第7章作业

一. 基础部分: 补全代码

FILE: lidar_localization/src/model/kalman_filter/error_state_kalman_filter.cpp

滤波算法主要包括预测(Update函数)和观测(Correct函数)两个部分:

预测部分接收imu数据,基于惯性解算更新名义值,基于状态方程更新误差值。 观测部分同时接收imu数据和定位数据,首先利用imu数据进行预测,保证状态与定位数据时间同步,然 后基于观测方程计算误差值,最后利用误差值对名义值进行修正,并将误差值清零。

修改1

FUNCTION: ErrorStateKalmanFilter::UpdateOdomEstimation

```
void ErrorStateKalmanFilter::UpdateOdomEstimation(
   Eigen::Vector3d &linear_acc_mid, Eigen::Vector3d &angular_vel_mid) {
 // TODO: this is one possible solution to previous chapter, IMU Navigation,
 // assignment
 //
 // get deltas:
   size_t index_curr_ = 1;
   size_t index_prev_ = 0;
   Eigen::Vector3d angular_delta;
   GetAngularDelta(index_curr_, index_prev_, angular_delta,
                          // 获取等效旋转矢量, 保存角速度中值
 angular_vel_mid);
 // update orientation:
   Eigen::Matrix3d R_curr_;
   Eigen::Matrix3d R_prev_;
   UpdateOrientation(angular_delta, R_curr_, R_prev_);
      更新四元数
 // get velocity delta:
   double delta_t_ = 0.0;
   Eigen::Vector3d velocity_delta_;
   GetVelocityDelta(index_curr_, index_prev_, R_curr_, R_prev_, delta_t_,
velocity_delta_, linear_acc_mid);
 // save mid-value unbiased linear acc for error-state update:
 // update position:
   UpdatePosition(delta_t_, velocity_delta_);
}
```

修改2

FUNCTION:ErrorStateKalmanFilter::SetProcessEquation

修改3

FUNCTION:ErrorStateKalmanFilter::UpdateErrorEstimation

```
void ErrorStateKalmanFilter::UpdateErrorEstimation(
   const double &T, const Eigen::Vector3d &linear_acc_mid,
   const Eigen::Vector3d &angular_vel_mid) {
 static MatrixF F 1st:
 static MatrixF F_2nd;
// TODO: update process equation:
 UpdateProcessEquation(linear_acc_mid , angular_vel_mid); // 更新状态方程
 // TODO: get discretized process equations: // 非线性化
   F_1st = F_ * T;  // T kalman 周期
   MatrixF F = MatrixF::Identity() + F_1st;
   MatrixB B = B_*T;
 // TODO: perform Kalman prediction
     P_{-} = F * P_{-} * F.transpose() + B * Q_{-} * B.transpose();
                                                                       //
只有方差进行了计算
}
```

修改4

FUNCTION: Error State Kalman Filter:: Correct Error Estimation Pose

```
G = GPose_;
// set measurement C

// TODO: set Kalman gain:
K = P_ * G.transpose() * ( G * P_ * G.transpose() + RPose_
).inverse();
}
```

修改5

FUNCTION:ErrorStateKalmanFilter::EliminateError

```
void ErrorStateKalmanFilter::EliminateError(void) {
 // 误差状态量 X_ : 15*1
 // TODO: correct state estimation using the state of ESKF
 // a. position:
 // do it!
 pose_.block<3, 1>(0, 3) = pose_.block<3, 1>(0, 3) - X_.block<3, 1>
(kIndexErrorPos, 0 ); // 减去error
 // b. velocity:
 // do it!
 vel_ = vel_ - X_.block<3,1>(kIndexErrorVel, 0 );
 // c. orientation:
 // do it!
 Eigen::Matrix3d delta_R = Eigen::Matrix3d::Identity() -
Sophus::S03d::hat(X_.block<3,1>(kIndexErrorOri, 0)).matrix();
                                                                 // 失准角
的反对称矩阵
 Eigen::Quaterniond dq = Eigen::Quaterniond(delta_R);
 dq = dq.normalized(); // 为了保证旋转矩阵是正定的
 pose\_.block<3, 3>(0, 0) = pose\_.block<3,3>(0,0) * dq.toRotationMatrix();
 // d. gyro bias:
 gyro_bias_ -= X_.block<3, 1>(kIndexErrorGyro, 0);
 // e. accel bias:
 accl_bias_ -= X_.block<3, 1>(kIndexErrorAccel, 0);
}
```

