

In case of transformers, the frequency f remains constant so that

$$P_h = K_h B_m^n f \propto B_m^2 \text{ (take } n \approx 2) \text{ and,}$$

$$P_e = K_e B_m^2 f^2 \propto B_m^2$$

$$\text{Thus, } P_c = (P_e + P_h) \propto B_m^2$$

Let $\phi = \Phi_m \sin \omega t$, then

$$\begin{aligned} v = e &= N \frac{d\Phi}{dt} = N \Phi_m \omega \cos \omega t \\ &= N(B_m A)(2\pi f) \cos \omega t \\ &= 2\pi N A (B_m f) \cos \omega t \end{aligned}$$

Therefore, the root mean square (rms) value of the voltage is given by

$$V = V_m / \sqrt{2} = 2\pi N A (B_m f) / \sqrt{2} = 4.44 N A B_m f$$

$$\begin{aligned} E_1 &= 4.44 N_1 A B_m f \quad \text{constant at 50 Hz} \\ \therefore E_1 &\propto B_m \\ E_1^2 &\propto B_m^2 \quad \text{--- (1)} \\ P_c &\propto B_m^2 \quad \text{--- (2)} \\ \therefore P_c &\propto E_1^2 \\ \text{Core loss } P_c &= \frac{E_1^2}{R_{c1}} \\ \Rightarrow P &= \frac{V^2}{R} \\ \therefore R_{c1} &\text{ connected across } E_1 \end{aligned}$$

A 23-kVA, 2300/230-V, 60-Hz transformer has the following parameters:

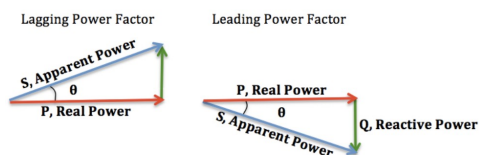
$$R_1 = 4 \, \Omega, R_2 = 0.04 \, \Omega, X_1 = 12 \, \Omega, X_2 = 0.12 \, \Omega,$$

$$R_{c1} = 20 \, \text{k}\Omega, \text{ and } X_{m1} = 15 \, \text{k}\Omega$$

Draw the actual equivalent circuit of the transformer. If the transformer delivers 75% of its rated load at 0.866 pf (lag) at rated voltage, determine

- the input current,
- the input voltage,
- the total copper loss,
- the core loss, and
- the input power.

(Solution)



The terms 'leading' and 'lagging' refer to where the load current phasor lies in relation to the supply voltage phasor. Capacitive-> leading; inductive-> lagging