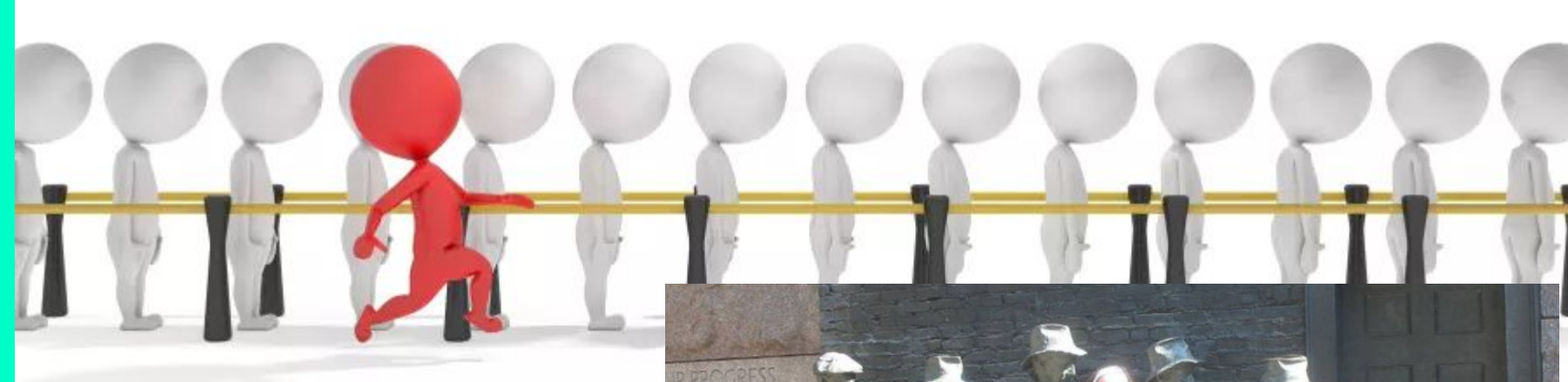


QUEUES

Lecture 6

MIC

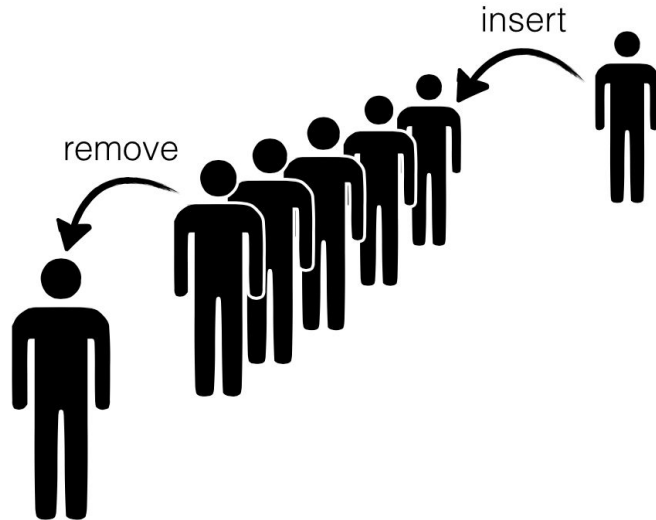


QUEUES (I'M CHEATING HERE 😊)

THE QUEUE ADT

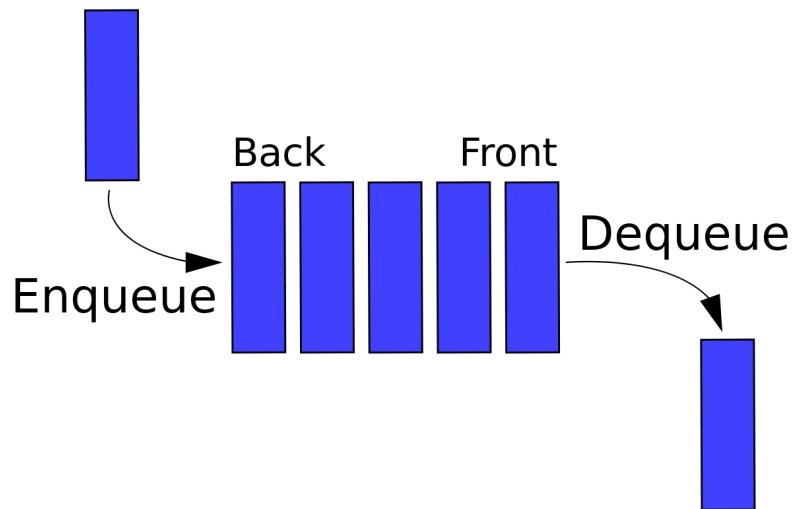
A **Queue** is a collection of objects inserted and removed according to the

