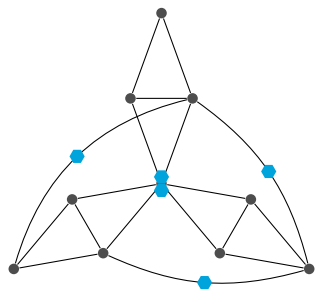
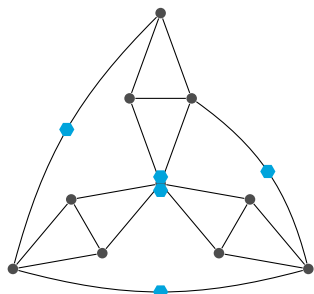


In this document, we list all simple graphs with at most 10 vertices for which the corresponding metric graph has lower gonality. The small blue hexagons represent a divisor with rank at least 1 and minimal degree on the 2-subdivision of the depicted graph. The graphs G in Figures 8, 21, and 29 satisfy $\text{dgon}(\Gamma(G)) = 6$ and $\text{dgon}(G) = 7$, and all other graphs G satisfy $\text{dgon}(\Gamma(G)) = 5$ and $\text{dgon}(G) = 6$. These counterexamples were found by checking all simple graphs on at most 10 vertices. For this we used the program **geng** from the **gtools** suite packaged with **nauty** to generate all graphs. The captions correspond to the **graph6** encodings of the graphs, as generated by **geng**.

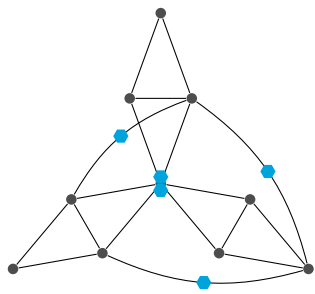
Graph 1: IC0ceRc~?



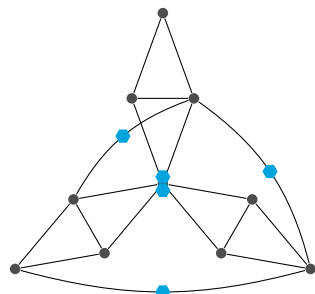
Graph 2: IC0ceRc^_



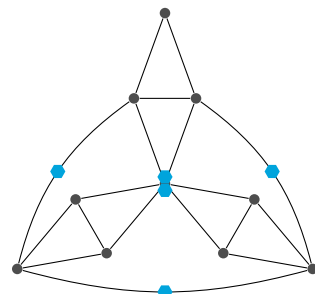
Graph 3: IC0ceRc|0



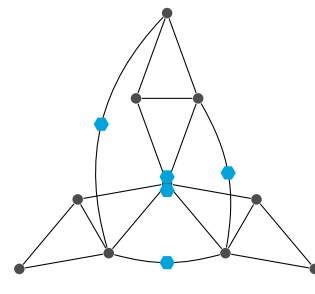
Graph 4: IC0ceRcn0



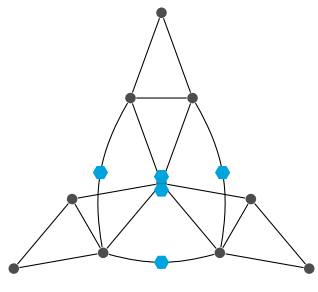
Graph 5: IC0ceRc\o



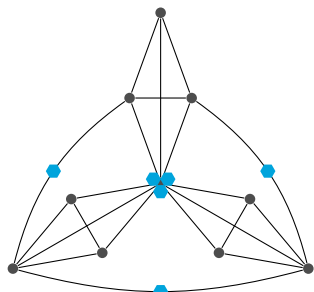
Graph 6: IC0ceRc}G



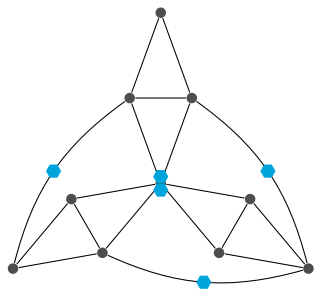
Graph 7: IC0ceRc{W



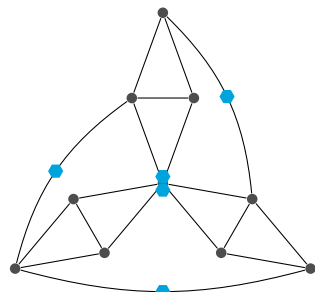
Graph 8: IC0ceRc~w



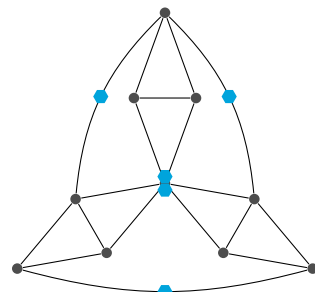
Graph 9: IC0cePs~?



