Objetivos a cubrir

Series numéricas. Criterios de convergencia y divergencia de una seria numérica.

Ejercicios propuestos

Código: MAT4-CDI.5

Aplique un criterio apropiado para determinar si la serie indicada converge ó diverge. En algunos casos puede aplicarse más de un criterio.

1.
$$\sum_{k=1}^{\infty} \frac{1}{k^{1.1}}$$

$$2. \qquad \sum_{n=1}^{\infty} \frac{1}{n^{0.99}}$$

$$3. \qquad \sum_{n=1}^{\infty} \frac{1}{2n+7}$$

$$4. \qquad \sum_{k=1}^{\infty} \frac{1}{10 + \sqrt{k}}$$

1.
$$\sum_{k=1}^{\infty} \frac{1}{k^{1.1}}$$
 2. $\sum_{n=1}^{\infty} \frac{1}{n^{0.99}}$ 3. $\sum_{n=1}^{\infty} \frac{1}{2n+7}$ 4. $\sum_{k=1}^{\infty} \frac{1}{10+\sqrt{k}}$ 5. $\sum_{n=2}^{\infty} \frac{1}{n\sqrt{n^2-1}}$

$$6. \qquad \sum_{n=1}^{\infty} \frac{1}{n^n}$$

7.
$$\sum_{n=1}^{\infty} (-1)^n$$

$$8. \qquad \sum_{k=1}^{\infty} \frac{k}{k^2 + k^2}$$

9.
$$\sum_{n=1}^{\infty} \frac{1}{n + \sqrt{n}}$$

6.
$$\sum_{n=1}^{\infty} \frac{1}{n^n}$$
 7.
$$\sum_{n=1}^{\infty} (-1)^n$$
 8.
$$\sum_{k=1}^{\infty} \frac{k}{k^2 + 5}$$
 9.
$$\sum_{n=1}^{\infty} \frac{1}{n + \sqrt{n}}$$
 10.
$$\sum_{k=1}^{\infty} \frac{2 + \sin k}{\sqrt[3]{k^4 + 1}}$$

$$11. \quad \sum_{n=1}^{\infty} \frac{1}{n!}$$

12.
$$\sum_{n=2}^{\infty} \frac{\ln n}{n^5}$$

$$13. \quad \sum_{n=1}^{\infty} \frac{\sqrt{n}}{n^2 + 1}$$

14.
$$\sum_{n=1}^{\infty} \frac{n^2}{n^2 + 16}$$

11.
$$\sum_{n=1}^{\infty} \frac{1}{n!}$$
 12. $\sum_{n=2}^{\infty} \frac{\ln n}{n^5}$ 13. $\sum_{n=1}^{\infty} \frac{\sqrt{n}}{n^2 + 1}$ 14. $\sum_{n=1}^{\infty} \frac{n^2}{n^2 + 16}$ 15. $\sum_{n=1}^{\infty} \frac{1 - \cos n}{n^2}$

$$16. \quad \sum_{k=1}^{\infty} \frac{2^k}{k!}$$

$$17. \quad \sum_{k=2}^{\infty} \frac{1}{\ln k}$$

18.
$$\sum_{i=1}^{\infty} \frac{ie^{-i}}{i+1}$$

19.
$$\sum_{k=1}^{\infty} k \left(\frac{2}{3}\right)^k$$

16.
$$\sum_{k=1}^{\infty} \frac{2^k}{k!}$$
 17. $\sum_{k=2}^{\infty} \frac{1}{\ln k}$ 18. $\sum_{i=1}^{\infty} \frac{ie^{-i}}{i+1}$ 19. $\sum_{k=1}^{\infty} k \left(\frac{2}{3}\right)^k$ 20. $\sum_{k=1}^{\infty} \frac{3}{2 + \sin k}$

21.
$$\sum_{n=1}^{\infty} \frac{n^2}{2^n}$$

$$22. \quad \sum_{n=1}^{\infty} \frac{e^{1/r}}{n^2}$$

$$23. \quad \sum_{n=2}^{\infty} \frac{1}{(\ln n)^r}$$

24.
$$\sum_{n=1}^{\infty} \frac{2^n}{3^n + 1}$$

21.
$$\sum_{n=1}^{\infty} \frac{n^2}{2^n}$$
 22. $\sum_{n=1}^{\infty} \frac{e^{1/n}}{n^2}$ 23. $\sum_{n=1}^{\infty} \frac{1}{(\ln n)^n}$ 24. $\sum_{n=1}^{\infty} \frac{2^n}{3^n+1}$ 25. $\sum_{n=1}^{\infty} \frac{\sin(1/k)}{k}$