First In First Out (FIFO) principle. Think of a queue of people to Rubios



QUEUE OPERATIONS

Enqueue (insert) and **Dequeue (remove)** are the two main operations





QUESTION

When using enqueue operation to place the following items in a queue:

enqueue(10)

enqueue(20)

enqueue(30)

enqueue(0)

enqueue(-30)

The output when dequeuing from the queue is:

A: 10, 20, 30, 0, -30

B: -30, 0, 10, 20, 30

C: 30, 10, 20, 0, -30

D: -30, 0, 30, 20, 10

E: 0, 30, -30, 10, 20

IMPLEMENTATION. ARRAYS. $O(1)$

Main update methods:

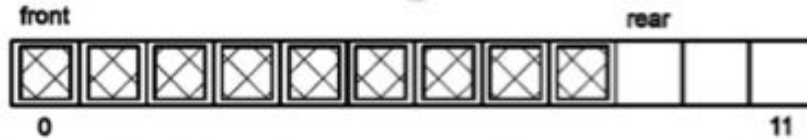
- Enqueue (e)
- Dequeue ()

Additional useful methods

- Peek(): Same as dequeue, but does not remove the element
- Empty(): Boolean, True when the queue is *empty*
- Size(): Returns the size of the queue

(INCORRECT)
ATTEMPTS TO
IMPLEMENT IT

REGULAR ARRAY: DEQUEUE



(a) Queue.front is always at 0 – shift elements *left* on dequeue().

```
def dequeue():  
    # potential issue if empty  
    # for now, assume not empty  
  
    elem = array[front]  
    # You code is here #  
    return elem
```

Select the correct code to delete from below:

A: `front = front + 1`

C:

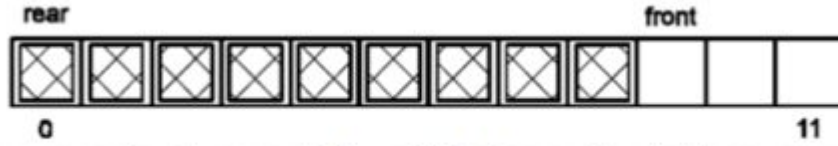
```
for i in range(rear):  
    array[i] = array[i+1]  
  
rear = rear - 1
```

B: `rear = rear - 1`

D: None of these are correct



REGULAR ARRAY: ENQUEUE



(b) `Queue.rear` is always at 0 – shift elements *right* on `enqueue()`.

```
def enqueue(elem):  
    # potential issue if full  
    # for now, assume not empty  
    # Your code is here #  
    front = front + 1
```

Select the correct code to insert from below:

A: `array[0] = elem`

C:

```
for i in range(front):  
    array[i+1] = array[i]  
  
array[front] = elem
```

B: `array[front] = elem`

D: None of these are correct

ISSUES

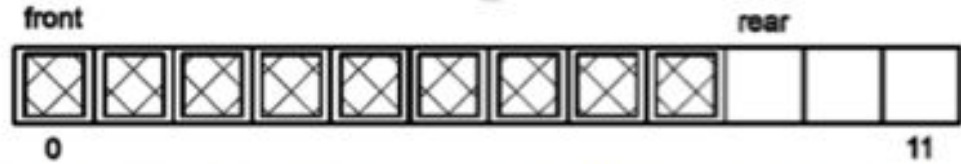
Dequeue:



(a) Queue.*front* is always at 0 – shift elements *left* on dequeue().

ISSUES

Dequeue:



(a) Queue.*front* is always at 0 – shift elements *left* on dequeue().

