### E. Profit Measures

## PROFIT VECTOR

 $Pr_t$  is the profit for year t at the end of year t given the contract is in force at the beginning of year t.

$$Pr_0 = -(E_0 + {}_0V)$$

 $E_0$  expenses are called *pre-contract expenses* 

For t > 0, the profit of a life insurance contract on (x) is:

$$Pr_{t} = (t-1V + G_{t} - E_{t}) (1+i)$$
$$-q_{x+t-1} (DB_{t}) - p_{x+t-1} (tV)$$

Understand the above formula because you need to be able to adjust it for different types of contracts

Change in reserve method:

$$Pr_t = (G_t - E_t) (1+i) + \Delta_t V - EDB_t$$

$$\Delta_t V = {}_{t-1}V \times (1+i) - p_{x+t-1} \times {}_tV$$

# PROFIT MEASURES

Risk discount rate (a.k.a. hurdle rate) = r

$$NPV = \sum_{t=0}^{n} \Pi_t v_r^t$$

Partial NPV at time t:

$$NPV(t) = \sum_{k=0}^{t} \Pi_k v_r^k$$

IRR is j such that:

$$\sum_{t=0}^{n} \Pi_t \, v_j^t = 0$$

Discount Payback Period:

$$DPP = \min\{t : NPV(t) \ge 0\}$$

$$profit margin = \frac{NPV}{P\ddot{a}_{x:\overline{n}1}}$$

#### PROFIT SIGNATURE

 $\Pi_t$  is the profit for year t at the end of year t given the contract is in force at issue.

$$\Pi_t = \begin{cases} \Pr_0 & t = 0\\ t - 1p_x \cdot \Pr_t & t > 0 \end{cases}$$

where  $t-1p_x$  is the probability that policy is in force at beginning of year t.

#### ZEROIZATION

- 1. Start with the last year and solve for the reserve such that the profit for the year is zero.
- 2. Working backwards continue this process for each year.
- 3. If a reserve is negative, then set the reserve to zero.
- 4. Perform profit test using these new **zeroized** reserves.

#### MULTIPLE STATE MODELS

- 1. For each in-force state i, calculate the profit vector  $\Pr^{(i)}$ .
- $2. \ \,$  The profit signature now multiplies by the probability of being in the in-force state

$$\Pi_t = \begin{cases} \Pr_t & t = 0, 1\\ \sum_{\text{all } i} t^{-1} p_x^{0i} \Pr_t^{(i)} & t = 2, 3, \dots \end{cases}$$