运行

代码运行命令:

```
roslaunch lidar_localization kitti_localization.launch
```

播放数据集命令:

```
rosbag play kitti_lidar_only_2011_10_03_drive_0027_synced.bag
```

保存里程计:

```
rosservice call /save_odometry
```

数据位于:

```
src/lidar_localization/slam_data/trajectory
```

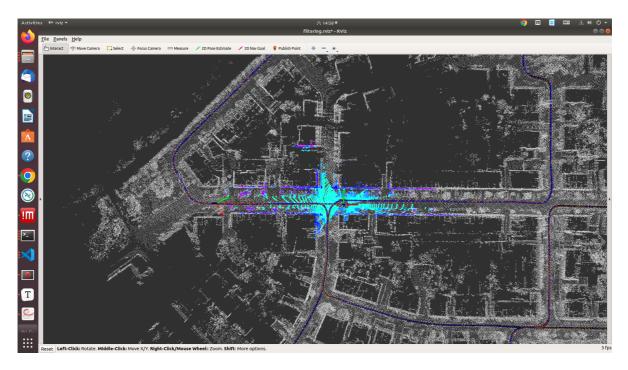
evo工具运行命令:

```
# a. laser 输出评估结果,并以zip的格式存储:
evo_ape kitti ground_truth.txt laser.txt -r full --plot --plot_mode xy --
save_results ./laser.zip
# b. fused 输出评估结果,并以zip的格式存储:
evo_ape kitti ground_truth.txt fused.txt -r full --plot --plot_mode xy --
save_results ./fused.zip
#c. 比较 laser fused 一并比较评估
evo_res *.zip -p
```

默认参数 (参数1)

```
covariance:
    prior:
        pos: 1.0e-6
       vel: 1.0e-6
        ori: 1.0e-6
        epsilon: 1.0e-6
        delta: 1.0e-6
    process:
        gyro: 1.0e-4
        accel: 2.5e-3
        bias_accel: 2.5e-3
        bias_gyro: 1.0e-4
   measurement:
       pose:
        pos: 1.0e-2
        ori: 1.0e-2
        pos: 1.0e-2
        vel: 2.5e-1
```

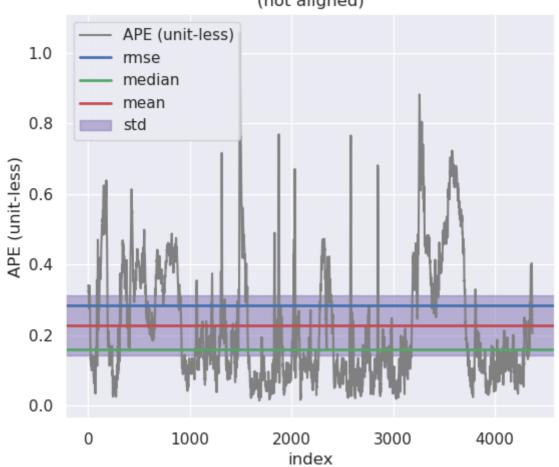
RVIZ效果

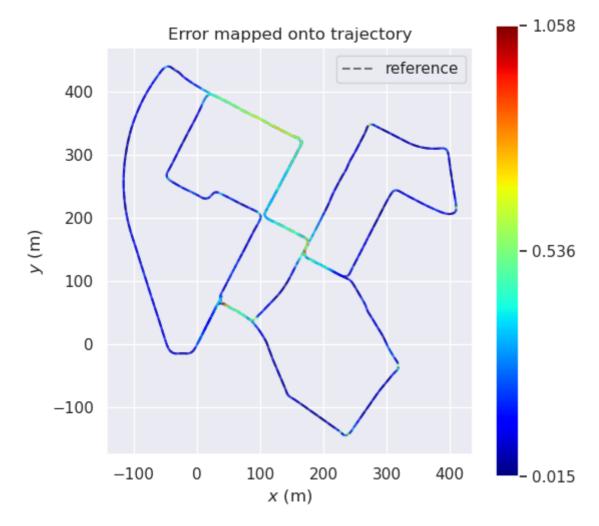


EVO评估

雷达:

