

Slide 19

1/ Favour Qubits with same value

x	y	$ax+by+cx+y+d$		
0	0	0	$d=0$	①
0	1	1	$b+d=1$	②
1	0	1	$a+d=1$	③
1	1	0	$a+b+c+d=0$	④

Substitute x, y , into above

$$\begin{aligned} \text{① in ④} \quad a+b+c &= 0 \quad \text{⑤} \\ \text{① in ②} \quad b+0 &= 1 \quad \text{⑥} \Rightarrow b=1 \\ \text{① in ③} \quad a+0 &= 1 \quad \text{⑦} \Rightarrow a=1 \\ \text{⑥, ⑦ in ⑤} \quad 1+1+c &= 0 \Rightarrow c=-2 \end{aligned}$$

$$\Rightarrow \text{objective} = ax+by+cx+y+d$$
$$= \underline{\underline{x + y - 2xy}}$$

2/ Manual computation

x	y	$x+y-2xy$
0	0	0
0	1	1
1	0	1
1	1	0

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3, Favour Qubits with different value

x	y	$ax+by+cx+dy+d$	Equation	
0	0	1	$d=1$	①
0	1	0	$b+d=0$	②
1	0	0	$a+d=0$	③
1	1	1	$a+b+c+d=1$	④

① in ② $b+1=0 \Rightarrow b=-1$

① in ③ $a+1=0 \Rightarrow a=-1$

④ $\Rightarrow -1-1+c+1=1 \Rightarrow c=2$

$$\begin{aligned}\text{Objective} &= ax+by+cx+dy+d \\ &= -x-y+2x+1\end{aligned}$$

4, Manual computation

x	y	$-x-y+2x+1$
0	0	1
0	1	0
1	0	0
1	1	1