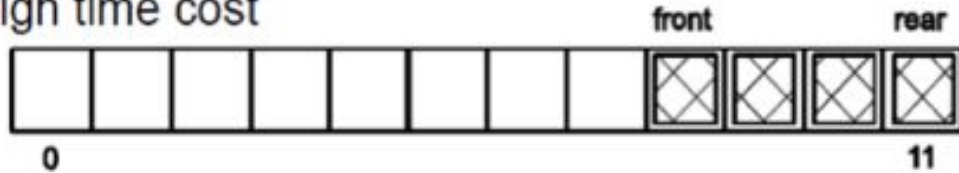


Enqueue:

(b) Queue.*rear* is always at 0 – shift elements *right* on enqueue().

REGULAR ARRAY

- Neither of those solutions is very good as they both involve *moving all the existing* data elements, which has high time cost

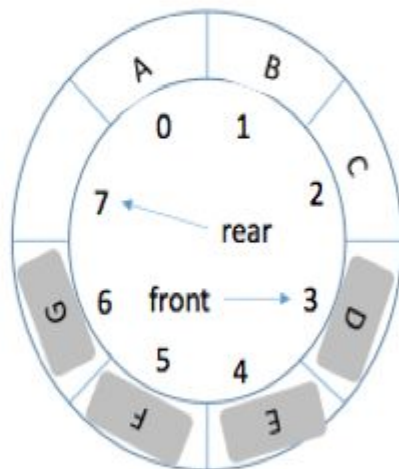
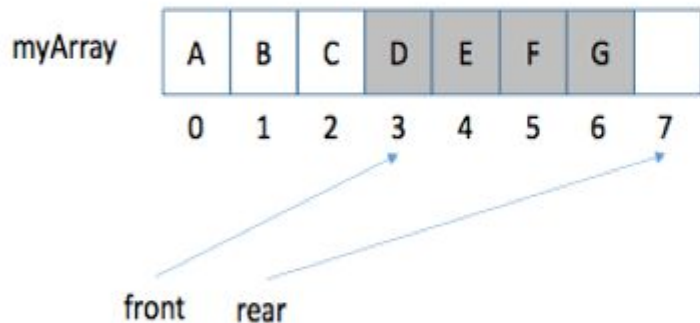


- Idea: Instead of moving data elements to a fixed position for *front* when removing, let *front* advance through the array

Hmmm....what do we do when we now add an element to that queue at the rear? What happens when we remove several elements, and *front* catches up with *rear*?...

Making a linear array appear circular

front==head
rear==tail



front

3

rear

7

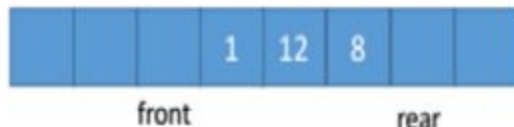
Design decisions: Where do front and rear point?

Which of these choices will work?

A



B



C

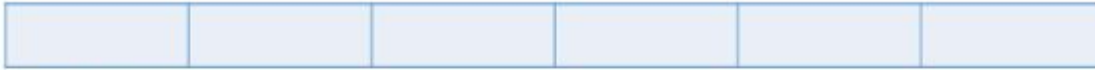


D

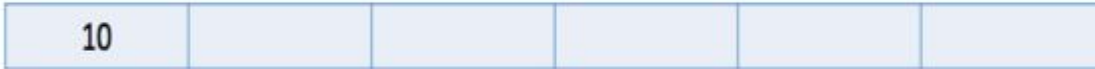
Any of these could work

QUEUES USING CIRCULAR ARRAYS

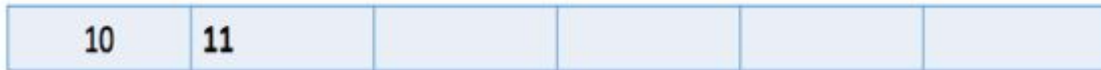
Initially empty:



front *rear*
enqueue(10)



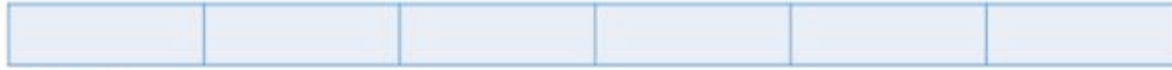
front *rear*
enqueue(11)



