

COMP7990 Principles and Practices of Data Analytics

Exercise on Classification

Given the following dataset where $x = \{x_0, x_1, x_2\}$ is the input vector and y is the true label:

x_0	x_1	x_2	y
1	1	-1	1
1	1	1	1
1	-1	1	1
1	-1	-1	-1

The initial values of the weight vector \mathbf{w} are set to be $[-1, -1, -1]^T$.

- 1) Run through the perceptron algorithm by filling in the following table until the weight vector \mathbf{w} converges.

Iteration #	\mathbf{w} (old)	\mathbf{x}	y	$y(\mathbf{w}^T \mathbf{x})$	Update (Y/N)	$y\mathbf{x}$	\mathbf{w} (new)
1	$[-1, -1, -1]$	$[1, 1, -1]$	1	-1	Y	$[1, 1, -1]$	$[0, 0, -2]$
2	$[0, 0, -2]$...					
3							
4							
5							

- 2) Write down the equation of the decision boundary.
- 3) Plot the decision boundary of the perceptron.
- 4) Assume that the initial values of the weight vector \mathbf{w} are $[0.3, 0.5, 0.5]$. Repeat 1-3.

Iteration #	\mathbf{w} (old)	\mathbf{x}	y	$y(\mathbf{w}^T \mathbf{x})$	Update (Y/N)	$y\mathbf{x}$	\mathbf{w} (new)
1							
2							
3							
4							
5							

- 5) Compare the two decision boundaries obtained and discuss which is better.