

MAS162 DISCRETE MATHEMATICS AND LOGIC Semester 2 2024

Test 1

Test conditions:

- You can use one A4 hand-written page of notes (one-sided) during the test, and any hand-held scientific or graphics calculator.
- Closed book: you may not access the internet or any materials other than your one-sided page of notes during the test.
- You may not communicate with anyone about the contents of the test until after you have submitted your answers.

Declaration: I have written and will submit my own answers to this test under the above conditions.

Name:	Student Number:
Signature:	

1. [7 marks] (a) State whether the sequence (t_n) defined recursively by

$$t_1 = 1, t_n = 2t_{n-1}, n \ge 2$$

is an arithmetic or a geometric sequence, and then write down a direct formula for the n-th term. Use your formula to find t_6 .

(b) Find a recursive definition of the sequence with direct formula:

$$t_n = \frac{2^n}{n!}, \quad n \ge 1.$$

2. [8 marks] A tower is to be built out of square shaped blocks according to the following scheme: the top layer consists of 1 block, the second layer consists of 3 blocks in an L-shape, and each subsequent layer below is also L-shaped, with the side length increasing by one block-width each layer. The top 4 layers of such a tower are pictured below.



(a) Write b_n for the number of blocks used in the *n*th layer counting down from the top, so that $b_1 = 1$, $b_2 = 3$ and so on. Find a recursive formula for b_n .

(b) Find a direct formula for b_n .

(c) Write T_n for the <u>total</u> number of blocks in such a tower with n layers, and find a recursive definition for T_n .

(d) The following MATLAB code is supposed to display the first 10 terms of the sequence T_n but it contains some errors.

i. What would the above code output?

ii. How would you change the code to produce the correct output?

SPACE FOR EXTRA WORKING