APE w.r.t. full transformation (unit-less) (not aligned)





```
max 1.058145

mean 0.228117

median 0.160389

min 0.014763

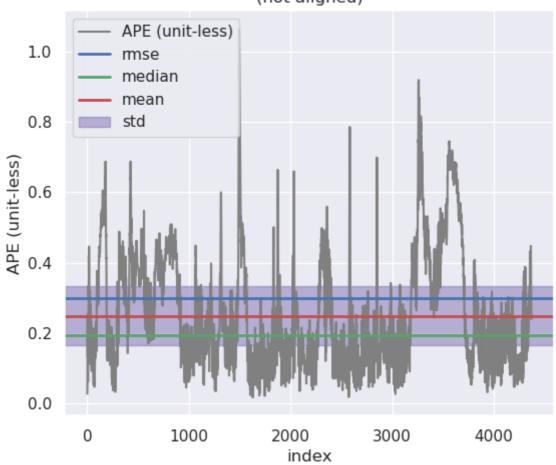
rmse 0.284866

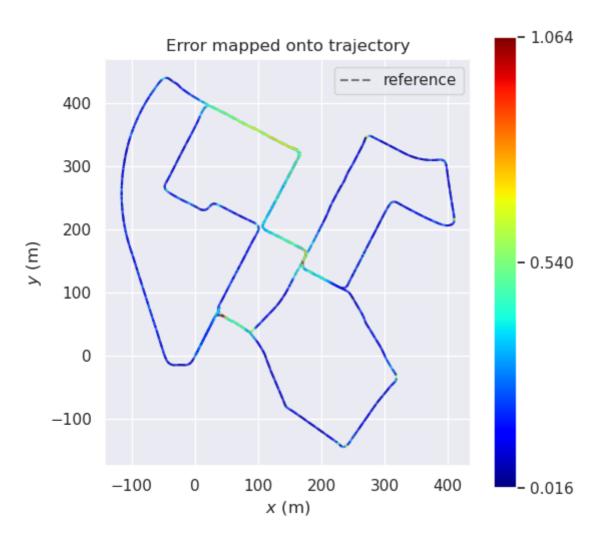
sse 354.780742

std 0.170620
```

融合后:

APE w.r.t. full transformation (unit-less) (not aligned)



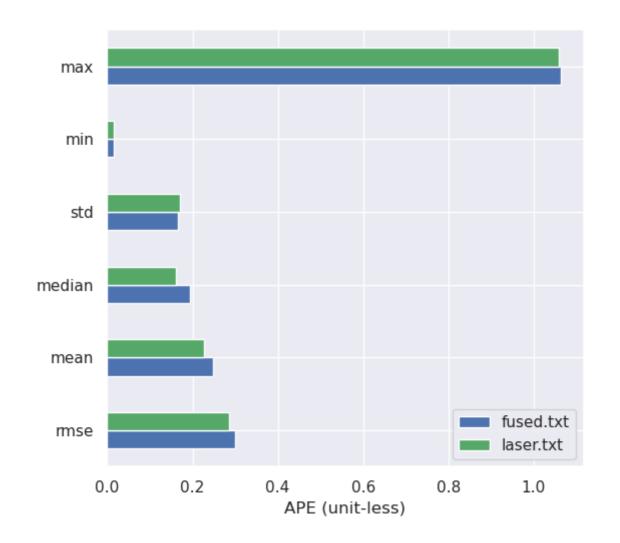


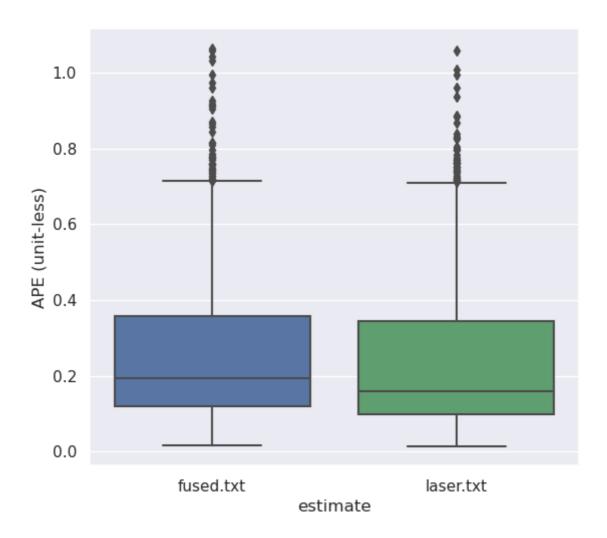
```
max 1.063830
mean 0.248405
median 0.193894
min 0.016452
rmse 0.299318
sse 391.693699
std 0.166992
```

