

**NANYANG TECHNOLOGICAL UNIVERSITY****SEMESTER 1 EXAMINATION 2020-2021****EE2002 – ANALOG ELECTRONICS**

November / December 2020

Time Allowed: 2 hours

**INSTRUCTIONS**

1. This paper contains 4 questions and comprises 10 pages.
  2. Answer all 4 questions.
  3. All questions carry equal marks.
  4. This is a closed book examination.
  5. Unless specifically stated, all symbols have their usual meanings.
  6. A list of formulae is provided in Appendix A on pages 7-10.
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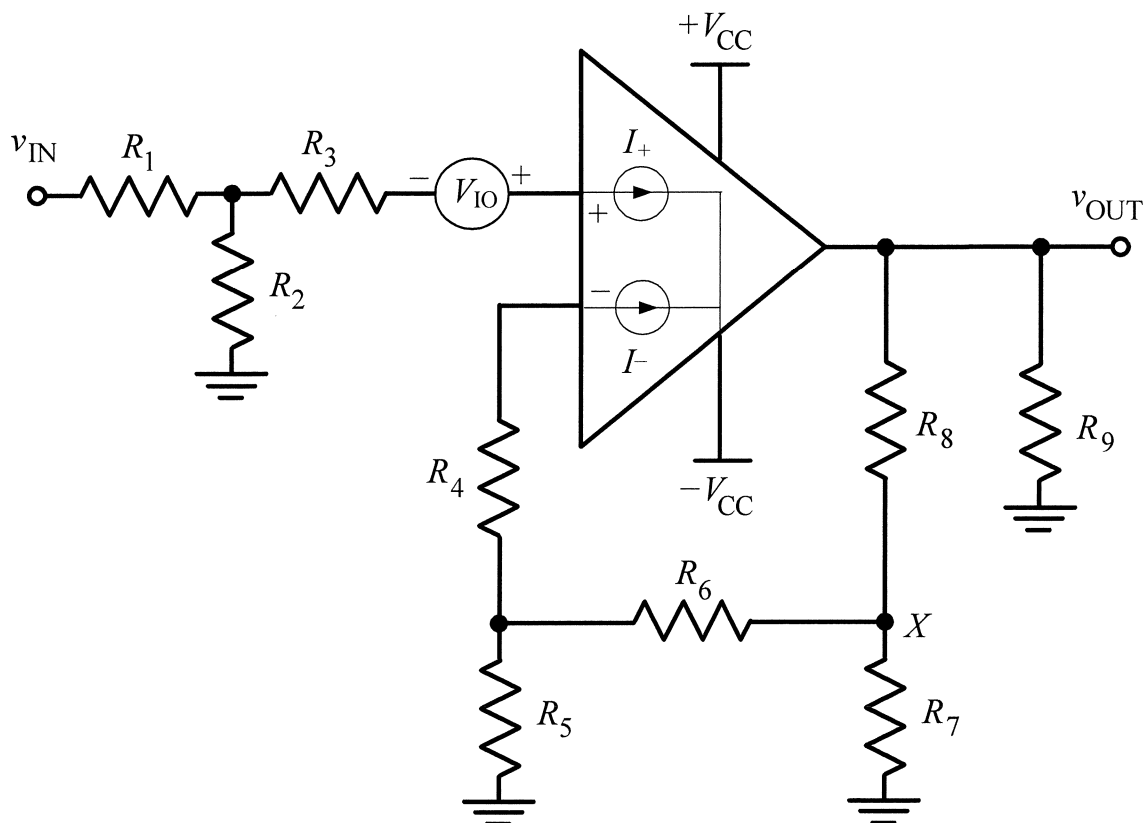
1. (a) A non-ideal Op-Amp configured with resistors is shown in Figure 1(a) on page 2. The Op-Amp is powered by  $\pm V_{CC}$  power supplies. It has 1 input source,  $v_{IN}$  and 3 non-ideal sources,  $I_+$ ,  $I_-$  and  $V_{IO}$ .

Derive the expression for the output voltage  $v_{OUT}$ , in terms of all or some of the followings:  $v_{IN}$ ,  $R_1$ ,  $R_2$ ,  $R_3$ ,  $R_4$ ,  $R_5$ ,  $R_6$ ,  $R_7$ ,  $R_8$ ,  $R_9$ ,  $I_+$ ,  $I_-$  and  $V_{IO}$ .

**Note:** Parallel resistance of  $R_x$  and  $R_y$  can be written as  $R_x // R_y$  without expanding it.

(13 Marks)

Note: Question No. 1 continues on page 2.

**Figure 1(a)**

(b) In Figure 1(b) on page 3, the empirical junction diode equation is:

$$V_D = nV_T \ln[I_D/I_S]$$

for the identical diodes  $D_1$ ,  $D_2$ ,  $D_3$  and  $D_4$ , given that 2 points on the diode  $I$ - $V$  characteristic curve are:

