

vectors

A 1 1 0 0
B 0 0 0 1
C 1 0 0 0
D 0 0 1 1

Learning Rate α

$\alpha(0) = 0.6$
 $\alpha(t+1) = 0.5 \times \alpha(t)$ (or)
 $\alpha(t) = 0.5 \times \alpha(t-1)$

unit (aka neuron) weights: (randomly init)

unit1 0.2 0.6 0.5 0.9
unit2 0.8 0.4 0.7 0.3

Learning Rate α

at $t = 0$:
 $\alpha(0) = 0.6$

at $t = 1$:
 $\alpha(1) = 0.5 \times \alpha(t-1)$
 $\alpha(1) = 0.5 \times \alpha(1-1)$
 $\alpha(1) = 0.5 \times \alpha(0)$
 $\alpha(1) = 0.5 \times 0.6$
 $\alpha(1) = 0.3$

Calculating vector A BMU

Vector A 1 1 0 0

unit1 0.2 0.6 0.5 0.9

unit2 0.8 0.4 0.7 0.3

$D(1)$ = euclidean distance to unit 1

$$D(1) = (0.2 - 1)^2 + (0.6 - 1)^2 + (0.5 - 0)^2 + (0.9 - 0)^2$$

$$D(1) = 1.86$$

$D(2)$ = euclidean distance to unit 2

$$D(2) = (0.8 - 1)^2 + (0.4 - 1)^2 + (0.7 - 0)^2 + (0.3 - 0)^2$$

$$D(2) = 0.98$$

$D(2) < D(1)$: Unit 2 is winning unit (BMU = Best Matching Unit)

Vector A 1 1 0 0

Updating weight of unit 2 (t=0)

unit2 0.8 0.4 0.7 0.3

Learning Rate $\alpha(0) = 0.6$

$$\begin{aligned}w_{i2}(\text{new}) &= w_{i2}(\text{old}) + \alpha[x_i - w_{i2}(\text{old})] \\&= w_{i2}(\text{old}) + 0.6[x_i - w_{i2}(\text{old})] \\&= w_{i2}(\text{old}) + 0.6[x_i] - 0.6[w_{i2}(\text{old})] \\&= [w_{i2}(\text{old}) - 0.6[w_{i2}(\text{old})]] + 0.6[x_i] \\&= [0.4w_{i2}(\text{old})] + 0.6[x_i]\end{aligned}$$

Updating weight of unit 2 (t=0)

Vector A 1 1 0 0

unit2 0.8 0.4 0.7 0.3

Learning Rate $\alpha(0)$ = 0.6

$$w_{i2}(\text{new}) = 0.4w_{i2}(\text{old}) + 0.6x_i$$

$$= 0.4(0.8) + 0.6(1)$$

$$0.4(0.4) + 0.6(1)$$

$$0.4(0.7) + 0.6(0)$$

$$0.4(0.3) + 0.6(0)$$

unit2(updated weights):

$$= 0.92 \quad 0.76 \quad 0.28 \quad 0.12$$