

Machine Design

Machine & Machine Element

Machine - perform useful work when some form of energy is applied

Machine element - Smallest component of machine

Machine Design

Combination of scientific principle
technical information
imagination

↓ to perform

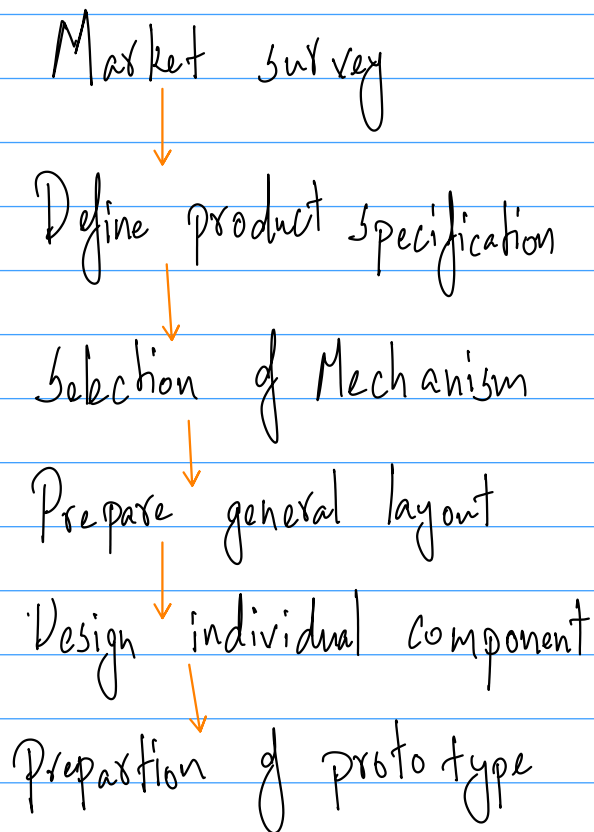
maximum economy and efficiency

Need for Design

→ safe, more efficient & comfortable
↓
safe design

→ friction b/w people & product
↓
design fail
↓
need for design arises

Basic Procedure of Machine Design



Machine Elements

→ Elementary Component of machine

(gears, shaft, clutch)

↳ General purpose machine element
↳ Special " " "

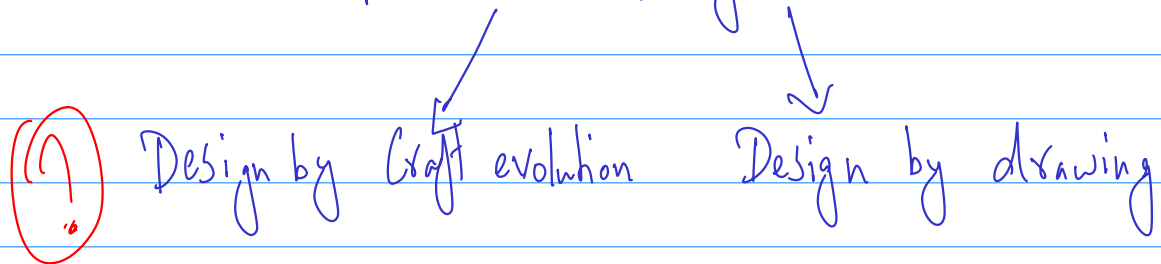
BASIC REQUIREMENTS OF MACHINE ELEMENTS



Design of machine elements

- specification of function
- Determination of force
- selection of material
- Failure Criterion
- Determination of Dimensions
- Design Modification
- Working Drawing

Traditional Design Methods



Design Synthesis

Process of selecting

- Configuration
- materials
- shapes
- dimension of product

Main objective is optimization

Ergonomics

→ relation ship between man, & machine

work natural laws

→ to solve problems b/w man & machine wing
→ anatomical
→ physiological
→ psychological principles

Aesthetic Consideration

→ customer attracted towards appealing product

→ external appearance dominates sale in market

Hooke's Law, elastic & plastic behaviour

elastic behaviour - material return back to its original size after removal of force