$$V_{Dx} = 0.650 \text{ V at } I_{Dx} = 400 \text{ } \mu\text{A and}$$

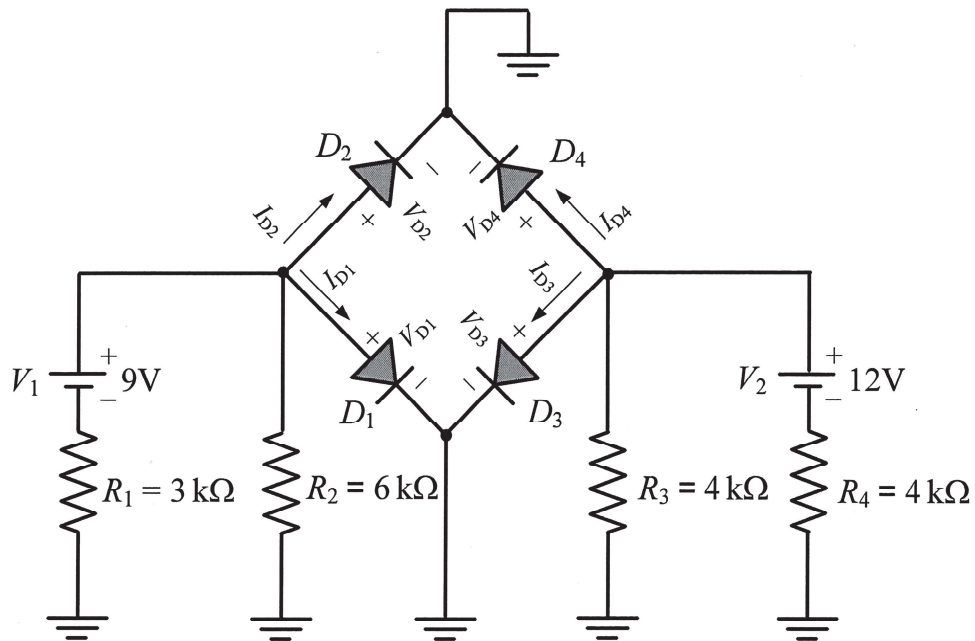
$$V_{Dy} = 0.740 \text{ V at } I_{Dy} = 4 \text{ mA.}$$

Also given that  $V_1 = 9 \text{ V}$  and  $V_2 = 12 \text{ V}$ ,  $R_1 = 3 \text{ k}\Omega$ ,  $R_2 = 6 \text{ k}\Omega$ ,  $R_3 = 4 \text{ k}\Omega$  and  $R_4 = 4 \text{ k}\Omega$ , find the DC operating point or quiescent (Q) - point ( $I_D$ ,  $V_D$ ) for the diodes  $D_1$ ,  $D_2$ ,  $D_3$  and  $D_4$  (to 3 decimal places in mA and V, respectively).

**Note:**  $D_1$ ,  $D_2$ ,  $D_3$  and  $D_4$  have the same  $nV_T$  and  $I_S$ .

(12 Marks)

Note: Question No. 1 continues on page 3.

**Figure 1(b)**

2. For the single-stage amplifier shown in Figure 2 on page 4, the MOSFET has parameters of  $K_n = 250 \mu\text{A}/\text{V}^2$ ,  $V_{TN} = 0.5 \text{ V}$  and  $\lambda = 0.01\text{V}^{-1}$ . All the capacitors  $C_i$  and  $C_o$  in the circuit are assumed to have infinite capacitance.

(a) Find the DC operating point ( $I_D$ ,  $V_{DS}$ ) of the MOSFET.

(6 Marks)

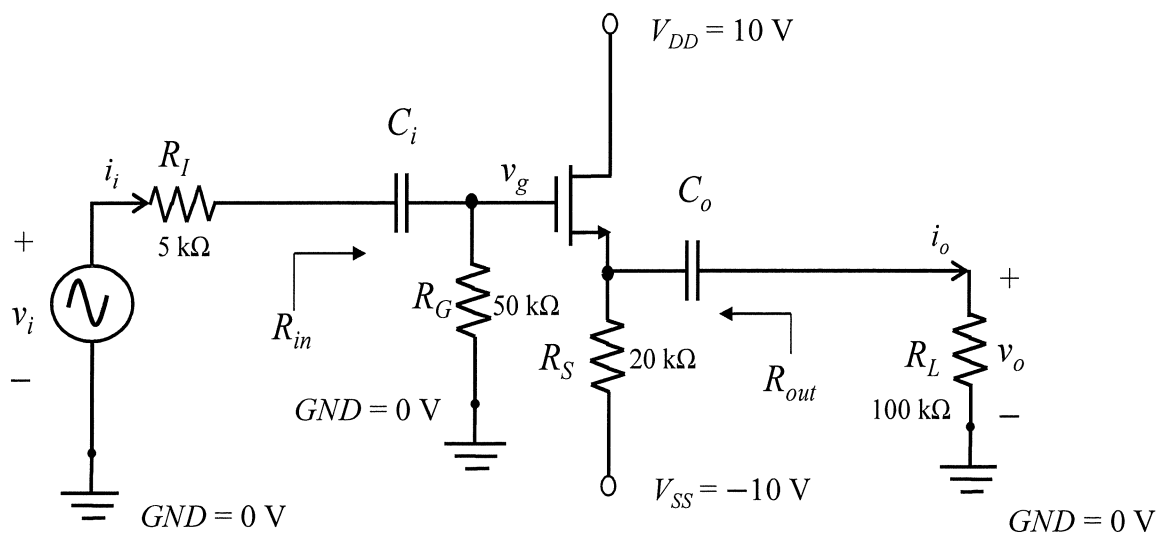
(b) Draw the small signal equivalent circuit and derive the algebraic expressions for the input and output resistances ( $R_{in}$  and  $R_{out}$ ), voltage and current gains ( $A_v = v_o/v_i$  and  $A_i = i_o/i_i$ ) of this circuit in terms of  $g_m$ ,  $r_o$  and the resistors in the figure.