对比:

rmse mean median std min max \
fused.txt 0.299318 0.248405 0.193894 0.166992 0.016452 1.06383
laser.txt 0.284866 0.228117 0.160389 0.17062 0.014763 1.058145

sse
fused.txt 391.693699
laser.txt 354.780742





结论

默认参数下, 融合的效果是差于单雷达的效果的, 基本差不多。

二.参数优化

参数修改 (参数6)

```
covariance:
    prior:
        pos: 1.0e-6
       vel: 1.0e-6
        ori: 1.0e-6
        epsilon: 1.0e-6
        delta: 1.0e-6
    process:
       gyro: 1.0e-4
        accel: 2.5e-3
        bias_accel: 2.5e-3
        bias_gyro: 1.0e-4
    measurement:
       pose:
        pos: 1.0e-4
        ori: 1.0e-4
        pos: 1.0e-4
       vel: 2.5e-3
```

EVO评估

```
rmse mean median std min max \
fused.txt 0.284697 0.227977 0.160314 0.170526 0.014329 1.058306
laser.txt 0.284696 0.227975 0.160564 0.170527 0.014763 1.058145

sse
fused.txt 354.848121
```

. . . .

laser.txt 354.846029

结论

经过参数调整,融合的效果基本和单雷达的效果一致。

三.不考虑随机游走的模型推导

公式推导

状态方程:

$$\delta \dot{x} = F_t \delta x + B_t w$$

状态量:

$$egin{aligned} \delta \dot{m{p}} &= \delta m{v} \ \delta \dot{m{v}} &= -m{R_t} [m{a_t} - m{b_{a_t}}]_{ imes} \delta m{ heta} + m{R_t} \left(m{n_a} - \delta m{b_a}
ight) \ \delta \dot{m{\theta}} &= - [m{\omega}_t - m{b}_{\omega_t}]_{ imes} \delta m{ heta} + m{n}_{\omega} - \delta m{b}_{\omega} \ \delta \dot{m{b}}_a &= 0 \ \delta \dot{m{b}}_w &= 0 \end{aligned}$$

过程噪声部分:

线性kalman:

非线性kalman:

$$m{Q} = egin{bmatrix} m{Q}_a & m{Q}_\omega & m{0} & m{0} \end{bmatrix} \ m{B}_{k-1} = egin{bmatrix} m{0} & m{0} & m{0} & m{0} & m{0} \ m{R}_{k-1} T & m{0} & m{0} & m{0} \ m{0} & m{I}_3 T & m{0} & m{0} \ m{0} & m{0} & m{0} & m{0} \ m{0} & m{0} & m{0} & m{0} \end{bmatrix}$$

工程实现

在 kitti_filtering.yaml 中添加bias_flag选项,以选择是否考虑使用随机游走。

FILE: src/lidar_localization/config/filtering/kitti_filtering.yaml

```
covariance:
       prior:
           pos: 1.0e-6
           vel: 1.0e-6
           ori: 1.0e-6
           epsilon: 1.0e-6
           delta: 1.0e-6
       process:
           gyro: 1.0e-4
           accel: 2.5e-3
           bias_accel: 2.5e-3
           bias_gyro: 1.0e-4
           bias_flag: true
       measurement:
           pose:
               pos: 1.0e-4
               ori: 1.0e-4
           pos: 1.0e-4
           vel: 2.5e-3
```

代码修改

FUNCTION:ErrorStateKalmanFilter::ErrorStateKalmanFilter

```
COV.PROCESS.BIAS_FLAG =
  node["covariance"]["process"]["bias_flag"].as<bool>();
```

FUNCTION:ErrorStateKalmanFilter::ErrorStateKalmanFilter

```
// c. process noise:
    Q_.block<3, 3>(kIndexNoiseAccel, kIndexNoiseAccel) = COV.PROCESS.ACCEL *
Eigen::Matrix3d::Identity();
    Q_.block<3, 3>(kIndexNoiseGyro, kIndexNoiseGyro) = COV.PROCESS.GYRO *
Eigen::Matrix3d::Identity();
    if (COV.PROCESS.BIAS_FLAG) {
        Q_.block<3, 3>(kIndexNoiseBiasAccel, kIndexNoiseBiasAccel) =
        COV.PROCESS.BIAS_ACCEL * Eigen::Matrix3d::Identity();
        Q_.block<3, 3>(kIndexNoiseBiasGyro, kIndexNoiseBiasGyro) =
        COV.PROCESS.BIAS_GYRO * Eigen::Matrix3d::Identity();
    }
}
```