26.
$$\sum_{n=1}^{\infty} \frac{n^4 + 3n^2}{n^5}$$

$$27. \quad \sum_{n=2}^{\infty} \frac{1}{n \ln^2 n}$$

$$28. \quad \sum_{n=1}^{\infty} \frac{\sin^2 n}{2^n}$$

26.
$$\sum_{n=1}^{\infty} \frac{n^4 + 3n}{n^5}$$
 27.
$$\sum_{n=2}^{\infty} \frac{1}{n \ln^2 n}$$
 28.
$$\sum_{n=1}^{\infty} \frac{\sin^2 n}{2^n}$$
 29.
$$\sum_{k=1}^{\infty} \frac{1}{(k+1)(k+2)}$$

$$30. \quad \sum_{n=1}^{\infty} \frac{1}{1 + \ln n}$$

31.
$$\sum_{n=1}^{\infty} \frac{2^n}{(2n+1)}$$

32.
$$\sum_{n=1}^{\infty} \frac{n!}{1000^n}$$

30.
$$\sum_{n=1}^{\infty} \frac{1}{1 + \ln n}$$
 31.
$$\sum_{n=1}^{\infty} \frac{2^n}{(2n+1)!}$$
 32.
$$\sum_{n=1}^{\infty} \frac{n!}{1000^n}$$
 33.
$$\sum_{k=1}^{\infty} \frac{1}{\sqrt{(k+1)(k+2)}}$$

$$34. \quad \sum_{n=1}^{\infty} \frac{n^4 + 9n}{n^{11/2}}$$

$$35. \quad \sum_{n=2}^{\infty} \frac{\left(\ln n\right)^{-2}}{n}$$

$$36. \quad \sum_{k=1}^{\infty} \frac{k}{(4k+1)^{3/2}}$$

35.
$$\sum_{n=2}^{\infty} \frac{(\ln n)^{-2}}{n}$$
 36.
$$\sum_{k=1}^{\infty} \frac{k}{(4k+1)^{3/2}}$$
 37.
$$\sum_{k=1}^{\infty} \frac{\sqrt{k+1}}{\sqrt[3]{64k^9+40}}$$

$$38. \quad \sum_{m=1}^{\infty} \frac{m!}{(2m)!}$$

39.
$$\sum_{k=1}^{\infty} \frac{1+8^k}{3+10^k}$$

40.
$$\sum_{k=1}^{\infty} \frac{(1.1)^k}{4k}$$

38.
$$\sum_{m=1}^{\infty} \frac{m!}{(2m)!}$$
 39. $\sum_{k=1}^{\infty} \frac{1+8^k}{3+10^k}$ 40. $\sum_{k=1}^{\infty} \frac{(1.1)^k}{4k}$ 41. $\sum_{m=1}^{\infty} \frac{1}{\sqrt{n(n+1)(n+2)}}$

42.
$$\sum_{k=1}^{\infty} \frac{1}{k\sqrt{3^k + k}}$$

43.
$$\sum_{1}^{\infty} \frac{1+3^n}{2^n}$$

42.
$$\sum_{k=1}^{\infty} \frac{1}{k\sqrt{3^k + k}}$$
 43.
$$\sum_{n=1}^{\infty} \frac{1+3^n}{2^n}$$
 44.
$$\sum_{n=1}^{\infty} \frac{5n^2 + n - n^{-1}}{2n^3 + 2n^2 + 8}$$
 45.
$$\sum_{k=2}^{\infty} \frac{2k+1}{k\sqrt{k \ln k}}$$

$$45. \quad \sum_{k=2}^{\infty} \frac{2k+1}{k\sqrt{k\ln k}}$$

46.
$$\sum_{k=1}^{\infty} \frac{k + e^{-k}}{5^k (k+9)^{k}}$$

$$47. \quad \sum_{k=1}^{\infty} \frac{5^{2k+1}}{k^k}$$

48.
$$\sum_{1}^{\infty} \frac{1+1/n}{10^n}$$

46.
$$\sum_{k=1}^{\infty} \frac{k + e^{-k}}{5^k (k+9)}$$
 47.
$$\sum_{k=1}^{\infty} \frac{5^{2k+1}}{k^k}$$
 48.
$$\sum_{n=1}^{\infty} \frac{1 + 1/n}{10^n}$$
 49.
$$\sum_{n=1}^{\infty} \frac{5n^2 + 2n}{3n (n^2 + 1)}$$