(12 Marks)

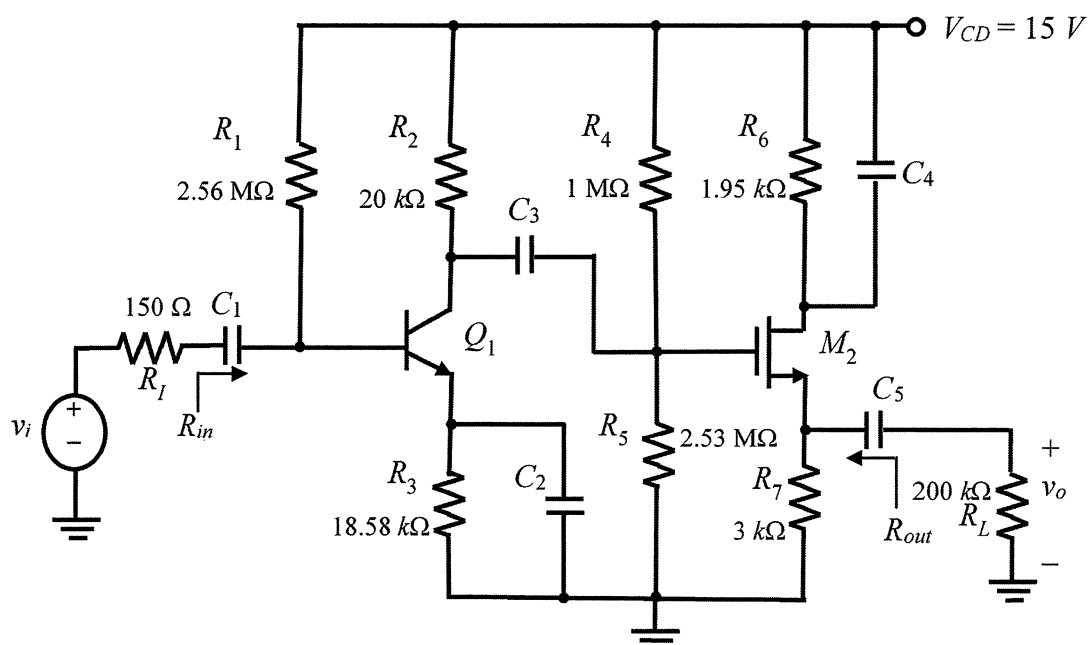
(c) Using the results of the DC analysis in part (a), find the values of the small signal parameters  $g_m$ ,  $r_o$  and use them to find the numerical values of  $R_{in}$ ,  $R_{out}$ ,  $A_v$  and  $A_i$  determined in part (b).

(7 Marks)

Note: Question No. 2 continues on page 4.

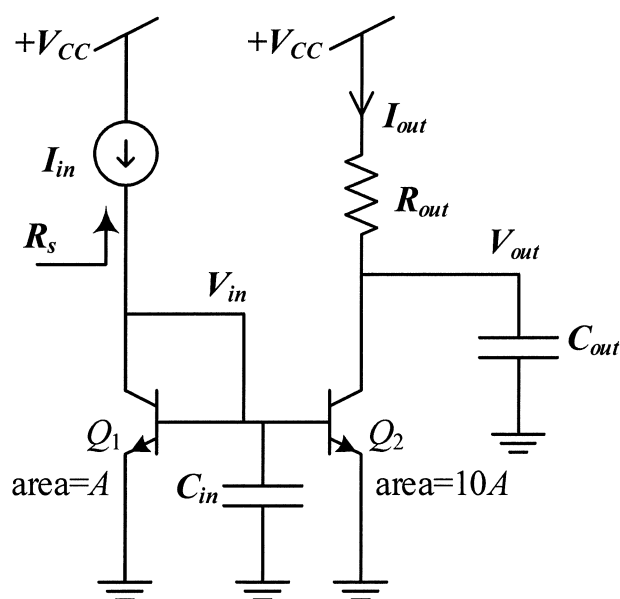
**Figure 2**

3. In Figure 3, the DC operating point for NPN BJT  $Q_1$  are  $I_C = 324\text{ }\mu\text{A}$  and  $V_{CE} = 2.5\text{ V}$ , and the DC operating point for NMOS transistor  $M_2$  are  $I_D = 2.56\text{ mA}$  and  $V_{DS} = 2.32\text{ V}$ .  $Q_1$  has  $\beta = 100$ ,  $V_A = 75\text{ V}$ , and  $V_T = 25\text{ mV}$  at room temperature, and  $M_2$  has  $K_n = 1.5\text{ mA/V}^2$ ,  $V_{TN} = 1\text{ V}$  and  $\lambda = 0.01\text{ V}^{-1}$ . Assume that  $V_{CD} = 15\text{ V}$  and all the capacitors have infinite values, and resistors have the values as indicated in Figure 3.

**Figure 3**

Note: Question No. 3 continues on page 5.

- (a) Draw the small signal equivalent circuits. (5 Marks)
- (b) Determine the voltage gain  $A_v = \frac{v_o}{v_i}$ . (7 Marks)
- (c) Determine the input resistance  $R_{in}$  and output resistance  $R_{out}$  of the amplifier. (8 Marks)
- (d) Determine the input signal range for this amplifier for small signal operation. (5 Marks)
4. The BJT current mirror shown in Figure 4 consists of an input transistor  $Q_1$  and an output transistor  $Q_2$ , which are sized to have emitter areas  $A$  and  $10A$  respectively. Both transistors have the same current gain  $\beta$ .



**Figure 4**

Note: Question No. 4 continues on page 6.