FUNCTION:ErrorStateKalmanFilter::SetProcessEquation

```
// b. set process equation for delta ori:
F_.block<3, 3>(kIndexErrorOri, kIndexErrorOri) = -
Sophus::SO3d::hat(w_b).matrix();
B_.block<3, 3>(kIndexErrorVel, kIndexErrorAccel) = C_nb;
if(COV.PROCESS.BIAS_FLAG){ // 判断是否考虑随机游走
    B_.block<3, 3>(kIndexErrorAccel, kIndexNoiseBiasAccel) =
Eigen::Matrix3d::Identity();
    B_.block<3, 3>(kIndexErrorGyro, kIndexNoiseBiasGyro) =
Eigen::Matrix3d::Identity();
}
```

FUNCTION:ErrorStateKalmanFilter::UpdateErrorEstimation

四.对比分析

当 Q/R 越大,则表示Q越大,预测的噪声越大,系统更相信观测;当 Q/R 越小,表示 R 越大,观测的噪声越大,系统更相信预测;

即当 Q 减少,R 不变时,更相信预测值;当 Q 增大,R 减小时,更相信观测值;当 R 减少,Q 不变时,更相信观测值;当 R 增大,Q 不变时,更相信预测值。

参数1:

```
covariance:
   prior:
        pos: 1.0e-6
       vel: 1.0e-6
        ori: 1.0e-6
        epsilon: 1.0e-6
        delta: 1.0e-6
   process:
       gyro: 1.0e-4
        accel: 2.5e-3
        bias_accel: 2.5e-3
        bias_gyro: 1.0e-4
   measurement:
        pose:
        pos: 1.0e-2
        ori: 1.0e-2
        pos: 1.0e-2
        vel: 2.5e-1
```

不考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.952761 0.721738 0.526481 0.621971 0.028239 3.90681
laser.txt 0.284661 0.227867 0.160084 0.170612 0.014763 1.058145

sse
fused.txt 3954.177354
laser.txt 352.974659
```

考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.299318 0.248405 0.193894 0.166992 0.016452 1.06383
laser.txt 0.284866 0.228117 0.160389 0.17062 0.014763 1.058145

sse
fused.txt 391.693699
laser.txt 354.780742
```

参数2:

```
covariance:
       prior:
           pos: 1.0e-6
           vel: 1.0e-6
           ori: 1.0e-6
           epsilon: 1.0e-6
           delta: 1.0e-6
       process:
           gyro: 1.0e-4
           accel: 2.5e-3
           bias_accel: 2.5e-3
           bias_gyro: 1.0e-4
       measurement:
           pose:
           pos: 1.0e-4
           ori: 1.0e-4
           pos: 1.0e-4
           vel: 2.5e-3
```

不考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.438888 0.357005 0.285806 0.255285 0.026705 2.178491
laser.txt 0.284607 0.227924 0.160545 0.170445 0.014763 1.058145

sse
fused.txt 839.64202
laser.txt 353.083373
```

考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.299679 0.24884 0.194298 0.166991 0.018342 1.065207
laser.txt 0.28465 0.22786 0.160084 0.170604 0.014763 1.058145

sse
fused.txt 391.201546
laser.txt 352.948792
```

参数3:

```
covariance:
   prior:
        pos: 1.0e-6
        vel: 1.0e-6
        ori: 1.0e-6
        epsilon: 1.0e-6
        delta: 1.0e-6
   process:
       gyro: 1.0e-4
        accel: 2.5e-3
        bias_accel: 2.5e-3
        bias_gyro: 1.0e-4
   measurement:
        pose:
        pos: 1.0e-6
        ori: 1.0e-6
        pos: 1.0e-6
        vel: 2.5e-5
```

不考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.354642 0.289052 0.226475 0.205474 0.021593 1.695696
laser.txt 0.284835 0.228046 0.160133 0.170663 0.014763 1.058145

sse
fused.txt 548.486621
laser.txt 353.811309
```

考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.289648 0.235745 0.175245 0.168287 0.020645 1.116669
laser.txt 0.284479 0.227683 0.159882 0.170555 0.014763 1.058145

sse
fused.txt 365.955408
laser.txt 353.010395
```