$$50. \quad \sum_{j=1}^{\infty} \frac{j^{30}}{(1.1)^j}$$

51.
$$\sum_{i=1}^{\infty} \frac{1}{j^5 (0.99)^3}$$

52.
$$\sum_{n=1}^{\infty} \frac{(2n)!}{n! (2n)^n}$$

50.
$$\sum_{i=1}^{\infty} \frac{j^{30}}{(1.1)^{j}} \qquad 51. \quad \sum_{i=1}^{\infty} \frac{1}{j^{5} (0.99)^{j}} \qquad 52. \quad \sum_{n=1}^{\infty} \frac{(2n)!}{n! (2n)^{n}} \qquad 53. \quad \sum_{n=1}^{\infty} \operatorname{sen} \left(\frac{\pi}{n^{2} + 1}\right)$$

54.
$$\sum_{n=1}^{\infty} \left(1 - \cos \frac{\pi}{n} \right)$$

55.
$$\sum_{n=1}^{\infty} \frac{n^3 2^{n+3}}{7^{n-1}}$$

54.
$$\sum_{n=1}^{\infty} \left(1 - \cos\frac{\pi}{n}\right)$$
 55. $\sum_{n=1}^{\infty} \frac{n^3 2^{n+3}}{7^{n-1}}$ 56. $\sum_{n=1}^{\infty} \frac{n + \ln n}{n^3 + 2n - 1}$ 57. $\sum_{k=1}^{\infty} \left(\frac{k}{k+1}\right)^{k^2}$

57.
$$\sum_{k=1}^{\infty} \left(\frac{k}{k+1}\right)^{k^2}$$

$$58. \quad \sum_{n=2}^{\infty} \frac{1}{n \ln n}$$

$$59. \quad \sum_{n=2}^{\infty} \frac{1}{n \ln^3 n}$$

58.
$$\sum_{n=2}^{\infty} \frac{1}{n \ln n}$$
 59. $\sum_{n=2}^{\infty} \frac{1}{n \ln^3 n}$ 60. $\sum_{n=1}^{\infty} \arcsin\left(\frac{1}{\sqrt{n}}\right)$ 61. $\sum_{n=1}^{\infty} \frac{1}{\sqrt{n(n+1)}}$

$$61. \quad \sum_{n=1}^{\infty} \frac{1}{\sqrt{n(n+1)}}$$

62.
$$\sum_{n=1}^{\infty} \operatorname{sen}\left(\frac{1}{n^4}\right) \qquad 63. \quad \sum_{n=1}^{\infty} \frac{\left(-1\right)^n}{\sqrt{n\left(n+1\right)}} \qquad 64. \quad \sum_{n=1}^{\infty} \ln\left(1+\frac{1}{n}\right) \qquad 65. \quad \sum_{n=1}^{\infty} \frac{4^{n-1}}{n3^{n+2}} = 1$$

66.
$$\sum_{n=1}^{\infty} \frac{n^2 + n + 1}{n^4 + n + 1}$$
 67.
$$\sum_{n=2}^{\infty} \frac{n}{(n^2 - 1) \ln n}$$
 68.
$$\sum_{n=2}^{\infty} \frac{1}{(3n + 2) \ln^2 n}$$
 69.
$$\sum_{n=1}^{\infty} \frac{\ln n}{\sqrt[4]{n^5}}$$

70.
$$\sum_{n=1}^{\infty} \frac{n^4}{\ln^4 (n+1)}$$
 71.
$$\sum_{n=2}^{\infty} \frac{n}{2^{n^2} + n \ln^2 n}$$
 72.
$$\sum_{n=2}^{\infty} \frac{1}{n (\ln n) \ln (\ln n)}$$
 73.
$$\sum_{n=1}^{\infty} \frac{n^2}{n!}$$

74.
$$\sum_{n=1}^{\infty} \frac{1}{(2n-1)2^{2n-1}}$$
 75.
$$\sum_{n=1}^{\infty} \frac{1}{(2n+1)!}$$
 76.
$$\sum_{n=1}^{\infty} \frac{1}{(\ln(n+1))^n}$$
 77.
$$\sum_{n=1}^{\infty} \frac{n}{2n-1}$$

78.
$$\sum_{n=1}^{\infty} \operatorname{sen}\left(\frac{\pi}{2^n}\right)$$
 79. $\sum_{n=1}^{\infty} \frac{1+n}{1+n^2}$ 80. $\sum_{n=1}^{\infty} \frac{1}{(n+1)(n+4)}$ 81. $\sum_{n=1}^{\infty} \frac{n+1}{n(n+2)}$