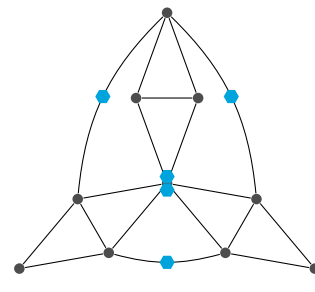
Graph 10: IC0cePsz_



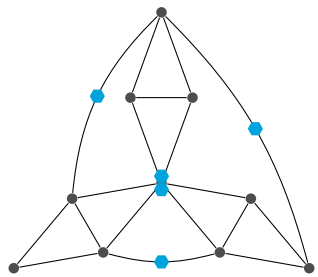
Graph 11: IC0cePs^_



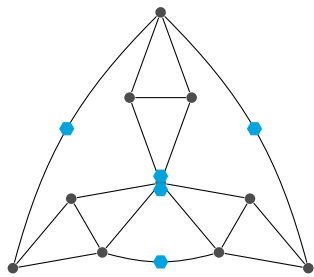
Graph 12: IC0cePs|0



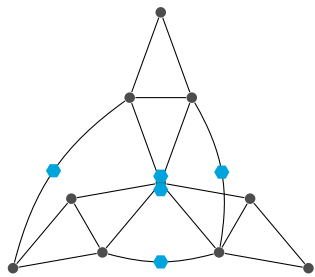
Graph 13: IC0cePsn0



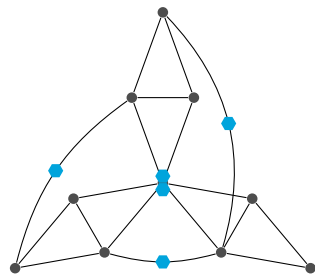
Graph 14: IC0cePsj0



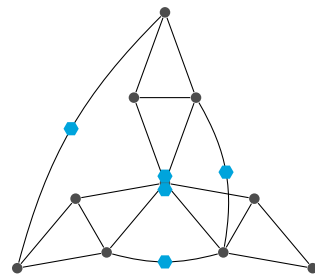
Graph 15: IC0cePs}G



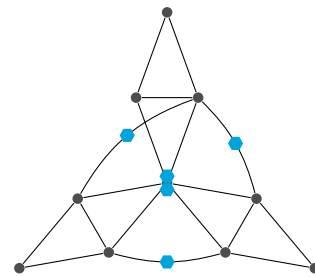
Graph 16: IC0cePsyg



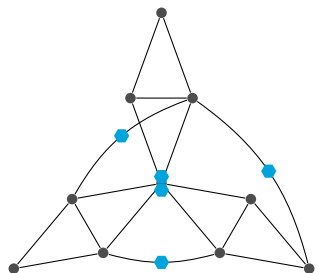
Graph 17: IC0cePs]g



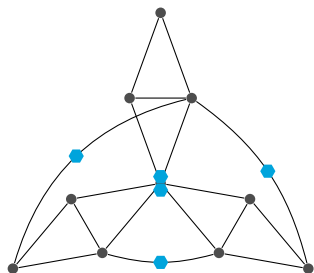
Graph 18: IC0cePs{W



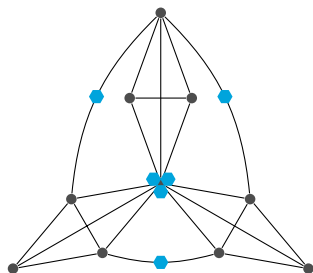
Graph 19: IC0cePsmW



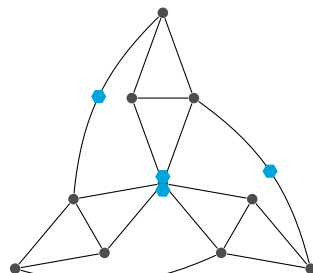
Graph 20: IC0cePsiw



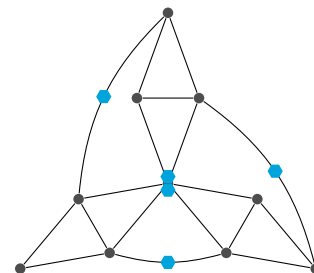
Graph 21: IC0cePs~w



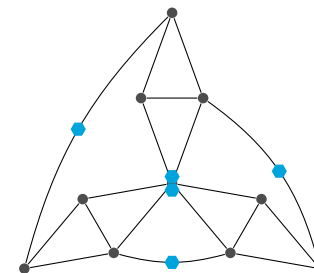
Graph 22: IC0edHg~?



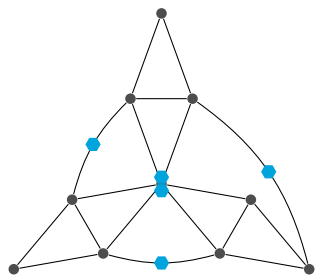
Graph 23: IC0edHg~_



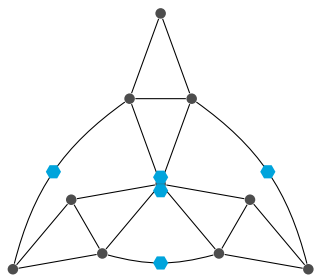
Graph 24: IC0edHg^_



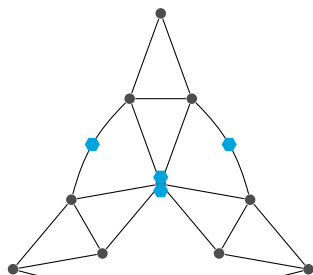
Graph 25: IC0edHgyo



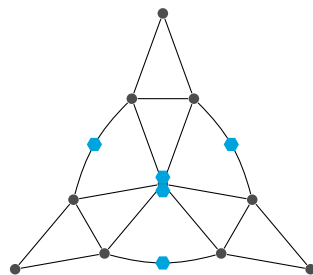
Graph 26: IC0edHg]o



Graph 27: IC0edHgro



Graph 28: IC0edHgww



Graph 29: IC0edHg~w

