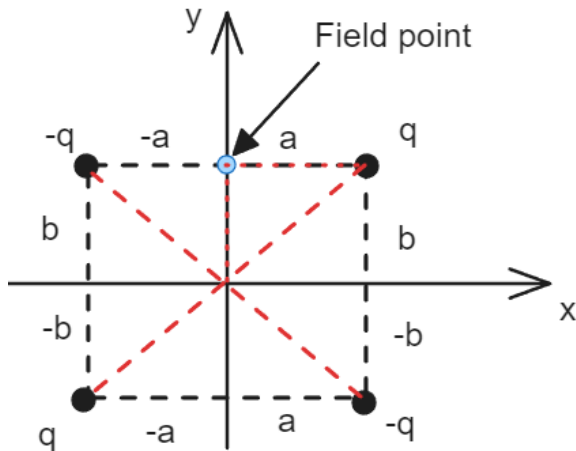


3. Method of images I *(hand in question)

Solve the problem stated in Griffiths Edition 4 3.11. The same problem in Griffiths Edition 5 is 3.13.

We replace the grounded plates with a negative point charge mirroring over first the plate on y-axis making a negative charge at equal distance from the y-axis.

We do the same for the x-axis grounded plate. To compensate for the extra negative charge we introduce a positive charge diagonal of the starting charge.



This way we get **2 negative** (-a,b & a,-b) charges and **2 positive** (a,b & -a,-b)

As we work in 2D symatri $z = 0$

The potential in the area is now given by

Electric potential due to a point charge

$$V = \frac{1}{4\pi\epsilon_0} \frac{q}{r} \quad (23.14)$$

Electric constant Value of point charge Distance from point charge to where potential is measured

$$\vec{r}_{sep} = (\vec{r}_{field} - \vec{r}'_{source})$$

$$|r_{sep}| = \sqrt{(x-a)^2 + (y-b)^2}$$

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \left(\frac{q}{\sqrt{(x-a)^2 + (y-b)^2}} + \frac{q}{\sqrt{(x+a)^2 + (y+b)^2}} - \frac{q}{\sqrt{(x+a)^2 + (y-b)^2}} - \frac{q}{\sqrt{(x-a)^2 + (y+b)^2}} \right)$$

where $(x, y) \neq (a, b)$

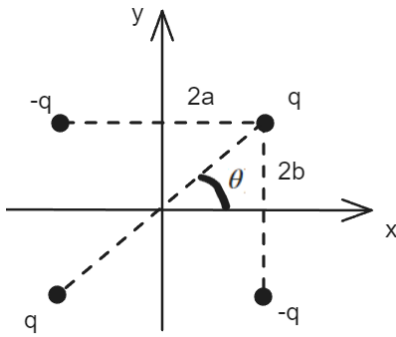
The force is now found with coulombs law know we have 3 point chagres acting on our source charge.

Coulomb's law: Magnitude of electric force between two point charges

$$F = \frac{1}{4\pi\epsilon_0} \frac{|q_1 q_2|}{r^2} \quad (21.2)$$

Electric constant Values of the two charges Distance between the two charges

By using superposition we sum up the force acting in each component.



$$F = \frac{1}{4\pi \epsilon_0} \left(\frac{q^2 \cdot \cos(\theta)}{\sqrt{(2a)^2 + (2b)^2}} \hat{x} - \frac{q^2}{(2a)^2} \hat{x} + \frac{q^2 \cdot \sin(\theta)}{\sqrt{(2a)^2 + (2b)^2}} \hat{y} - \frac{q^2}{(2b)^2} \hat{y} \right)$$

$$F = \frac{q^2}{4\pi \epsilon_0} \left[\left(\frac{\cos(\theta)}{\sqrt{(2a)^2 + (2b)^2}} - \frac{1}{(2a)^2} \right) \hat{x} + \left(\frac{\sin(\theta)}{\sqrt{(2a)^2 + (2b)^2}} - \frac{1}{(2b)^2} \right) \hat{y} \right]$$

We find the work to bring the charge from infinity to the current position using the work energy theorem

$$W = Q \left(V(\vec{r}_{a,b}) - V(\vec{r}_{\infty}) \right)$$

at $\infty V \rightarrow 0$

$$V(\vec{r}_{\infty}) = 0$$

$$W_{\text{tot}} = \frac{1}{8\pi \epsilon_0} \sum_{i \neq j} \frac{q_i q_j}{r_{\text{script},ij}}$$

$$W_{\text{tot}} = \frac{q^2}{8\pi \epsilon_0} \left(\frac{1}{\sqrt{(2a)^2 + (2b)^2}} - \frac{1}{2a} - \frac{1}{2b} - \frac{1}{2a} - \frac{1}{2b} + \frac{1}{\sqrt{(2a)^2 + (2b)^2}} \right)$$

$$W_{\text{tot}} = \frac{q^2}{8\pi \epsilon_0} \left(\frac{2}{\sqrt{(2a)^2 + (2b)^2}} - \frac{1}{a} - \frac{1}{b} \right)$$

Here i have used the interaction between the mirrored charges as well i am not use if this is correct.

The image method only works if we can place a mirror charge such that we are not forced to put an other charge in the area of our source charge.