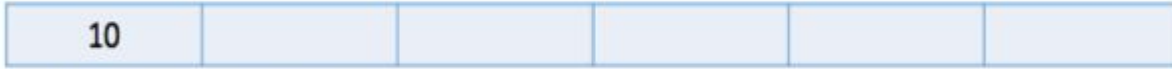
front *rear*

QUEUES USING CIRCULAR ARRAYS

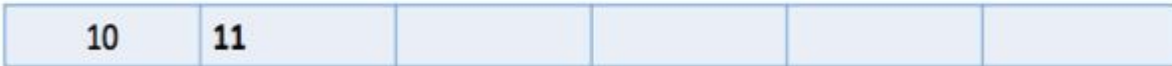
Initially empty:



front *rear*
enqueue(10)



front *rear*
enqueue(11)



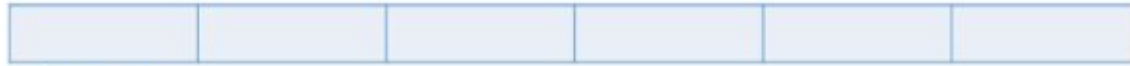
front *rear*

What should be the value of *front* after the next dequeue?

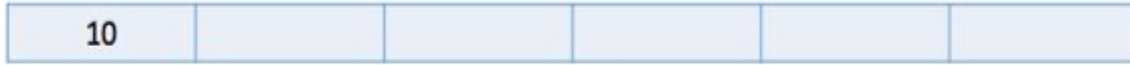
- A. 0 B. 1 C. 2 D. 5

QUEUES USING CIRCULAR ARRAYS

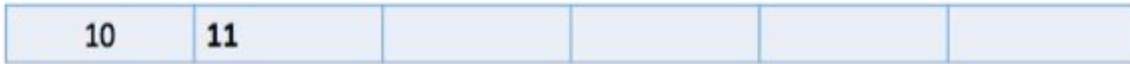
Initially empty:



front *rear*
enqueue(10)



front *rear*
enqueue(11)

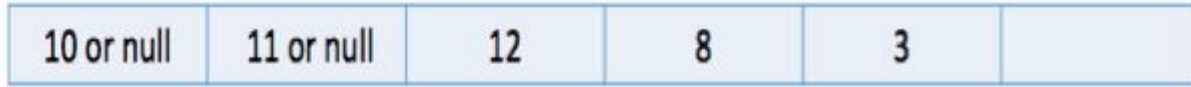


front *rear*

What should be the value stored at arr[0] after the next dequeue?

- A. 10 B. 0 C. null D. It doesn't matter

QUEUES USING CIRCULAR ARRAYS



10 or null	11 or null	12	8	3	
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enqueue(20)

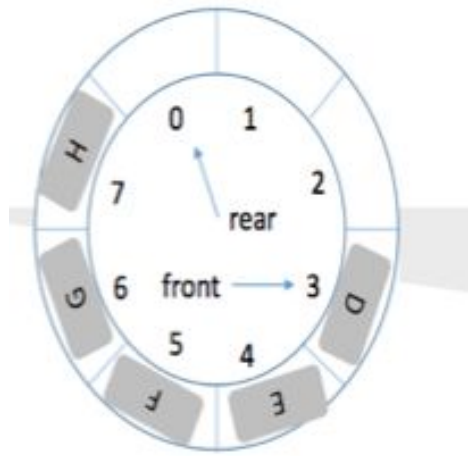
front

rear

What is the value of rear after this enqueue?

- A. 5
- B. 0
- C. 1
- D. 2
- E. Other

D: None of these are correct



```
def enqueue(elem):  
    #Your code is here#  
    size = size + 1
```

Select the correct code to insert from below:

A:

```
rear = rear + 1  
if (rear == len(array)):  
    rear = 0  
array[rear] = elem
```

B:

```
array[rear] = elem  
rear = rear + 1
```

C:

```
for i in range(rear):  
    array[i] = array[i+1]  
array[rear] = elem  
front = front - 1
```

D: None of these are correct

COMPLEXITY OF AN ARRAY BASED QUEUES

Method	Running Time
size	$O(1)$
isEmpty	$O(1)$
first	$O(1)$
enqueue	$O(1)$
dequeue	$O(1)$