

# Schmidt decomposition = SVD in quantum mechanics context

state in the joint system  $A+B$

$$|\psi\rangle = |\varphi\rangle_A |\phi\rangle_B A^{\alpha\beta} \xrightarrow{\text{Schmidt decomposition}} |u_i\rangle |v_i\rangle \lambda_i$$

↑ subsystem A    ↑ B    ↑ "dummy"

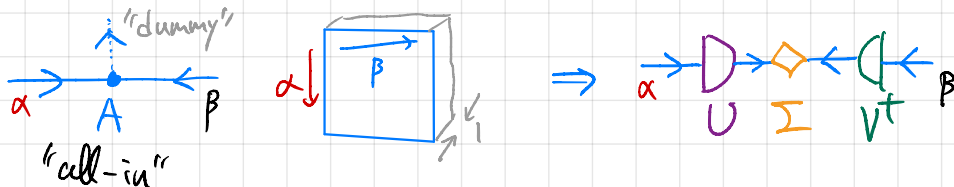
SVD:  $A = U \Sigma V^T$

$$U = [\vec{u}_1 \vec{u}_2 \dots] \quad V = [\vec{v}_1 \vec{v}_2 \dots]$$

$$\Sigma_{ij} = \lambda_i \delta_{ij}$$

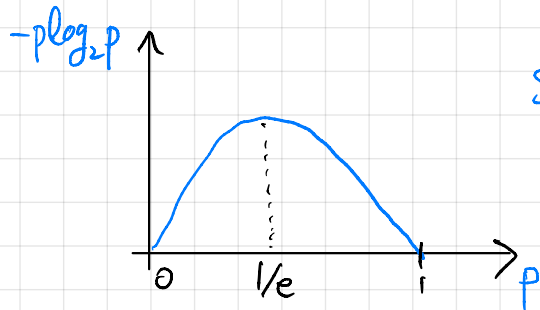
Normalization:  $\langle \psi | \psi \rangle = 1 \Rightarrow \sum_i |\lambda_i|^2 = 1$

In TN diagram:



Entanglement entropy:  $S(\{\lambda_i\}) = - \sum_i |\lambda_i|^2 \log_2 |\lambda_i|^2$

to use the unit of 'ebit's



$S(\{\lambda_i\})$  is maximal when  $|\lambda_i|^2 = 1/d$  for all  $i$ 's, where  $d = \min(d_\alpha, d_\beta)$  ( $\because -p \log_2 p$  is concave)