

## List of Selected Formulae

### (1) P-N junction:

$$V_{bi} = \frac{kT}{q} \ln \frac{N_A N_D}{n_i^2}; \quad N_A x_p = N_D x_n; \quad W = \sqrt{\frac{2\epsilon_s}{q} \left[ \frac{1}{N_A} + \frac{1}{N_D} \right] (V_{bi} - V)}; \quad x_n = \frac{N_A W}{N_A + N_D}; \quad x_p = \frac{N_D W}{N_A + N_D}$$

$$\xi_m = \frac{qN_D x_n}{\epsilon_s} = \frac{qN_A x_p}{\epsilon_s}; \quad C_j = \frac{\epsilon_s}{W} = \sqrt{\frac{q\epsilon_s N_A N_D}{2(V_{bi} - V)(N_A + N_D)}}; \quad L_p = \sqrt{D_p \tau_p}$$

$$J = J_n(-x_p) + J_p(x_n) = \left( \frac{qD_p p_{no}}{L_p} + \frac{qD_n n_{po}}{L_n} \right) (e^{qV/kT} - 1)$$

### (2) Bipolar Junction Transistor:

$$\gamma \equiv \frac{I_{Ep}}{I_E} = \frac{I_{Ep}}{I_{Ep} + I_{En}}; \quad \alpha_T \equiv \frac{I_{Cp}}{I_{Ep}}; \quad \alpha_0 = \gamma \alpha_T; \quad \beta_0 = \frac{\alpha_0}{1 - \alpha_0}; \quad I_C = \alpha_0 I_E + I_{CBO};$$

$$I_{CEO} = (1 + \beta_0) I_{CBO}; \quad p_n(x) = p_{no} e^{qV_{EB}/kT} \left(1 - \frac{x}{W}\right); \quad \gamma = \frac{1}{1 + \frac{D_E}{D_p} \cdot \frac{N_B}{N_E} \cdot \frac{W}{L_E}};$$

$$I_{Ep} = qA \frac{D_p p_{n0}}{W} e^{(qV_{EB}/kT)}; \quad I_{En} = qA \frac{D_E n_{E0}}{L_E} (e^{qV_{EB}/kT} - 1); \quad I_{Cn} = qA \frac{D_C n_{C0}}{L_C};$$

$$p_{n0} \cdot N_B = n_{E0} \cdot N_E = n_{C0} \cdot N_C = n_i^2; \quad \tau_B = \frac{W^2}{2D_p}; \quad f_T = \frac{1}{2\pi\tau_B}.$$

### For npn BJT:

$$n_E(x) = n_{EO} + n_{EO} \left( e^{qV_{EB}/kT} - 1 \right) \exp\left(\frac{x+x_E}{L_E}\right); \quad n_C(x) = n_{CO} - n_{CO} \exp\left(-\frac{x-x_C}{L_C}\right); \quad p_n(x) = p_n(0) \left[ 1 - \frac{x}{W} \right]$$

### (3) MOS diode and MOSFET:

$$q\phi_{ms} = q\phi_m - q\phi_s = q\phi_m - \left( q\chi + \frac{E_g}{2} + q\Psi_B \right)$$

$$\psi_s = 2\psi_B = \frac{2kT}{q} \ln\left(\frac{N_A}{n_i}\right); \quad W_m^2 = \frac{2\epsilon_s(2\psi_B)}{qN_A} = \frac{4\epsilon_s kT}{q^2 N_A} \ln\left(\frac{N_A}{n_i}\right); \quad V_T = \frac{qN_A W_m}{C_o} + 2\psi_B;$$

$$\frac{C}{C_0} = \frac{1}{\sqrt{1 + \frac{2\epsilon_{ox}^2 V}{qN_A \epsilon_s d^2}}}; \quad \frac{1}{C_{min}} = \frac{d}{\epsilon_{ox}} + \frac{W_m}{\epsilon_s}; \quad V_{FB} = \phi_{ms} - \frac{(Q_f + Q_m + Q_{ot})}{C_0}.$$

**Enhancement mode NMOS**

$$I_D = K_n [(V_{GS} - V_T) V_{DS} - \frac{V_{DS}^2}{2}] \text{ for } V_{DS} < V_{GS} - V_T; \quad V_T = \frac{q N_A W_m}{C_0} + 2\psi_B \text{ when } V_{FB} = 0;$$

$$I_D = \frac{K_n}{2} (V_{GS} - V_T)^2 \text{ for } V_{DS} \geq V_{GS} - V_T; \quad K_n = \mu_n C_{ox} \frac{W}{L}.$$

**(4) Thermal oxidation:**

$$t_{ox}^2 + A t_{ox} = B(t + \tau); \quad \tau = \frac{t_{oxi}^2}{B} + \frac{t_{oxi}}{B/A} \cdot t_{ox} = \frac{-A + \sqrt{A^2 + 4B(t + \tau)}}{2}$$

**(5) Diffusion**

Constant source diffusion:  $N(z, t) = N_s \operatorname{erfc}\left(\frac{z}{2\sqrt{Dt}}\right); \quad Q = \frac{2}{\sqrt{\pi}} N_s \sqrt{Dt}$

Limited source diffusion:  $N(z, t) = \frac{Q}{\sqrt{\pi Dt}} \exp\left[-\frac{z^2}{4Dt}\right];$

For pre-deposition:  $Q = 2N_s \sqrt{\frac{Dt}{\pi}}; \quad \text{Diffusion coefficient } D = D_0 \exp\left(-\frac{E_a}{kT}\right)$

**(6) Ion implantation:**Before Annealing

$$N(x) = \frac{Q}{\sqrt{2\pi}\Delta R_p} \exp\left[-\frac{(x - R_p)^2}{2\Delta R_p^2}\right]$$

$$Q = \int_0^\infty N(x) dx = \sqrt{2\pi} N_p \Delta R_p$$

After annealing

$$N(x) = \frac{Q}{\sqrt{2\pi}(\Delta R_p^2 + 2Dt)^{1/2}} \exp\left[-\frac{(x - R_p)^2}{2(\Delta R_p^2 + 2Dt)}\right]$$

Silicon oxide for masking

$$N(t_{ox}) = N_p \exp\left[-\frac{(t_{ox} - R_p)^2}{2\Delta R_p^2}\right] < \frac{N_B}{10}$$

$$t_{ox} \geq R_p + \Delta R_p \sqrt{2 \ln\left(\frac{10N_p}{N_B}\right)}$$

**Table of Physical Constants**

Physical Constant	Symbol	Value	Units
Electronic charge	$q$	$1.6 \times 10^{-19}$	C
Boltzmann's constant	$k$	$8.62 \times 10^{-5}$ $1.38066 \times 10^{-23}$	eV/K J/K
Planck's constant	$h$	$6.626 \times 10^{-34}$	J·s
Permittivity of free space	$\epsilon_0$	$8.85 \times 10^{-14}$	F/cm
Dielectric constant of Si	$\epsilon_{Si}$	11.7	-
Dielectric constant of SiO <sub>2</sub>	$\epsilon_{ox}$	3.9	-
Electron Mass	$m$	$9.11 \times 10^{-31}$	kg
Speed of Light	$c$	$3 \times 10^8$	m/s
Bandgap of Si at 300 K	$E_g$	1.12	eV
Intrinsic carrier concentration in Si at 300 K	$n_i$	$1.5 \times 10^{10}$	cm <sup>-3</sup>