



Phase IV (Updated): Physical Constants and Fundamental Laws

This document refines the Phase IV discussion of the Recursive Structural Model (RSM) in light of thoughtful feedback. It maintains a strictly structural perspective while acknowledging where detailed mathematical development is still required. The goal is to highlight conceptual connections between RSM and fundamental physics without overstating what has been achieved.

1 Dimensionless constants and recursive ratios

Dimensionless physical constants—such as the fine-structure constant $\alpha \approx 1/137$ —play a special role because they set interaction strengths independently of units. In RSM these constants are viewed as **ratios arising from co-emergent scales**. Each level of recursion introduces new degrees of freedom; the ratios between these levels determine how strongly different modes couple.

1.1 Universality and fixed points

Near continuous phase transitions, very different systems display identical critical exponents because the correlation length diverges and the system becomes scale-free ¹. Renormalization-group flows approach fixed points characterised by a few dimensionless numbers. RSM uses this analogy to suggest that fundamental constants might represent ratios that are stable under reciprocal scaling. However, the model does not yet derive specific numerical values or their running with energy scale. Establishing such predictions would require embedding the hyperbolic grammar within the renormalization-group framework.

1.2 Hierarchy and recursion depth

The vast differences between coupling strengths and particle masses are reframed as differences in **recursion depth**. Interactions operating at a shallower recursion level—such as electromagnetism—couple more strongly than those emerging from deeper levels, like gravitation. Neutrinos and dark sector particles may reflect still deeper layers of the hyperbolic field. This conceptual map does not assign numbers but offers a structural lens through which hierarchy problems can be viewed.

1.3 Anthropic considerations

Anthropic arguments note that life requires certain constant values. Within RSM, these values arise not because they were “selected” but because only certain ratios allow co-emergent balance. Irrational ratios, such as those involving the golden ratio in quasicrystals ², avoid resonances; by analogy, the specific values of physical constants may be structurally necessary to maintain stability. This is an interpretive perspective rather than a predictive claim.

2 Thermodynamic irreversibility and temporal asymmetry

The second law of thermodynamics presents a challenge for any structural model: how do irreversible macroscopic trends emerge from reversible microscopic dynamics? In RSM the answer lies in the asymmetry between **refinement and coarsening** along the hyperbolic field.

2.1 Entropy and information distribution

Entropy measures how many microscopic states correspond to a given macroscopic description. Differential entropy remains invariant under volume-preserving transformations ³, which correspond to reversible flows. Irreversibility enters when we discard fine information—when we coarse-grain. In hyperbolic coordinates, increasing the scale parameter r represents coarsening. Because moving toward smaller r (higher precision) requires energy, spontaneous dynamics favour the direction of increasing r . This structural bias underpins the arrow of time. A full derivation of the second law would require defining explicit probability measures on G_1 and showing that coarse-graining leads to monotonic entropy increase; this remains an open project.

2.2 Fluctuations and suppression

Fluctuation theorems quantify the probability of temporary entropy decreases in small systems. Within RSM these rare events correspond to excursions toward smaller r , which are exponentially suppressed because they require concentrating information. This aligns qualitatively with fluctuation theorem results, but connecting the precise exponential factors to the hyperbolic flow parameter awaits a detailed statistical treatment.

2.3 Emergent temporal direction

Time asymmetry is not imposed externally but emerges from the structural grammar. Circulation on the hyperbolic field couples expansion in one coordinate to contraction in the other. Over many recursions the net effect is a drift toward larger scales and coarser descriptions. The second law thus reflects a **structural tendency** rather than a fundamental imbalance.

3 Quantum vacuum fluctuations and minimal circulation

Vacuum fluctuations, zero-point energies and Casimir forces illustrate how “empty” space contains activity. RSM interprets this activity as the minimal circulation required by the hyperbolic constraint.

3.1 Zero-point energy and uncertainty

In quantum mechanics a harmonic oscillator’s ground state has energy $\frac{1}{2}\hbar\omega$ because position and momentum uncertainties cannot both vanish. RSM views this as a direct analogue of $X_1Y_1 = \text{constant}$: reducing one component increases the other. Zero-point energy represents the minimal circulation that preserves the paradox. Extending this idea to quantum fields suggests that each mode carries a minimal energy. However, summing these energies leads to divergent vacuum energy density. Reconciling the structural interpretation with renormalization procedures is a substantial mathematical challenge.

3.2 Casimir effect and boundary conditions

When conducting plates are placed close together, certain electromagnetic modes are excluded, leading to a measurable force. RSM interprets this as truncating the recursion depth: the allowed hyperbolic orbits are restricted, shifting the balance point. Qualitatively this explains why the Casimir force depends on plate separation. Quantitatively reproducing the precisely measured force requires integrating RSM with full quantum electrodynamics; this has yet to be achieved.

3.3 Cosmological constant and scale separation

The enormous discrepancy between quantum field theory's vacuum energy and observed dark energy is recast as a mismatch between **local** and **global** recursion scales. Local zero-point energies arise from minimal circulation at short scales, while the cosmological constant reflects circulation at the scale of the universe. Treating these contributions separately rather than summing them may alleviate the tension. Developing a multiscale formalism that respects both hyperbolic grammar and general covariance is a key research direction.

Conclusion and outlook

This updated Phase IV document emphasises **interpretive clarity and restraint**. The recursive structural model offers a fresh lens through which to view dimensionless constants, entropy and vacuum fluctuations, but does not claim to solve these problems. Each section identifies conceptual parallels and highlights where rigorous integration with established theories is needed. Future work will require collaboration with experts in quantum field theory and statistical mechanics to turn these structural insights into quantitative statements.

¹ Critical phenomena - Wikipedia

https://en.wikipedia.org/wiki/Critical_phenomena

² Quasicrystal - Wikipedia

<https://en.wikipedia.org/wiki/Quasicrystal>

³ entropy190327.pdf

<https://sites.math.rutgers.edu/~oldstein/papers/entropy190327.pdf>