

Step 1)

Input Matrix:

A = [12, 1, 5, 3, 16], // Stock 1
[4, 4, 13, 4, 9], // Stock 2
[6, 8, 6, 1, 2], // Stock 3
[14, 3, 4, 8, 10] // Stock 4

Step 2)

STOCK 1:

| BUY DAY | SELL DAY | PROFIT |
|---------|----------|--------|
| 1 | 2 | -11 |
| 1 | 3 | -7 |
| 1 | 4 | -9 |
| 1 | 5 | 4 |
| 2 | 3 | 4 |
| 2 | 4 | 2 |
| 2 | 5 | 15 |
| 3 | 4 | -2 |
| 3 | 5 | 11 |
| 4 | 5 | 13 |

STOCK 2:

| BUY DAY | SELL DAY | PROFIT |
|---------|----------|--------|
| 1 | 2 | 0 |
| 1 | 3 | 9 |
| 1 | 4 | 0 |
| 1 | 5 | 5 |
| 2 | 3 | 9 |
| 2 | 4 | 0 |
| 2 | 5 | 5 |
| 3 | 4 | -9 |
| 3 | 5 | -4 |
| 4 | 5 | 5 |

STOCK 3:

| BUY DAY | SELL DAY | PROFIT |
|---------|----------|--------|
| 1 | 2 | 2 |
| 1 | 3 | 0 |
| 1 | 4 | -5 |
| 1 | 5 | -4 |
| 2 | 3 | -2 |
| 2 | 4 | -7 |
| 2 | 5 | -6 |
| 3 | 4 | -5 |
| 3 | 5 | -4 |
| 4 | 5 | 1 |

STOCK 4:

| BUY DAY | SELL DAY | PROFIT |
|---------|----------|--------|
| 1 | 2 | -11 |
| 1 | 3 | 10 |
| 1 | 4 | -6 |
| 1 | 5 | -4 |
| 2 | 3 | 1 |
| 2 | 4 | 5 |
| 2 | 5 | 7 |
| 3 | 4 | 4 |
| 3 | 5 | 6 |
| 4 | 5 | 2 |

Step 3)

Stock 1 most profitable transaction:

Buy at day 2 for 1 and sell at day 5 for 16. Profit = 15

Stock 2 most profitable transaction:

Buy at day 1 for 4 and sell at day 3 for 13. Profit = 9

Stock 3 most profitable transaction:

Buy at day 1 for 6 and sell at day 2 for 8. Profit = 2

Stock 4 most profitable transaction:

Buy at day 2 for 3 and sell at day 5 for 10. Profit = 7

Step 4)

Maximum profit is 15 from Stock 1 – Buy day 2 and sell day 5

OUTPUT: (1, 2, 5, 15)

Problem Statement 2

You are given a matrix A of dimensions $m \times n$, where each element represents the predicted prices of m different stocks for n consecutive days. Additionally, you are given an integer k ($1 \leq k \leq n$). Your task is to manually find a sequence of at most k transactions, each involving the purchase and sale of a single stock, that yields the maximum profit.

Step 1)

Input Matrix:

```
A = [[25, 30, 15, 40, 50], // Stock 1
      [10, 20, 30, 25, 5],  // Stock 2
      [30, 45, 35, 10, 15], // Stock 3
      [ 5, 50, 35, 25, 45]] // Stock 4
```

Step 2)

STOCK 1:

| BUY DAY | SELL DAY | PROFIT |
|---------|----------|--------|
|---------|----------|--------|

| | | |
|---|---|---|
| 1 | 2 | 5 |
|---|---|---|

| | | |
|---|---|-----|
| 1 | 3 | -10 |
|---|---|-----|

| | | |
|---|---|----|
| 1 | 4 | 15 |
|---|---|----|

| | | |
|---|---|----|
| 1 | 5 | 25 |
|---|---|----|

| | | |
|---|---|-----|
| 2 | 3 | -15 |
|---|---|-----|

| | | |
|---|---|----|
| 2 | 4 | 10 |
| 2 | 5 | 20 |
| 3 | 4 | 25 |
| 3 | 5 | 35 |
| 4 | 5 | 10 |

STOCK 2:

| BUY DAY | SELL DAY | PROFIT |
|---------|----------|--------|
| 1 | 2 | 10 |
| 1 | 3 | 20 |
| 1 | 4 | 15 |
| 1 | 5 | -5 |
| 2 | 3 | 10 |
| 2 | 4 | 5 |
| 2 | 5 | -15 |
| 3 | 4 | -5 |
| 3 | 5 | -25 |
| 4 | 5 | -20 |