- (a) Without considering the Early effect, find the DC mirror ratio  $I_{out} / I_{in}$ , in terms of the current gain  $\beta$ . You may ignore the AC effects produced by  $R_s$ ,  $C_{in}$  and  $C_{out}$  for now.  
(3 Marks)
- (b) Now considering the Early effect, find a new expression for the mirror ratio  $I_{out} / I_{in}$ , which includes the terms  $V_{in}$ ,  $V_{out}$  and Early voltage  $V_A$ .  
(3 Marks)
- (c) Calculate the value of  $I_{out}$  given that  $I_{in} = 1\mu\text{A}$ ,  $\beta = 100$ ,  $V_{in} = 0.7\text{V}$ ,  $V_{cc} = 5\text{V}$ ,  $V_A = 50\text{V}$  and  $R_{out} = 0.1\text{ M}\Omega$ . [Hint: express  $V_{out}$  in terms of  $I_{out}$  due to load resistor  $R_{out}$ , and substitute that into your answer for part (b)]  
(8 Marks)
- (d) Now consider the AC effects produced by  $R_s$ ,  $C_{in}$  and  $C_{out}$  on the transfer function  $I_{out} / I_{in}$ . Draw the small-signal circuit for Figure 4, including these components.  
(4 Marks)
- (e) Explain whether  $C_{in}$  and  $C_{out}$  will contribute to the lower cut-off frequency  $\omega_L$ , or the upper cut-off frequency  $\omega_H$ . In your answer, use either the SCTC or OCTC method to calculate  $\tau_{in}$  and  $\tau_{out}$  under the DC condition found in part (c). Assume  $R_s = 1\text{M}\Omega$ ,  $C_{in} = C_{out} = 1\text{pF}$ .  
(4 Marks)
- (f) Based on your answer in part (e), solve for the relevant cut-off frequency (either  $\omega_L$  or  $\omega_H$ ). Is one of the time constants,  $\tau_{in}$  or  $\tau_{out}$ , a dominant term in your answer? If so, explain why.  
(3 Marks)

**Appendix A****List of Formulae (with the usual notations)****Op-Amps:**

Closed-Loop Negative Feedback Inverting Gain,  $A_{VCL} = \frac{v_o}{v_i} = -\frac{R_f}{R_i}$

Figure (a)

Closed-Loop Negative Feedback Non-Inverting Gain,  $A_{VCL} = \frac{v_o}{v_i} = \left(1 + \frac{R_f}{R_i}\right)$

Figure (b)

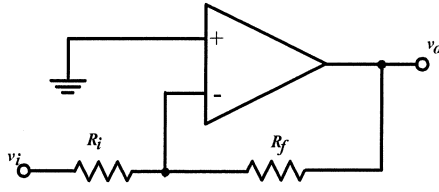


Figure (a)

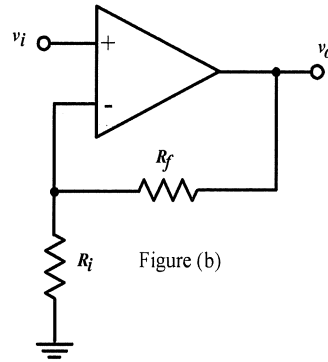


Figure (b)

Op-Amp's Slew Rate,  $SR \geq \left| \frac{dv_o}{dt} \right|_{\max} = A_{VCL} \omega a_m = A_{VCL} a_m 2\pi f$ ,

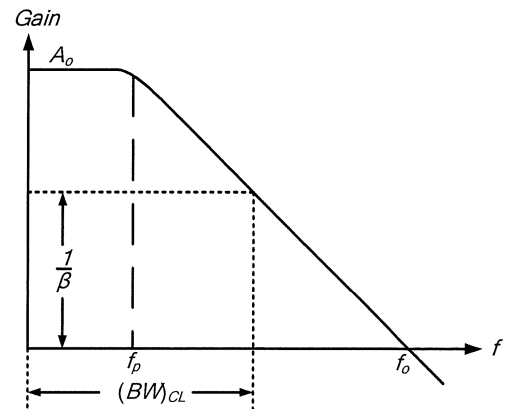
where  $v_i = a_m \sin(\omega t)$ ,  $v_o = A_{VCL} v_i$ ,  $v_o = A_{VCL} a_m \sin(\omega t)$  and  $\left| \frac{dv_o}{dt} \right| = A_{VCL} \omega a_m \cos(\omega t)$

Op-Amp's frequency response:  $A_{VOL}(jf) = \frac{A_o}{\left(1 + \frac{jf}{f_p}\right)}$

Gain-Bandwidth Product:  $A_o f_p = f_o = \frac{1}{\beta} (BW)_{CL}$

where  $\frac{1}{\beta} = \frac{R_f + R_i}{R_i}$

$t_r = \frac{0.35}{(BW)_{CL}}$

**Diodes:**

$v_D \approx nV_T \ln\left(\frac{i_D}{I_S}\right)$  or  $i_D \approx I_S e^{\left(\frac{v_D}{nV_T}\right)}$

where  $e^x = 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \dots$

**Appendix A (Continued)**

Diode conductance:  $g_D = \frac{1}{r_D} = \frac{I_D}{nV_T}$

**BJT in Forward Active Region:**

Ignore early effect:  $i_C = I_S \exp\left(\frac{v_{BE}}{V_T}\right)$

With early effect:  $i_C = I_S \exp\left(\frac{v_{BE}}{V_T}\right) \left(1 + \frac{v_{CE}}{V_A}\right)$

where  $I_S$ : Saturation current,

$V_T$ : Thermal voltage, assume 25 mV at room temperature,

$V_A$ : Early voltage.