82.
$$\sum_{n=1}^{\infty} \tan\left(\frac{\pi}{4^n}\right)$$
 83.
$$\sum_{n=1}^{\infty} \frac{1}{n^2 + 1}$$
 84.
$$\sum_{n=1}^{\infty} \left(\sqrt{n} - \sqrt{n-1}\right)$$
 85.
$$\sum_{n=1}^{\infty} \frac{1}{\ln(n+1)}$$

86.
$$\sum_{n=1}^{\infty} \frac{1}{n^2 - 4n + 5}$$
 87.
$$\sum_{n=1}^{\infty} \left(\frac{1 + n^2}{1 + n^3}\right)^2$$
 88.
$$\sum_{n=1}^{\infty} \frac{1}{\sqrt{n^2 + 2n}}$$
 89.
$$\sum_{n=1}^{\infty} \frac{1}{3n - 1}$$

90.
$$\sum_{n=1}^{\infty} \sqrt{\frac{1}{n^4 + 1}}$$
 91. $\sum_{n=1}^{\infty} \arctan^n \left(\frac{1}{n}\right)$ 92. $\sum_{n=1}^{\infty} n \tan \left(\frac{\pi}{2^{n+1}}\right)$ 93. $\sum_{n=1}^{\infty} \frac{(n+1)!}{2^n n!}$

94.
$$\sum_{n=1}^{\infty} n^2 \operatorname{sen}\left(\frac{\pi}{2^n}\right) \qquad 95. \quad \sum_{n=1}^{\infty} \frac{2 \cdot 5 \cdots (3n-1)}{1 \cdot 5 \cdots (4n-3)} \qquad 96. \quad \sum_{n=1}^{\infty} \frac{n^2}{3^n} \qquad 97. \quad \sum_{n=1}^{\infty} \frac{1}{(n+1)\sqrt{n+1}}$$

98.
$$\sum_{n=1}^{\infty} \frac{1}{n} \left(\sqrt{n+1} - \sqrt{n-1} \right)$$
 99.
$$\sum_{n=1}^{\infty} \operatorname{sen} \left(\frac{\pi}{2n} \right)$$
 100.
$$\sum_{n=1}^{\infty} \frac{n}{(n+1)!}$$
 101.
$$\sum_{n=1}^{\infty} \frac{2^n}{n^4}$$

102.
$$\sum_{n=1}^{\infty} \frac{1}{3^n} \left(\frac{n+1}{n} \right)^{n^2}$$
 103.
$$\sum_{n=1}^{\infty} \frac{1}{\sqrt{n}} \tan \left(\frac{n+1}{n-1} \right)$$
 104.
$$\sum_{n=1}^{\infty} \frac{1}{(n+1) (\ln (n+1))^2}$$

105.
$$\sum_{n=1}^{\infty} \left(\frac{n}{2n+1}\right)^n$$
 106. $\sum_{n=1}^{\infty} \arcsin\left(\frac{1}{n}\right)$ 107. $\sum_{n=1}^{\infty} \left(\frac{1+n}{1+n^2}\right)^2$ 108. $\sum_{n=1}^{\infty} \frac{n}{2^n}$

109.
$$\sum_{n=1}^{\infty} \frac{1}{n} \left(\sqrt{n^2 + n + 1} - \sqrt{n^2 - n + 1} \right)$$
 110.
$$\sum_{n=1}^{\infty} \frac{n^2 + 1}{n^3}$$
 111.
$$\sum_{n=1}^{\infty} \frac{1 \cdot 3 \cdots (2n-1)}{3^n n!}$$

112.
$$\sum_{n=1}^{\infty} \sqrt{\frac{n+1}{n}}$$
 113. $\sum_{n=1}^{\infty} \frac{n}{1000n+1}$ 114. $\sum_{n=1}^{\infty} \frac{n}{1+n^2}$ 115. $\sum_{n=1}^{\infty} \frac{1}{(5n-4)(4n-1)}$

116.
$$\sum_{n=1}^{\infty} \frac{2n-1}{3n}$$
 117.
$$\sum_{n=1}^{\infty} \frac{3^n}{n2^n}$$
 118.
$$\sum_{n=1}^{\infty} \frac{n!}{n^n}$$
 119.
$$\sum_{n=1}^{\infty} (-1)^{\frac{n^2+n}{2}} \frac{n}{2^n}$$

