 000	0.001	0.03	0.13	3294

#### 2. Insertion Sort

	K = 1	K = 2	K = 10	K = N/2
N = 10	0	0	0	0
N = 100	0	0	0	0
N = 1000	0.003	0.003	0.0029	0.0029
N = 1 000 000	3304	3387	3467	3412

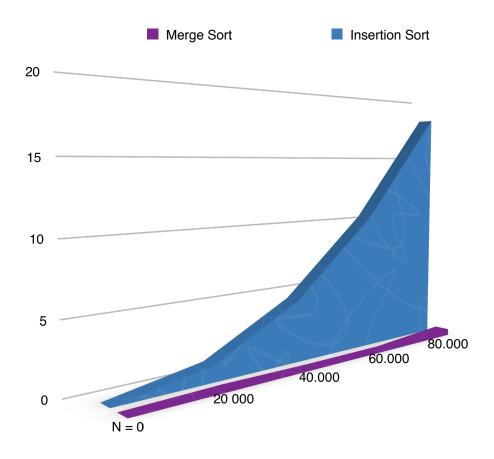
### 3. Merge Sort

	K = 1	K = 2	K = 10	K = N/2
N = 10	0	0	0	0
N = 100	0	0	0	0
N = 1000	0.0004	0.0005	0.0004	0.0004
N = 1 000 000	0.7132	0.7013	0.6926	0.6883

## 4. Average Times of Execution Time of Algorithms

	Linear Search	Insertion Sort	Merge Sort
N = 10	0	0	0
N = 100	0	0	0
N = 1000	0.002	0.00295	0.00042
N = 1 000 000	823.54	3392.5	0.526

### C. 2-Line Plotting of Running Time Complexity



N (Number of data)

As it is shown above that if there is a sorting around small amount of data(ex: 500), there are not so big differences between insertion sort and merge sort

But Merge sort is more effective than insertion sort when sorting big amount of data (ex;more than 1000) because it has much more less complexity than insertion sort (**logn < n after specific point**).