For npn transistor,  $|v_{BE}| = v_{BE}$  and  $|v_{CE}| = v_{CE}$ ;

For pnp transistor,  $|v_{BE}| = v_{EB}$  and  $|v_{CE}| = v_{EC}$ .

**Small-signal model parameters of BJT:**

$$g_m = \frac{I_C}{V_T}, \quad r_\pi = \frac{\beta}{g_m} \quad \text{and} \quad r_o = \frac{V_A + |V_{CE}|}{I_C} \approx \frac{V_A}{I_C}$$

where  $I_C$ : DC collector current at Q-point

$V_{CE}$ : DC collector-emitter voltage at Q-point

Criterion for small-signal operation of BJT:  $|v_{be}| \leq 0.2V_T$

**MOSFET in Saturation Region:**

Criterion:  $V_{DS} \geq V_{GS} - V_{TN}$  for NMOS;

$|V_{DS}| \geq |V_{GS}| - |V_{TP}|$  for PMOS

where  $V_{TN}$ ,  $V_{TP}$ : Threshold voltage,

$V_{DS}$ : DC drain-source voltage,

$V_{GS}$ : DC gate-source voltage.

Ignore channel-length modulation effect:  $i_D = \frac{K_n}{2} (v_{GS} - V_{TN})^2$  for NMOS,

$$i_D = \frac{K_p}{2} (|v_{GS}| - |V_{TP}|)^2 \quad \text{for PMOS.}$$



**Appendix A (Continued)**

With channel-length modulation effect:  $i_D = \frac{K_n}{2}(v_{GS} - V_{TN})^2(1 + \lambda v_{DS})$  for NMOS,

$$i_D = \frac{K_p}{2}(|v_{GS}| - |V_{TP}|)^2(1 + \lambda |v_{DS}|) \text{ for PMOS.}$$

where  $\lambda$ : channel length modulation parameter,

For NMOS  $K_n = K'_n \left( \frac{W}{L} \right)$  and  $K'_n = \mu_n C_{ox}$ ; For PMOS  $K_p = K'_p \left( \frac{W}{L} \right)$  and  $K'_p = \mu_p C_{ox}$ .

**MOSFET in Triode Region:**

Criterion:  $V_{DS} < V_{GS} - V_{TN}$  for NMOS;  
 $|V_{DS}| < |V_{GS}| - |V_{TP}|$  for PMOS

Ignore channel-length modulation effect:  $i_D = K_n \left( v_{GS} - V_{TN} - \frac{v_{DS}}{2} \right) v_{DS}$  for NMOS,

$$i_D = K_p \left( |v_{GS}| - |V_{TP}| - \frac{|v_{DS}|}{2} \right) |v_{DS}| \text{ for PMOS.}$$

With channel-length modulation effect:  $i_D = K_n \left( v_{GS} - V_{TN} - \frac{v_{DS}}{2} \right) v_{DS} (1 + \lambda v_{DS})$  for NMOS,

$$i_D = K_p \left( |v_{GS}| - |V_{TP}| - \frac{|v_{DS}|}{2} \right) |v_{DS}| (1 + \lambda |v_{DS}|) \text{ for PMOS.}$$

**Small-signal model parameters of MOSFET**

For NMOS:  $g_m = \sqrt{2K_n I_D (1 + \lambda V_{DS})} \approx \sqrt{2K_n I_D}$  and  $r_o = \frac{\frac{1}{\lambda} + V_{DS}}{I_D} \approx \frac{1}{\lambda I_D}$

For PMOS:  $g_m = \sqrt{2K_p I_D (1 + \lambda |V_{DS}|)} \approx \sqrt{2K_p I_D}$  and  $r_o = \frac{\frac{1}{\lambda} + |V_{DS}|}{I_D} \approx \frac{1}{\lambda I_D}$

where  $I_D$ : DC drain current at Q-point

$V_{DS}$ : DC drain-source voltage at Q-point

Criterion for small-signal operation:

For NMOS:  $|v_{gs}| \leq 0.2(V_{GS} - V_{TN})$

For PMOS:  $|v_{gs}| \leq 0.2(|V_{GS}| - |V_{TP}|)$

where  $V_{GS}$ : DC gate-source voltage at Q-point.

**Appendix A (Continued)****Frequency Response: OCTC and SCTC**

- 0) DISABLE DC sources...  
voltage sources -> SHORT CIRCUIT, current sources -> OPEN CIRCUIT
- 1) Identify capacitors contributing (reducing  $V_o$  or causing trouble) to the frequency of interest (i.e. lower or higher cut-off).
- 2) DISABLE all independent AC sources...  
voltage sources -> SHORT CIRCUIT, current sources -> OPEN CIRCUIT  
DO NOT remove or "disable" dependent sources!