参数4:

```
covariance:
    prior:
        pos: 1.0e-6
        vel: 1.0e-6
        ori: 1.0e-6
        epsilon: 1.0e-6
        delta: 1.0e-6
        process:
        gyro: 1.0e-2
        accel: 2.5e-1
        bias_accel: 2.5e-1
```

```
bias_gyro: 1.0e-2
measurement:
    pose:
    pos: 1.0e-6
    ori: 1.0e-6
    pos: 1.0e-6
    vel: 2.5e-5
```

不考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.32493 0.263788 0.204127 0.189725 0.017245 1.290073
laser.txt 0.284226 0.227177 0.1588 0.170808 0.014763 1.058145

sse
fused.txt 460.115907
laser.txt 352.059608
```

考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.28542 0.229484 0.16391 0.169711 0.01556 1.062555
laser.txt 0.284606 0.227953 0.160545 0.170405 0.014763 1.058145

sse
fused.txt 356.895876
laser.txt 354.863676
```

参数5:

```
covariance:
   prior:
        pos: 1.0e-6
       vel: 1.0e-6
        ori: 1.0e-6
        epsilon: 1.0e-6
        delta: 1.0e-6
   process:
        gyro: 1.0e-1
        accel: 2.5e-0
        bias_accel: 2.5e-0
        bias_gyro: 1.0e-1
   measurement:
        pose:
        pos: 1.0e-6
        ori: 1.0e-6
        pos: 1.0e-6
        vel: 2.5e-5
```

不考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.305093 0.248036 0.187818 0.177651 0.018315 1.099339
laser.txt 0.284907 0.228132 0.160604 0.170669 0.014763 1.058145

sse
fused.txt 404.905921
laser.txt 353.098237
```

考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.284888 0.228233 0.159983 0.170501 0.015389 1.059236 laser.txt 0.284809 0.22809 0.160186 0.170561 0.014763 1.058145

sse fused.txt 354.99839 laser.txt 354.803164
```

参数6:

```
covariance:
   prior:
        pos: 1.0e-6
       vel: 1.0e-6
       ori: 1.0e-6
        epsilon: 1.0e-6
        delta: 1.0e-6
   process:
        gyro: 1.0e-1
        accel: 2.5e-0
        bias_accel: 2.5e-0
        bias_gyro: 1.0e-1
   measurement:
        pose:
        pos: 1.0e-7
        ori: 1.0e-7
        pos: 1.0e-7
        vel: 2.5e-6
```

不考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.29411 0.237169 0.17132 0.17393 0.010965 1.015445
laser.txt 0.284321 0.227608 0.159898 0.170391 0.014763 1.058145

sse
fused.txt 378.613827
laser.txt 353.830077
```

考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.284697 0.227977 0.160314 0.170526 0.014329 1.058306
laser.txt 0.284696 0.227975 0.160564 0.170527 0.014763 1.058145

sse
fused.txt 354.848121
laser.txt 354.846029
```

参数7:

```
covariance:
   prior:
        pos: 1.0e-6
       vel: 1.0e-6
       ori: 1.0e-6
        epsilon: 1.0e-6
        delta: 1.0e-6
   process:
       gyro: 1.0e-6
        accel: 2.5e-5
        bias_accel: 2.5e-5
        bias_gyro: 1.0e-6
   measurement:
        pose:
        pos: 1.0e-6
        ori: 1.0e-6
        pos: 1.0e-6
        vel: 2.5e-5
```

不考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.452069 0.378197 0.327996 0.247655 0.022795 1.967658 |
laser.txt 0.284223 0.2275 0.159953 0.170371 0.014763 1.058145 |
sse
fused.txt 891.03615 |
laser.txt 352.212622
```

考虑随机游走:

