# Phil 120, Finals

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 $\mathbf{Q}\mathbf{1}$ 

p	q	r	$(\neg p$	$\wedge$	$(q \vee$	$\neg r))$	$\leftrightarrow$	$(\neg q$	$\rightarrow p)$
F	_	_	_	_	_	Τ	_	<del>-</del>	_
$\mathbf{F}$						F			
F	_	_	_	_	_	Τ	_	_	${ m T}$
F	_	_	_	_	_	F	_	_	${ m T}$
_	_	_	_	_	_	Τ	_	_	${ m T}$
T	F	Τ	F	F	F	F	F	Τ	${ m T}$
T	Τ	F	F	F	T	Τ	T	F	${ m T}$
T	Τ	Τ	F	F	$\mathbf{T}$	F	T	F	${ m T}$

so, the formula is not a) a logical validity, b) is contingent, c) is not a falsehood.

### $\mathbf{Q2}$

**a**)

let a be alfred, k be kurt, Lx if x proves a lemma, Tx if x proves a theorem, Px if x writes a paper.

$$(Tk \lor Lk) \to Pa$$

b)

let a be alfred, b be albert, Cx if x is cooking, Rx if it is raining where x is, Sx if x is shopping.

$$\neg Sa \wedge (\neg Rb \rightarrow Cb)$$

**c**)

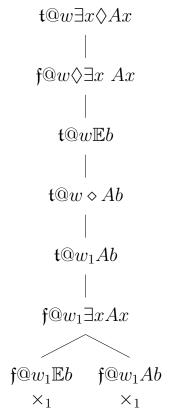
let s be snow, let t be 2 + 2, f be 5, u be tuesday, Wx if x is white, Tx if today's weekday is x.

$$Ws \to (t = f \lor \neg Tu)$$

d)

let a be alfred, k be kurt, Hx if x is on a hike, Cxy if x is chatting with y.  $Ha \to \neg Cka$ 

### $\mathbf{Q3}$



since all branches closed with rule 1, the statement holds in CL, k3, LP, and fde.

## $\mathbf{Q4}$

suppose there are 2 worlds in the universe, w1 and w2 such that C is true in w1, but false in w2.

since  $\neg\Box C \iff \diamond \neg C$  (proof is trivial from tableaux),  $\Box \neg\Box C \iff \Box \diamond \neg C$ . Then since  $\neg C$  is satisfied in at least world,  $\diamond \neg C$  holds in every worlds, which means  $\Box \diamond \neg$  holds too. However,  $\neg C$  does not hold in every world, so  $\Box \neg C$  is false, and so this is a counter example for the implication statement( $\rightarrow$ ).

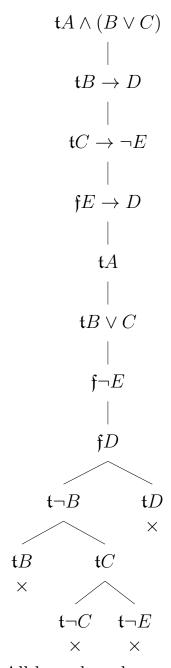
### $\mathbf{Q5}$

**a**)

Suppose  $A \subseteq B$ , then for any  $(a_1, a_2, ... a_i) \in \mathcal{P}(A), a_1, a_2 ... a_i \in A \subseteq B$ , then  $a_1, a_2 ... a_i \in B \implies (a_1, a_2 ... a_i) \in \mathcal{P}(B)$  by definition of powerset, and so a) holds.

b)

 $|C \times C \times C| = |C|^3 = 27,25 < 27 < 30$ , so yes, the statement holds.



All branches closes, the consequence relation holds in TV.