120.
$$\frac{1}{2} + \frac{1}{4} + \frac{1}{6} + \dots + \frac{1}{2n} + \dots$$
 121. $\frac{1}{\sqrt{1.2}} + \frac{1}{\sqrt{2.3}} + \frac{1}{\sqrt{3.4}} + \dots + \frac{1}{\sqrt{n(n+1)}} + \dots$

122.
$$\frac{1}{10^{1/2}} - \frac{1}{10^{1/3}} + \frac{1}{10^{1/4}} - \dots + \frac{(-1)^n}{10^{1/(n+1)}} + \dots$$
 123. $1 + \frac{1}{2!} + \frac{1}{3!} + \dots + \frac{1}{n!} + \dots$

124.
$$\frac{1}{3} + \frac{1}{8} + \frac{1}{15} + \dots + \frac{1}{(n+1)^2 - 1} + \dots$$
 125. $\left(\frac{3}{4}\right)^{\frac{1}{2}} + \frac{5}{7} + \dots + \left(\frac{2n+1}{3n+1}\right)^{\frac{n}{2}} + \dots$

126.
$$1 - \frac{2}{7} + \frac{3}{13} - \dots + \frac{(-1)^{n-1}n}{6n-5} + \dots$$
 127. $-\frac{1}{2} - \frac{2}{4} + \frac{3}{8} + \frac{4}{16} + \dots + (-1)^{\frac{n^2+n}{2}} \frac{n}{2^n} \dots$ 128. $1 - \frac{1}{3} + \frac{1}{3} - \frac{1}{3^2} + \frac{1}{5} - \frac{1}{3^3} + \dots$ 129. $\frac{1}{\sqrt{2}-1} - \frac{1}{\sqrt{2}+1} + \frac{1}{\sqrt{3}-1} - \frac{1}{\sqrt{3}+1} + \dots$

Respuestas

1. Conv.;	2. Div.;	3. Div.; 4.	Div.; 5.	Conv.; 6.	Conv.; 7.	Div.; 8. Div.;
9. Div.;	10. Conv.;	11. Conv.;	12. Conv.;	13. Conv.;	14. Div.;	15. Conv.;
16. Conv.;	17. Div.;	18. Conv.;	19. Conv.;	20. Div.;	21. Conv.;	22. Conv.;
23. Conv.;	24. Conv.;	25. Conv.;	26. Div.;	27. Conv.;	28. Conv.;	29. Conv.;
30. Div.;	31. Conv.;	32. Div.;	33. Div.;	34. Conv.;	35. Conv.;	36. Div.;
37. Conv.;	38. Conv.;	39. Conv.;	40. Div.;	41. Conv.;	42. Conv.;	43. Div.;
44. Div.;	45. Div.;	46. Conv.;	47. Conv.;	48. Conv.;	49. Div.;	50. Conv.;
51. Div.;	52. Conv.;	53. Conv.;	54. Div.;	55. Conv.;	56. Div.;	57. Conv.;
58. Div.;	59. Conv.;	60. Div.;	61. Div.;	62. Conv.;	63. Conv.;	64. Div.;
65. Div.;	66. Conv.;	67. Div.;	68. Conv.;	69. Conv.;	70. Div.;	71. Conv.;
72. Div.;	73. Conv.;	74. Conv.;	75. Conv.;	76. Conv.;	77. Div.;	78. Conv.;
79. Div.;	80. Conv.;	81. Div.;	82. Div.;	83. Conv.;	84. Div.;	85. Div.;
86. Conv.;	87. Conv.;	88. Div.;	89. Div.;	90. Conv.;	91. Conv.;	92. Conv.;
93. Conv.;	94. Conv.;	95. Conv.;	96. Conv.;	97. Conv.;	98. Conv.;	99. Div.;
100. Conv.;	101. Conv.;	102. Conv.;	103. Con	v.; 104. C	onv.; 105.	Conv.;
106. Conv.;	107. Conv.;	108. Conv.;	109. Div.	.; 110. Div	т.; 111. Со	nv.; 112. Div.;
113. Div.;	114. Div.;	115. Conv.;	116. Div.;	117. Div.;	118. Conv.	; 119. Conv.;
120. Div.;	121. Div.;	122. Div.;	123. Conv.;	124. Conv.;	125. Conv	v.; 126. Div.;
127. Conv.;	128. Div.;	129. Div.;				

Bibliografía

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Cálculo Diferencial e Integral - Series numéricas.

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