```
rmse mean median std min max \
fused.txt 0.294391 0.242138 0.185901 0.167438 0.013392 1.10459
laser.txt 0.284545 0.227908 0.160545 0.170365 0.014763 1.058145

sse
fused.txt 378.471748
laser.txt 353.578696
```

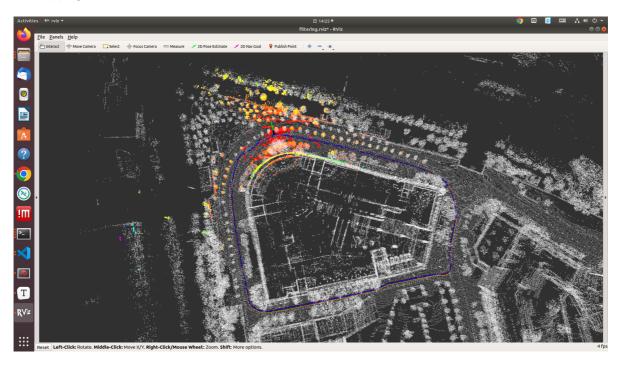
五.实车部署

实车硬件如下:

1. 松灵Scout2, 车速为1.5m/s

- 2. 速腾16线雷达
- 3. SBG-ellipse-N 九轴惯导+单天线RTK

rviz效果



evo评估

rmse mean median std min max \
fused.txt 0.674251 0.62103 0.606449 0.262556 0.118306 1.116956 |
laser.txt 0.673647 0.620549 0.605487 0.262144 0.118514 1.114238 |

sse |
fused.txt 276.405189 |
laser.txt 275.910958

总结和思考

总结

参数表:

	参数1	参数2	参数3	参数4	参数5	参数6	参数7
Q	gyro: 1.0e-4 accel: 2.5e-3 bias_accel: 2.5e-3 bias_gyro: 1.0e-4	gyro: 1.0e-4 accel: 2.5e-3 bias_accel: 2.5e-3 bias_gyro: 1.0e-4	gyro: 1.0e-4 accel: 2.5e-3 bias_accel: 2.5e-3 bias_gyro: 1.0e-4	gyro: 1.0e-2 accel: 2.5e-1 bias_accel: 2.5e-1 bias_gyro: 1.0e-2	gyro: 1.0e- 1 accel: 2.5e- 0 bias_accel: 2.5e-0 bias_gyro: 1.0e-1	gyro: 1.0e- 1 accel: 2.5e- 0 bias_accel: 2.5e-0 bias_gyro: 1.0e-1	gyro: 1.0e-6 accel: 2.5e-5 bias_accel: 2.5e-5 bias_gyro: 1.0e-6
R	pos: 1.0e-2 ori: 1.0e-2 pos: 1.0e-2 vel: 2.5e-1	pos: 1.0e-4 ori: 1.0e-4 pos: 1.0e-4 vel: 2.5e-3	pos: 1.0e-6 ori: 1.0e-6 pos: 1.0e-6 vel: 2.5e-5	pos: 1.0e-6 ori: 1.0e-6 pos: 1.0e-6 vel: 2.5e-5	pos: 1.0e-6 ori: 1.0e-6 pos: 1.0e-6 vel: 2.5e-5	pos: 1.0e-7 ori: 1.0e-7 pos: 1.0e-7 vel: 2.5e-6	pos: 1.0e-6 ori: 1.0e-6 pos: 1.0e-6 vel: 2.5e-5

kitti数据集不同参数融合指标对比,选取sse作为评判指标参数,考虑随机游走:

parameter/trajectory	参数1	参数2	参数3	参数4	参数5	参数6	参数7
laser	354.780742	352.948792	353.010395	354.863676	354.803164	354.846029	353.578696
fused	391.693699	391.201546	365.955408	356.895876	354.99839	354.848121	378.471748

kitti数据集不同参数融合指标对比,选取sse作为评判指标参数,不考虑随机游走:

parameter/trajectory	参数1	参数2	参数3	参数4	参数5	参数6	参数7
laser	52.974659	353.083373	353.811309	352.059608	353.098237	353.830077	352.212622
fused	3954.177354	839.64202	548.486621	460.115907	404.905921	378.613827	891.03615

从指标得出这次实验的结论:

- 1. 考虑随机游走能够提高精度;
- 2. 单雷达下的精度比融合后的精度高,则说明观测更加可靠;增大Q,减小R;或者增加Q,R不变;或者Q不变,减小R;这些都代表更相信观测,能提高精度。相反,减小Q,R不变;Q不变,增大R;减小Q,增大R;这些代表更相信预测,则减小精度。

思考和疑问

1. 为什么调不到一组融合后比单雷达下精度高的参数? 无论是在kitti数据集还是自采数据集, 融合后的精度都是比单雷达要低一些? 原因是?