

Area law of entanglement

Tensor networks as efficient representation of many-body states:

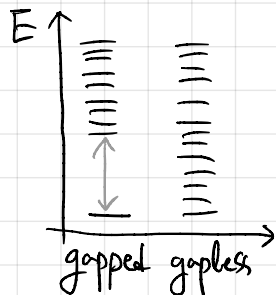
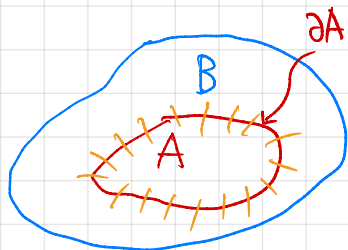


$$\# \text{ of elements} = d^N$$



$$\gg \# \text{ of elements} = O(ND^2d)$$

How can we use finite bond dimensions?: area law

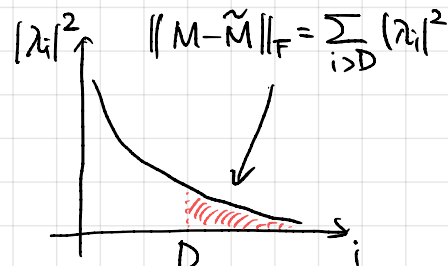


Entanglement entropy between A & B
 \propto area of ∂A

- 1D gapped: $\sim \text{const.}$
- 1D gapless: $\sim \text{const} + \log L$
- 2D gapped: $\sim L$
- 3D gapped: $\sim L^2$

$$\tilde{M} = \sum_{i=1}^D \vec{u}_i \lambda_i \vec{v}_i^t$$

truncation error =
discarded weight:



$$\|M - \tilde{M}\|_F = \sum_{i>D} |\lambda_i|^2$$

$$\text{bond entanglement} \leq \log_2 D$$