↓  
higher cut-off  
(OCTC)

↓  
lower cut-off  
(SCTC)

- 3) Idealize irrelevant capacitors by SHORT CIRCUIT (because at high  $f$ , cap  $\rightarrow$  short)

Next step to find time constant

- 4) For each contributing capacitor  $C_i$ , set all other capacitors (other than the one you are looking at) removed (i.e. OPEN CIRCUITS) and determine the resistance,  $R_i$  seen by  $C_i$

- 5) Higher cut-off frequency is estimated as:

$$\omega_{H-3dB} \approx \frac{1}{\sum_i C_i R_i} = \frac{1}{C_1 R_1 + C_2 R_2 + \dots}$$

- 3) Idealize irrelevant capacitors by OPEN CIRCUIT (because at low  $f$ , cap  $\rightarrow$  open)

Next step to find time constant

- 4) For each contributing capacitor  $C_i$ , set all other capacitors (other than the one you are looking at) removed (i.e. SHORT CIRCUITS) and determine the resistance,  $R_i$  seen by  $C_i$

- 5) Lower cut-off frequency is estimated as:

$$\omega_{L-3dB} \approx \sum_i \frac{1}{C_i R_i} = \frac{1}{C_1 R_1} + \frac{1}{C_2 R_2} + \dots$$

END OF PAPER

1. a) By superposition theorem

$$V_{out} = V|_{I_N} + V|_{I_+} + V|_{I_-} + V|_{V_{IO}}$$

Regardless of all other factors  
for  $V|_{I_N}$

$$V_+ = V_{IN} \cdot \frac{R_2}{R_1 + R_2} = V_-$$

$$V_x = V_- \cdot \frac{R_5 + R_6}{R_5}$$

$$V_{out1} = (V_- / R_5 + V_x / R_7) \cdot R_8 + V_x$$

$$= V_{IN} \left[ \frac{R_2 \cdot R_8}{(R_1 + R_2) \cdot R_5} + \frac{R_2 \cdot (R_5 + R_6) \cdot R_8}{R_5 \cdot R_7 \cdot (R_1 + R_2)} \right] + V_{IN} \cdot \frac{R_2 \cdot (R_5 + R_6)}{R_5 \cdot (R_1 + R_2)}$$

for  $V|_{I_+}$

$$V_+ = -I_+ \cdot [R_3 + R_1 \parallel R_2] = V_-$$

$$V_x = V_- \cdot (R_5 + R_6) / R_5$$

$$V_{out2} = (V_- / R_5 + V_x / R_7) \cdot R_8 + V_x$$

$$= -I_+ \left[ \frac{(R_3 + R_1 \parallel R_2) \cdot R_8}{R_5} + \frac{(R_3 + R_1 \parallel R_2) \cdot (R_5 + R_6) \cdot R_8}{R_5 \cdot R_7} \right]$$

for  $V|_{I_-}$

$$+ -I_+ \cdot \frac{(R_3 + R_1 \parallel R_2) \cdot (R_5 + R_6)}{R_5}$$

$$V_+ = V_- = 0$$

$$\left( \frac{R_4 \cdot I_-}{R_5} + I_- \right) \times R_6 + I_- \cdot R_4 = V_x$$

$$V_{out3} = \left( \frac{R_4 \cdot I_-}{R_4 \parallel R_5} \right) \times R_8 + (V_x / R_7) \times R_8 + V_x$$

$$= I_- \left[ \left( \frac{R_4 R_8}{R_5} + R_8 \right) + \left( \frac{R_4 R_6 R_8}{R_5 \cdot R_7} + \frac{R_6 R_8}{R_7} \right) + \frac{R_4 R_8}{R_7} + \frac{(R_4 + R_5) \cdot R_6}{R_5} + R_4 \right]$$

for  $V|_{V_{IO}}$

$$V_+ = V_- = V_{IO}$$

$$V_x = V_{IO} \times \frac{(R_5 + R_6)}{R_5}$$

$$V_{out4} = V_{IO} \left[ (R_8 / R_5) + \frac{(R_5 + R_6) \cdot R_8}{R_5 \cdot R_7} + \frac{R_5 + R_6}{R_5} \right]$$

Combine them together

$$V_{out} = V_{out1} + V_{out2} + V_{out3} + V_{out4}$$



$$1 \text{ b) } V_{Dx} = nV_T \ln [I_{Dx} / I_S] \dots ①$$

$$V_{Dy} = nV_T \ln [I_{Dy} / I_S] \dots ②$$

to find the value of  $nV_T$  &  $I_S$

$$② - ①$$

$$V_{Dy} - V_{Dx} = nV_T \ln [I_{Dy} / I_{Dx}]$$

$$\Rightarrow nV_T = 39.1 \text{ mV}$$

$$\Rightarrow I_S = 2.412 \times 10^{-11} \text{ A}$$

Based on Figure 1(b)

$$V_{D1} = V_{D2} ; V_{D3} = V_{D4}$$

$$\text{ie. } I_{D1} = I_{D2} ; I_{D3} = I_{D4}$$

$$\text{left: } (I_{D1} + I_{D2} + \frac{V_{D1}}{R_2}) \cdot R_1 = V_1 - V_{D1}$$

$$\Rightarrow V_{D1} = 6 - 4k I_{D1}$$

$$\text{right: } (I_{D3} + I_{D4} + \frac{V_{D3}}{R_3}) \cdot R_4 = V_2 - V_{D3}$$

$$\Rightarrow V_{D3} = 6 - 4k I_{D3}$$

$$\therefore V_{D1} = V_{D2} = V_{D3} = V_{D4} = V_D ; I_{D1} = I_{D2} = I_{D3} = I_{D4} = I_D$$

$$\begin{cases} I_D = \frac{1}{4k} \cdot (6 - V_D) \\ V_D = 0.0391 \cdot \ln [I_D / 2.412 \times 10^{-11}] \end{cases}$$

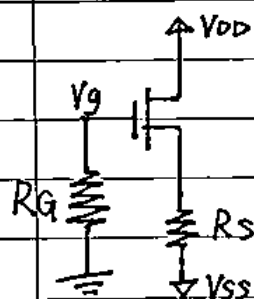
do iteration

$$V_D \quad 0.700 \text{ V} \rightarrow 0.697 \rightarrow 0.697 \checkmark$$

$$I_D \quad 1.325 \text{ mA} \quad 1.326 \checkmark$$

$$\therefore \text{Q point } I_D = 1.326 \text{ mA} \quad V_D = 0.697 \text{ V}$$