Plastic behaviour - deformation remains after removal force

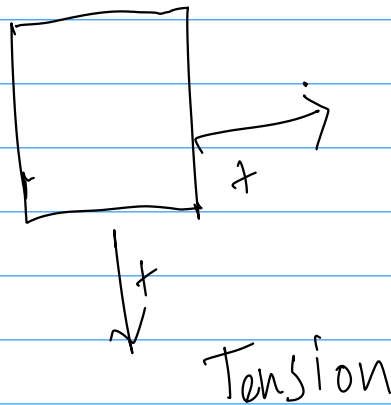
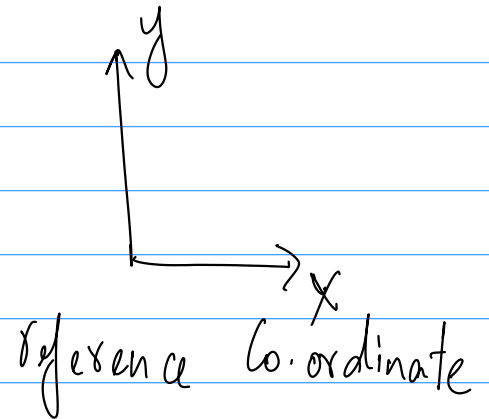
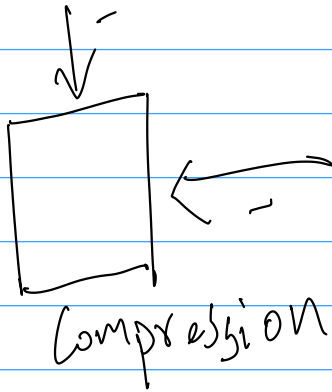
Hooke's Law

$$F = k \Delta x$$

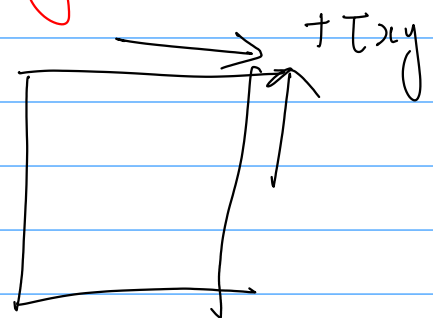
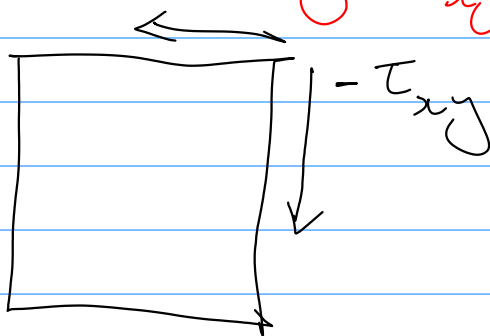
Force Spring Constant Stretched length - original length

$\sigma_x \sigma_y \rightarrow$ Normal stress

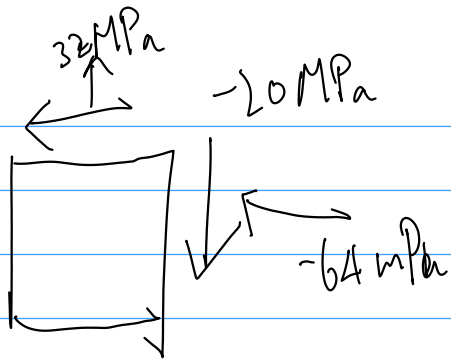
$\tau_{xy} \rightarrow$ Shear stress



Determining τ_{xy} & its sign



Shear force



Three different methods

- Mohr's Circle
- Matrix & Determinants
- Formulae

Mohr's Circle

→ Give graphical solution

1) Determine the principal stress σ_1 & σ_2

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + (\tau_{xy})^2}$$

2) Determine the max shear stress τ_{max1} & τ_{max2}

$$\tau_{max1,2} = \pm \frac{(\sigma_1 - \sigma_2)}{2}$$

3) Determine Principal direction ϕ_1 & ϕ_2

$$\tan(2\phi_1) = \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$$

$$\phi_2 = \phi + 90^\circ$$

Failure of Ductile & brittle materials

Failure of ductile material \rightarrow initiation of yielding

Failure of brittle material \rightarrow fracture

Theories of failure for ductile material

\rightarrow Maximum shear stress theory (Tresca Yield criterion)

Most cause of yielding \rightarrow slipping

\downarrow
occurs along the contact
planes of randomly ordered crystal

Slipping is due to shear stress $\tau_{\max}^{\text{abs}} = \frac{\sigma_{\max} - \sigma_{\min}}{2}$

Maximum Distortion Energy theory (Von Mises Yield criterion)

For 3-d $\Rightarrow \sigma_0 = \sqrt{(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2}$

For 2-d $\Rightarrow \sigma_0 = \sqrt{\sigma_1^2 - \sigma_1 \sigma_2 + \sigma_2^2}$