### $\mathbf{Q7}$

**a**)

let Cx if x is car, Sx if x is small, Fx if x is fast.  $\exists x (Cx \land Sx \land Fx)$ 

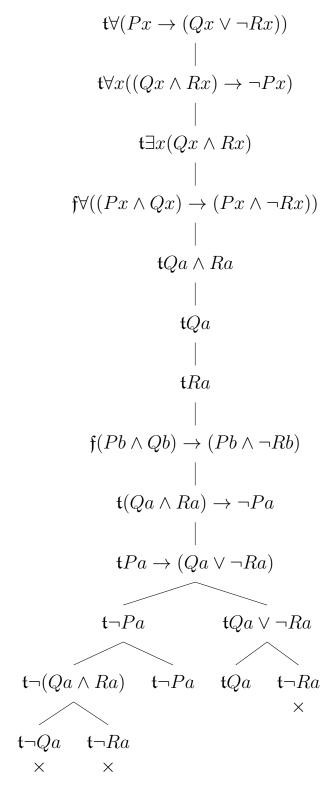
b)

let  $\mathbb{N}, \mathbb{R} - \mathbb{Q}, \mathbb{R}$  be the set of natural, irrational, and real numbers. let  $x \in A$  be the preicate that x is in the set A. x < y if x is less than y.

$$\forall n \in \mathbb{N}(((2n+1) \in \mathbb{R} - \mathbb{Q}) \lor (\exists x \ (x \in \mathbb{R} \land (2n+1) < x)))$$

**c**)

let Sx if x is student, Bx if x is bike, Oxy if x owns y, Rxy if x rides y daily.  $\forall x(Sx \to (\exists y(By \land Oxy) \to Rxy))$ 



looks like i choses the wrong variable names, but i dont have time to redo this question. most likely the first 2 'forall' statements should take the same variable name as the name chosen for the conclusion.

#### $\mathbf{Q}9$

let D = 
$$\{01, 02\}$$
, E =  $\{01\}$ ,  $\delta(a) = o1$ ,  $\delta(b) = o2$   
+(F) =  $\{01\}$ , -(F) =  $\{02\}$ , +(G) =  $\{01, 02\}$ , -(G) =  $\emptyset$ .

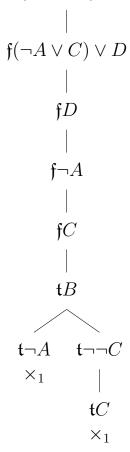
So, for all x, x = a since x can only be assigned o1, which denotes a. Fa is true so  $Favee \neg Gb$  is true,  $\forall x(Fx \rightarrow Gx)$  holds since x can only be o1, and o1 is in the extension set of both F and G. however the conclusion is false since on existing object to be assigned to y satisfy both  $\neg Fy$  and  $\neg Gy$ 

Q10

p	q	$(\neg p)$	$\leftrightarrow$	$\neg$	$(q \vee p)$	$\rightarrow$	$(p \wedge$	$\neg q$
$\overline{F}$	F	Τ	Τ	Τ	F	F	F	Τ
$\mathbf{F}$	Τ	T	$\mathbf{F}$	F	${ m T}$	T	f	$\mathbf{F}$
F	N	${ m T}$	N	N	N	N	F	N
Τ	F	F	Τ	F	${ m T}$	T	T	Τ
Τ	Τ	F	Τ	F	${ m T}$	$\mathbf{F}$	$\mathbf{F}$	F
Τ	N	F	Τ	F	${ m T}$	N	N	N
N	F	N	N	N	N	N	N	Τ
N	Τ	N	N	F	${ m T}$	N	$\mathbf{F}$	F
N	N	N	N	N	N	N	N	N

## **Q11**

 $\mathfrak{t}\neg(A\wedge\neg C)\wedge B$  all branches closed under rule 1, relation holds in fde.



### Q12

a) false. since there are no theorems in K3, its not possible to find a formula that is a theorem in both K3 and LP.

- b) true. the shared content is that if the premise is satisfied(true or both), then the conclusion be be satisfied also.
- c) true. truth table and tableaux both provide ways to determine truth value of a formula in all 4 logic theories.
  - d) true.

e)false. if a predicate is that 'at most five of some thing', then in particular, it could be 0 or fewer, so 'at least one...' is not implied here.