2. a) Draw DC diagram



Since  $I_G = 0 \therefore V_g = 0$

$$0 = V_{GS} + I_D \cdot R_S + V_{SS}$$

$$10 \text{ V} = V_{GS} + \frac{K_n}{2} (V_{GS} - V_{TN})^2 \times R_S$$

$$10 = V_{GS} + \frac{250 \mu}{2} (V_{GS} - 0.5)^2 \times 20k$$

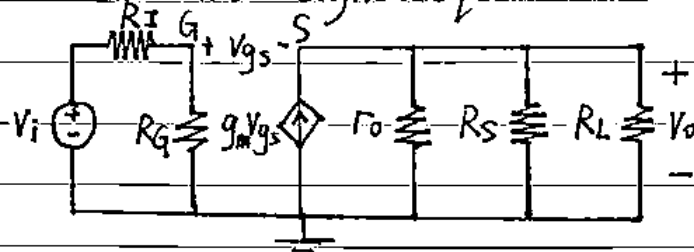
$$2.5 V_{GS}^2 - 1.5 V_{GS} + \frac{5}{8} = 10$$

$$V_{GS} = 2.26 \text{ V}$$

$$\therefore I_D = 387.2 \mu\text{A} ; \therefore V_{DD} - V_{DS} - I_D R_S - V_{SS} = 0 \Rightarrow V_{DS} = 12.256 \text{ V}$$



2. b) the small signal equivalent circuit :



$$R_L' = r_o \parallel R_S \parallel R_L$$

$$A_{vt} = V_s/V_g = g_m V_{gs} R_L' / V_{gs} + g_m V_{gs} R_L' = \frac{g_m R_L'}{1 + g_m R_L'}$$

$$\therefore A_v = V_o/V_i = A_{vt} \times \frac{R_G}{R_G + R_I}$$

$$= \frac{g_m \cdot R_G \cdot (r_o \parallel R_S \parallel R_L)}{(R_G + R_I) \cdot [1 + g_m (r_o \parallel R_S \parallel R_L)]}$$

$$R_{in} = R_G$$

$$\therefore i_x = \frac{V_x}{R_S} + \frac{V_x}{r_o} - g_m V_{gs} ; V_{gs} = -V_x$$

$$\therefore i_x = \left( \frac{1}{R_S} + \frac{1}{r_o} + g_m \right) V_x$$

$$R_{out} = V_x / i_x = R_S \parallel r_o \parallel \frac{1}{g_m}$$

$$A_i = i_o / i_i$$

$$= (V_o / R_{out}) / (V_i / R_{in}) = A_v \cdot \frac{R_{in}}{R_{out}} = A_v \cdot \frac{R_G}{R_S \parallel r_o \parallel \frac{1}{g_m}}$$

c)

$$g_m = \sqrt{2K_n I_D (1 + \lambda V_{DS})} = 0.4662 \text{ mS}$$

$$r_o = \left( \frac{1}{\lambda} + V_{DS} \right) / I_D = 289.92 \text{ k}\Omega$$

$$R_{in} = 50 \text{ k}\Omega$$

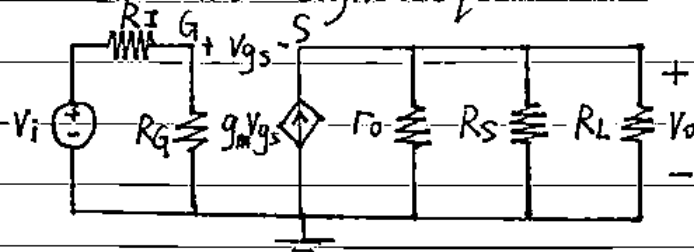
$$R_{out} = 1924.38 \Omega$$

$$A_v = 0.8$$

$$A_i = 20.786$$



2. b) the small signal equivalent circuit :



$$R_L' = r_o \parallel R_S \parallel R_L$$

$$A_{vt} = V_s/V_g = g_m V_{gs} R_L' / V_{gs} + g_m V_{gs} R_L' = \frac{g_m R_L'}{1 + g_m R_L'}$$

$$\therefore A_v = V_o/V_i = A_{vt} \times \frac{R_G}{R_G + R_I}$$

$$= \frac{g_m \cdot R_G \cdot (r_o \parallel R_S \parallel R_L)}{(R_G + R_I) \cdot [1 + g_m (r_o \parallel R_S \parallel R_L)]}$$

$$R_{in} = R_G$$

$$\therefore i_x = \frac{V_x}{R_S} + \frac{V_x}{r_o} - g_m V_{gs} ; V_{gs} = -V_x$$

$$\therefore i_x = \left( \frac{1}{R_S} + \frac{1}{r_o} + g_m \right) V_x$$

$$R_{out} = V_x/i_x = R_S \parallel r_o \parallel \frac{1}{g_m}$$

$$A_i = i_o/i_i$$

$$= (V_o/R_{out}) / (V_i/R_{in}) = A_v \cdot \frac{R_{in}}{R_{out}} = A_v \cdot \frac{R_G}{R_S \parallel r_o \parallel \frac{1}{g_m}}$$

c)

$$g_m = \sqrt{2K_n I_D (1 + \lambda V_{DS})} = 0.4662 \text{ mS}$$

$$r_o = \left( \frac{1}{\lambda} + V_{DS} \right) / I_D = 289.92 \text{ k}\Omega$$