$\left. \begin{array}{l} |\sigma_1| = \sigma_y \\ |\sigma_2| = \sigma_y \end{array} \right\} \sigma_1 \text{ \& \& } \sigma_2 \text{ have same sign}$ $\left. \begin{array}{l} |\sigma_1 - \sigma_2| = \sigma_y \\ \downarrow \\ \text{for opposite sign} \end{array} \right\}$

\Rightarrow Yield stress occurs when $\sigma_o = \sigma_y$

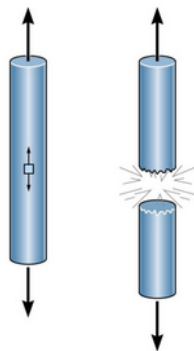
Allowable stress, σ_{allow} by safety factor, SF

While designing

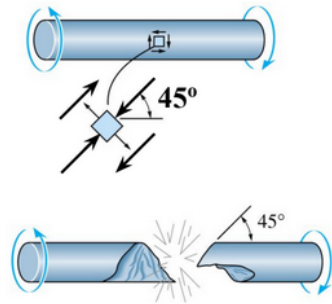
$$\sigma_{allow} \leq \sigma_o$$

$$\text{Where } \sigma_o \leq \frac{\sigma_y}{SF}$$

Theory of failure for brittle materials



Failure of a brittle material
in tension



Failure of a brittle material
in torsion

For plane stress

$$|\sigma_1| = \sigma_{ultimate}$$

$$|\sigma_2| = \sigma_{ultimate}$$

$$\text{stress due to axial load} = \frac{F}{A}$$

$$\text{torsional load} = \frac{Tc}{J}$$

Polar moment of inertia

Design Against fluctuating loads

fluctuating loads:

→ forces which are not static & vary with time

→ 80% of Component fail due to this

Three popular Criteria

→ Gerber line

→ Soderberg line

→ Goodman line

Stress concentration

→ localisation of high stress due to irregularities ^{accumulation}

→ to find stress concentration, stress concentration factor is used

$$K_t = \sigma_{\max} / \sigma_0$$

Causes of stress concentration

- Variation in property of material
- load application
- Abrupt change in section
- Discontinuities
- Machining scratches

Stress Concentration factors

- Ductile material under static load
- Ductile material under fluctuating load
- Brittle material

→ To reduce stress concentration

→ avoid abrupt change in stress flow line

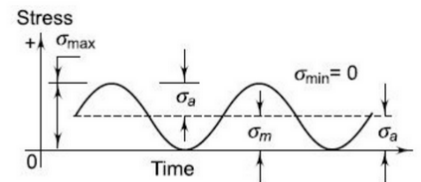
→ smoother change gives lower stress concentration

Variable stress → magnitude / direction / both changing

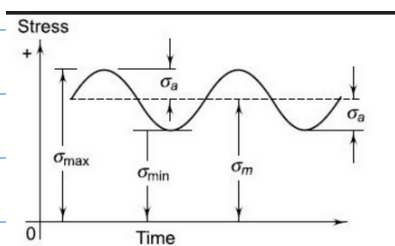
→ Fluctuating stress

→ Repeated stress

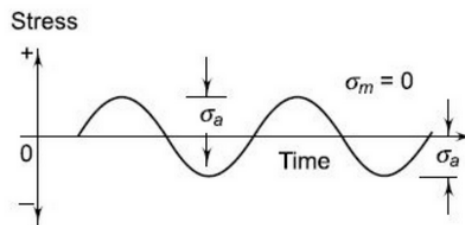
→ Reversed stress



(b) Repeated stresses



(a) Fluctuating stresses



(c) Reversed stresses

$$\sigma_{\text{mean}} = \frac{\sigma_{\text{max}} + \sigma_{\text{min}}}{2}$$

$$\sigma_{\text{alternating}} = \frac{\sigma_{\text{max}} - \sigma_{\text{min}}}{2}$$

