

vectors

A 1 1 0 0
B 0 0 0 1
C 1 0 0 0
D 0 0 1 1

Learning Rate α

$$\begin{aligned}\alpha(0) &= 0.6 \\ \alpha(t+1) &= 0.5 \times \alpha(t) \text{ (or)} \\ \alpha(t) &= 0.5 \times \alpha(t-1)\end{aligned}$$

unit (aka neuron) weights: (randomly init)

unit1 0.2 0.6 0.5 0.9
unit2 0.8 0.4 0.7 0.3

Learning Rate α

$$\begin{aligned}\text{at } t = 0: \\ \alpha(0) &= 0.6 \\ \text{at } t = 1: \\ \alpha(1) &= 0.5 \times \alpha(t-1) \\ \alpha(1) &= 0.5 \times \alpha(1-1) \\ \alpha(1) &= 0.5 \times \alpha(0) \\ \alpha(1) &= 0.5 \times 0.6 \\ \alpha(1) &= 0.3\end{aligned}$$

Vector A	1	1	0	0
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Calculating vector A BMU

unit1	0.2	0.6	0.5	0.9
unit2	0.8	0.4	0.7	0.3

D(1) = euclidean distance to unit 1

$$D(1) = (0.2 - 1)^2 + (0.6 - 1)^2 + (0.5 - 0)^2 + (0.9 - 0)^2$$

$$D(1) = 1.86$$

D(2) = euclidean distance to unit 2

$$D(2) = (0.8 - 1)^2 + (0.4 - 1)^2 + (0.7 - 0)^2 + (0.3 - 0)^2$$

$$D(2) = 0.98$$

D(2) < D(1) : Unit 2 is winning unit (BMU = Best Matching Unit)

Vector A	1	1	0	0
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Updating weight of unit 2 (t=0)

unit2	0.8	0.4	0.7	0.3
Learning Rate $\alpha(0)$	=	0.6		

$$\begin{aligned}
 w_{i2}(\text{new}) &= w_{i2}(\text{old}) + \alpha[x_i - w_{i2}(\text{old})] \\
 &= w_{i2}(\text{old}) + 0.6[x_i - w_{i2}(\text{old})] \\
 &= w_{i2}(\text{old}) + 0.6[x_i] - 0.6[w_{i2}(\text{old})] \\
 &= [w_{i2}(\text{old}) - 0.6[w_{i2}(\text{old})]] + 0.6[x_i] \\
 &= [0.4w_{i2}(\text{old})] + 0.6[x_i]
 \end{aligned}$$

Vector A	1	1	0	0
unit2	0.8	0.4	0.7	0.3
Learning Rate $\alpha(0)$	= 0.6			

Updating weight of unit 2 (t=0)

$$\begin{aligned}
 w_{i2}(\text{new}) &= 0.4w_{i2}(\text{old}) + 0.6x_i \\
 &= 0.4(0.8) + 0.6(1) \\
 &\quad 0.4(0.4) + 0.6(1) \\
 &\quad 0.4(0.7) + 0.6(0) \\
 &\quad 0.4(0.3) + 0.6(0)
 \end{aligned}$$

unit2(updated weights):

$$= 0.92 \quad 0.76 \quad 0.28 \quad 0.12$$