$$R_{in} = 50 \text{ k}\Omega$$

$$R_{out} = 1924.38 \Omega$$

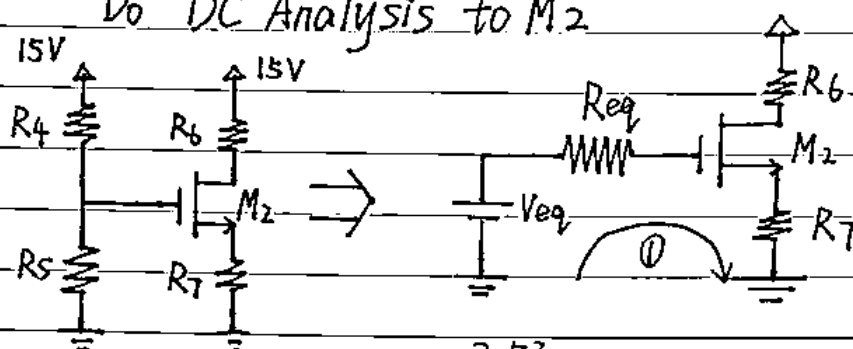
$$A_v = 0.8$$

$$A_i = 20.786$$



3 d) At  $V_{GS}$ , signal reach the maximum  
 $\therefore |V_{GS}| \leq 0.2 (V_{GS} - V_{TN})$

Do DC Analysis to  $M_2$



where  $V_{eq} = \frac{2.53}{1+2.53} \times 15 = 10.75 \text{ V}$

$$R_{eq} = R_4 \parallel R_5 = 0.717 \text{ M}\Omega$$

KVL1:  $\therefore I_G = 0, V_{eq} = V_{GS} + I_D R_S$

$$10.75 = V_{GS} + 0.5 \times 15 \text{ m} (V_{GS} - 1)^2 \times 3 \text{ k}$$

$$2.25 V_{GS}^2 - 3.5 V_{GS} - 8.5 = 0$$

$$V_{GS} = 2.87 \text{ V}$$

$$\therefore |V_{GS}| \leq 0.374 \text{ V}$$

$$\therefore |V_i \times \frac{r_{\pi} \parallel R_1}{R_1 + r_{\pi} \parallel R_1} \times A_{v_{t1}}| \leq 0.374$$

$$V_i \leq 1.635 \text{ mV}$$

4 a) in DC Analysis without early effect

$$I_{C1} = I_{S0} \cdot (A_{E1}/A) \cdot e^{V_{BE}/V_T}$$

$$I_{C2} = I_{S0} \cdot (10 A_{E1}/A) \cdot e^{V_{BE}/V_T}$$

$$I_{B1} = I_{C1} / \beta \quad I_{B2} = I_{C2} / \beta$$

$$MR = \frac{I_{out}}{I_{REF}} = \frac{I_{C2}}{I_{C1} + I_{B1} + I_{B2}} = \frac{10}{1 + \frac{11}{\beta}}$$

b) with early effect

$$I_{C1} = I_{S0} \cdot (A_{E1}/A) \cdot e^{V_{BE}/V_T} \cdot (1 + \frac{V_{in}}{V_A})$$

$$I_{C2} = I_{S0} \cdot (10 A_{E1}/A) \cdot e^{V_{BE}/V_T} \cdot (1 + \frac{V_{out}}{V_A})$$

$$MR = \frac{10 \cdot (1 + \frac{V_{out}}{V_A})}{1 + \frac{V_{in}}{V_A} + \frac{11}{\beta}}$$

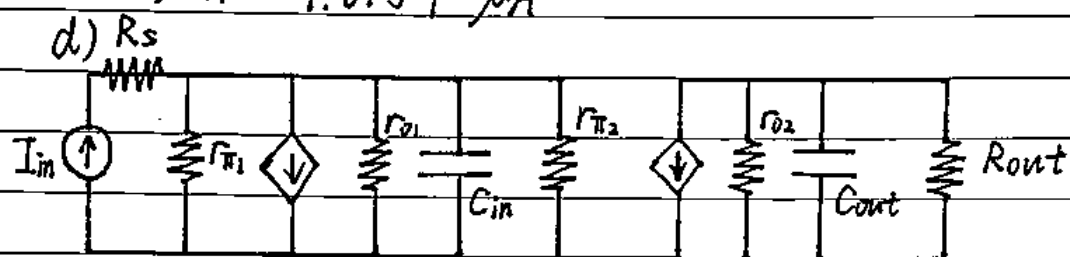


4 c) set  $I_{out}$  as  $x$

$$V_{out} = V_{oc} - I_{out} \cdot R_{out}$$

$$MR = \frac{10 + 10 \cdot (5 - x \cdot 10^5) / 50}{1 + \frac{0.7}{50} + \frac{11}{100}} = \frac{x}{1/\mu}$$

$$\Rightarrow x = 9.6154 \mu A$$



e) & f) didn't have time to finish  $x$

Tips: 1. a) op-amp analysis

b) diodes circuit analysis (iteration method)

2. simple BJT/MOSFET circuit DC & AC analysis

3. Multi-Stage or Differential Amplifiers



Based on simple structure in Q2



Try to remember the result

derived in ~~the~~ slides

4. Current Mirror + Frequency Response

Most of us didn't have enough time to finish.

If you are out of time, just leave the derived equation there and skip calculation part. (Especially for Q3)

Try as many pyp papers as you can to be familiar with the types of questions.

Good luck

祝好

陈