STOCK 3:

| BUY DAY | SELL DAY | PROFIT |
|---------|----------|--------|
|---------|----------|--------|

| | | |
|---|---|----|
| 1 | 2 | 15 |
|---|---|----|

| | | |
|---|---|---|
| 1 | 3 | 5 |
|---|---|---|

| | | |
|---|---|-----|
| 1 | 4 | -20 |
|---|---|-----|

| | | |
|---|---|-----|
| 1 | 5 | -15 |
|---|---|-----|

| | | |
|---|---|-----|
| 2 | 3 | -10 |
|---|---|-----|

| | | |
|---|---|-----|
| 2 | 4 | -35 |
|---|---|-----|

| | | |
|---|---|-----|
| 2 | 5 | -30 |
|---|---|-----|

| | | |
|---|---|-----|
| 3 | 4 | -25 |
|---|---|-----|

| | | |
|---|---|-----|
| 3 | 5 | -20 |
|---|---|-----|

| | | |
|---|---|---|
| 4 | 5 | 5 |
|---|---|---|

STOCK 4:

| BUY DAY | SELL DAY | PROFIT |
|---------|----------|--------|
|---------|----------|--------|

| | | |
|---|---|----|
| 1 | 2 | 45 |
|---|---|----|

| | | |
|---|---|----|
| 1 | 3 | 30 |
|---|---|----|

| | | |
|---|---|----|
| 1 | 4 | 20 |
|---|---|----|

| | | |
|---|---|----|
| 1 | 5 | 40 |
|---|---|----|

| | | |
|---|---|-----|
| 2 | 3 | -15 |
|---|---|-----|

| | | |
|---|---|-----|
| 2 | 4 | -25 |
| 2 | 5 | -5 |
| 3 | 4 | -10 |
| 3 | 5 | 10 |
| 4 | 5 | 20 |

Step 3)

Finding optimal non-overlapping transactions (k=3):

Best profitable transactions:

1. Stock 4: (1,2) → Profit = 45
2. Stock 1: (3,5) → Profit = 35
3. Stock 4: (1,5) → Profit = 40
4. Stock 1: (1,5) → Profit = 25
5. Stock 1: (3,4) → Profit = 25

Selected non-overlapping transactions:

- Transaction 1: Stock 4, Buy Day 1, Sell Day 2 → Profit = 45
- Transaction 2: Stock 1, Buy Day 3, Sell Day 5 → Profit = 35

Total Maximum Profit = 80

Output: [(4,1,2), (1,3,5)]

Problem 3

Problem Statement

You are given a matrix A of dimensions $m \times n$, where each element represents the predicted prices of m different stocks for n consecutive days. Additionally, you are given an integer c ($1 \leq c \leq n - 2$). Your task is to determine the maximum profit achievable under the given trading restrictions, where you cannot buy any stock for c days after selling any stock. If you sell a stock on day i , you are not allowed to buy any stock until day $i + c + 1$.

Input

| | Day 1 | Day 2 | Day 3 | Day 4 | Day 5 | Day 6 | Day 7 |
|---------|-------|-------|-------|-------|-------|-------|-------|
| Stock 1 | 7 | 1 | 5 | 3 | 6 | 8 | 9 |
| Stock 2 | 2 | 4 | 3 | 7 | 9 | 1 | 8 |
| Stock 3 | 5 | 8 | 9 | 1 | 2 | 3 | 10 |
| Stock 4 | 9 | 3 | 4 | 8 | 7 | 4 | 1 |
| Stock 5 | 3 | 1 | 5 | 8 | 9 | 6 | 4 |

Cooldown: $c = 2$

First let's define $\text{best}(t)$ as the maximum profit achievable with one buy, sell between days t and 7.

| t | Window | Best trade | $\text{best}_t(t)$ |
|------------|---------------|--|--------------------------------------|
| 1–4 | Days 1 to 7 | buy Stock 3 on day 4 at 1 then sell on day 7 at 10 | 9 |
| 5 | Days 5 to 7 | buy Stock 3 on day 5 at 2 then sell on day 7 at 10 | 8 |
| 6 | Days 6 to 7 | buy Stock 2 on day 6 at 1 then sell on day 7 at 8 | 7 |
| 7 | day 7 | no transaction | 0 |

Now for each possible first trade (i, j, l) , let's compute $\text{Profit}_1 = P[i, l] - P[i, j]$, earliest next buy $B = l + 3$, $\text{Profit}_2 = \text{best}_1(B)$, and $\text{Total} = \text{Profit}_1 + \text{Profit}_2$. Here are the top contenders:

| Buy j | First trade (i, l) | Profit_1 | Next $B=l+3$ | Profit_2 | Total |
|--------------|-------------------------------|-------------------------------------|--------------------------------|-------------------------------------|--------------|
| j = 1 | Stock 2: buy | 7 | 8 to 0 | 0 | 7 |

| | | | | | |
|--------------|---------------------------|---|---------|---|----|
| | 1, sell 5 | | | | |
| j = 2 | Stock 1: buy 2, sell 3 | 4 | 6 to 7 | 7 | 11 |
| j = 3 | Stock 2: buy 3, sell 5 | 6 | 8 to 0 | 0 | 6 |
| j = 4 | Stock 3: buy 4, sell 7 | 9 | 10 to 0 | 0 | 9 |
| j = 5 | Stock 3: buy 5, sell 7 | 8 | 10 to 0 | 0 | 8 |
| j = 6 | Stock 2: buy 6, sell 7 | 7 | 10 to 0 | 0 | 7 |

The best total (11) come from:

1. Stock 1: buy on day 2 at 1 then sell on day 3 at 5 ($\text{Profit}_1 = 4$) with the cooldown until day 6 ($3 + 2 + 1$)
2. Stock 2: buy on day 6 at 1 then sell on day 7 at 8 ($\text{Profit}_2 = 7$)

Total profit = $4 + 7 = 11$.

Final Answer

Maximum profit: 11

Trades: ($i = 1, j = 2, l = 3$) and ($i = 2, j = 6, l = 7$)