Endurance limit

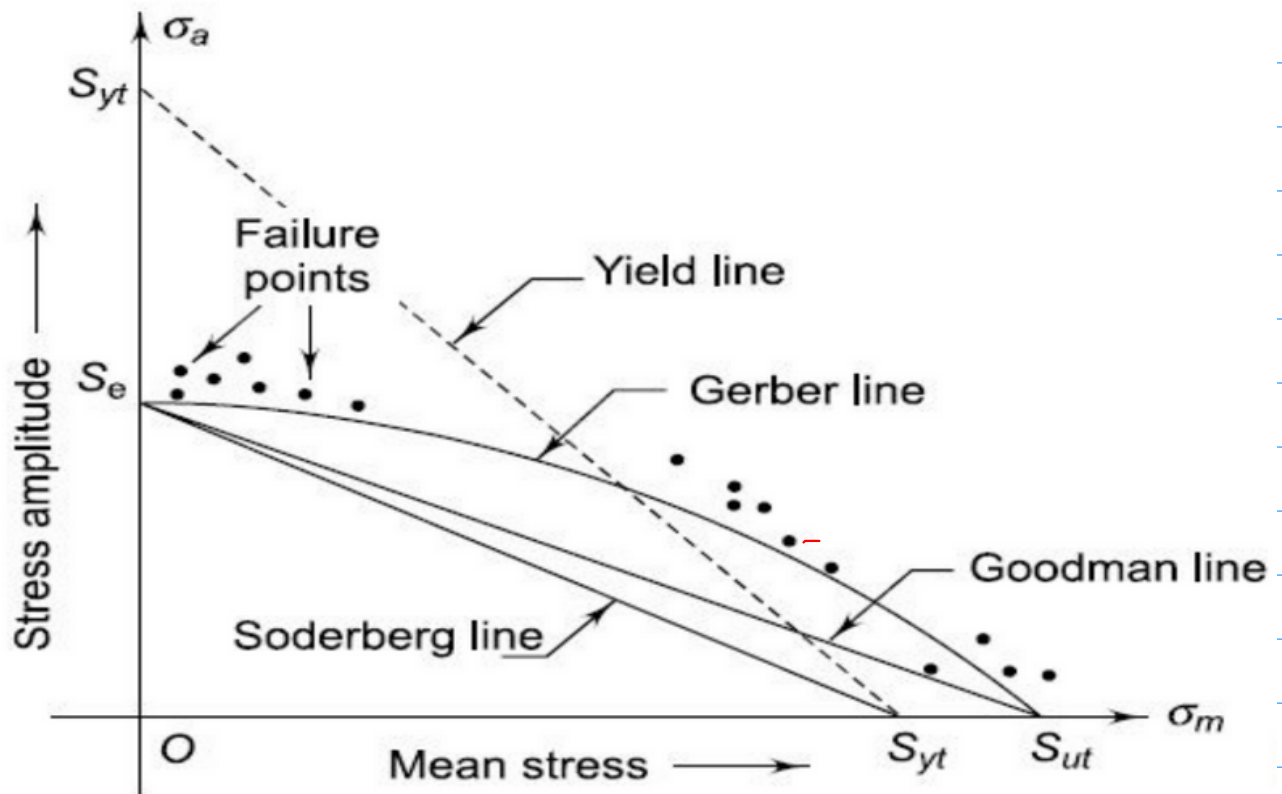
→ maximum amplitude of frequency a specimen can stand for ∞ cycles

→ In general $\infty \approx 10^6$ times

Notch sensitivity

→ Sensitivity of material developing notch during fluctuating load

Soderberg and Goodman Equation



Pf - 2

Spring - elastic body - function \rightarrow distort on load
 \rightarrow recover on removal

Applications

to absorb shock and vibration Car spring
to apply force in brakes Clutch
storage of potential energy watches & toys

Types of springs



Helical springs



Conical & Volute spring

Torsion spring



Laminate / leaf springs

Disc or bellville springs

Special purpose springs

Helical springs

- \rightarrow Wired coils in form of helix
- \rightarrow Cross section may be circular, square or rectangular

Closed & open coil helical springs

Closely Coiled \rightarrow wires are so close to each other
 \rightarrow Subjected to torsion (twisting force)
 \rightarrow major force - shear stress due to twisting

Open Coil

- \rightarrow gap between two adjacent turns
- \rightarrow application is limited

Advantages

- \rightarrow Easy to manufacture
- \rightarrow Available in wide range
- \rightarrow reliable
- \rightarrow Constant spring rate
- \rightarrow performance can be predicted

Conical & Volute Spring

- \rightarrow application where varying spring rate
spring rate \uparrow with load \uparrow
- \rightarrow Constant pitch & angle
- \Rightarrow decreasing coil \rightarrow \uparrow in spring rate
- reduces \rightarrow vibration problem with varying mass
- \rightarrow Shear stress due to twisting

Torsion Springs

→ helical or spiral type

helical → load winds up spring

spiral → used where load tends to increase

Major force Tensile & Compressive

Disc Springs

→ consists of number of conical discs around central tube

→ used when high spring rate is required

Special Purpose Springs

→ liquid springs, rubber springs, ring springs

Materials for helical spring

Properties → high fatigue strength
→ high ductility

Services

Severe service - rapid loads

Average intermittent operation

light service - static load, infrequently varied