

**NANYANG TECHNOLOGICAL UNIVERSITY**  
**SEMESTER 2 EXAMINATION 2018-2019**  
**EE2003 – SEMICONDUCTOR FUNDAMENTALS**

April / May 2019

Time Allowed: 2½ hours

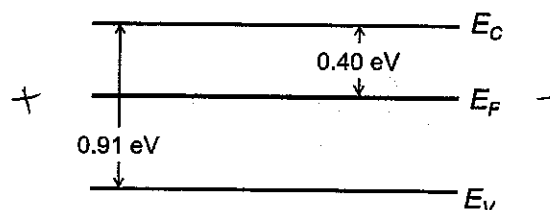
**INSTRUCTIONS**

1. This paper contains 4 questions and comprises 10 pages.
  2. Answer ALL questions.
  3. All questions carry equal marks.
  4. This is a closed book examination.
  5. Unless specifically stated, all symbols have their usual meanings.
  6. A List of Selected Formulae, Table of Physical Constants and Table of Material Properties are provided in Appendices A, B and C, respectively, on pages 6-8, 9 and 10.
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1. (a) A hypothetical compound semiconductor, made up of two different atoms A and B, has a diamond crystal structure of lattice constant  $a$ . The diameter of atom B is 0.75 times that of atom A. The atoms are closely packed such that the surface of one atom (assumed to be spherical in shape) is in contact with its nearest neighbours.
    - (i) If  $r$  is the radius of atom A, express  $r$  in terms of the lattice constant  $a$ .
    - (ii) Determine the percentage of the unit cell volume occupied by the atoms.
    - (iii) Sketch the placement of atoms on the (110) plane. If the surface density of atoms on this plane is  $5.4 \times 10^{14}$  atoms/cm<sup>2</sup>, calculate  $a$ .
- (12 Marks)

Note: Question No. 1 continues on page 2.

- (b) Figure 1 shows the thermal equilibrium energy band diagram of a uniformly doped semiconductor at 350 K. The intrinsic carrier concentration is  $3.3 \times 10^{14} \text{ cm}^{-3}$  at this temperature.



**Figure 1**

- (i) Determine the doping type and density.
- (ii) Additional doping is added and as a result, the Fermi level is shifted to 0.35 eV above the valence band edge  $E_V$ . What is the doping type and density required to achieve that?
- (iii) A voltage of 0.5 V is applied across the semiconductor, with the positive terminal of the voltage source connected to the left end. Sketch and label the energy band diagram under this condition.

(13 Marks)

2. (a) A p-type semiconductor bar of length  $L = 30 \text{ } \mu\text{m}$  has non-uniform doping concentration  $N_A$  that varies with distance  $x$  according to

$$N_A(x) = N_{A0} \exp\left(-\frac{x}{d}\right) \text{ cm}^{-3},$$

where  $0 \leq x \leq L$ ,  $N_{A0} = 2.6 \times 10^{16} \text{ cm}^{-3}$  and  $d = 12 \text{ } \mu\text{m}$ .  $N_A(x)$  is everywhere much greater than the intrinsic carrier concentration. The mobility of the majority carriers is  $750 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at 300 K.

- (i) At thermal equilibrium, what would be the drift current density and electric field strength at the middle of the bar?
- (ii) A voltage source connected across the bar results in a total current density of  $+15 \text{ A/cm}^2$ . Determine an expression for the applied electric field.

(9 Marks)

Note: Question No. 2 continues on page 3.

- ✓ (b) A semi-infinitely long  $p$ -type semiconductor sample, doped uniformly to a concentration of  $2 \times 10^{16} \text{ cm}^{-3}$ , is injected with excess minority carriers at one end ( $x = 0$ ) at 300 K. The steady-state diffusion current density  $J_n$  at  $x = 0$  is  $-50 \text{ mA} \cdot \text{cm}^{-2}$ . The minority carriers have a lifetime of  $2 \mu\text{s}$  and a mobility of  $950 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$ . The intrinsic carrier concentration is  $1.5 \times 10^{12} \text{ cm}^{-3}$ .

- Determine the excess minority carrier concentration at  $x = 0$ .
- Is low-level injection condition valid?
- At what distance into the semiconductor would the diffusion current density become half of its value at  $x = 0$ ?

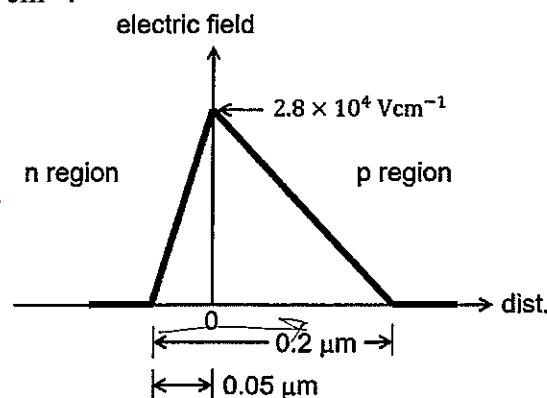
(8 Marks)

- (c) A silicon  $n$ - $p$ - $n$  bipolar junction transistor has impurity concentrations of  $3 \times 10^{18}$ ,  $5 \times 10^{16}$  and  $5 \times 10^{15} \text{ cm}^{-3}$  in the emitter, base and collector, respectively. The base width of the transistor is  $W_b = 1.0 \mu\text{m}$  and the device cross-section area is  $10^{-3} \text{ mm}^2$ . Assume that the lifetime of minority carriers in all 3 sections is  $0.1 \mu\text{s}$ , the mobility of the electrons and holes are  $\mu_n = 1250 \text{ cm}^2/\text{V} \cdot \text{s}$ , and  $\mu_p = 350 \text{ cm}^2/\text{V} \cdot \text{s}$ , respectively, and the device is operating under the forward active mode at  $T = 300 \text{ K}$ . If the base-emitter junction is biased at  $0.5 \text{ V}$ , determine:

- the minority carrier charge in the base region.
- the collector current  $I_c$ .

(8 Marks)

3. (a) Figure 2 shows the electric field profile of an abrupt uniformly doped Ge  $p$ - $n$  junction diode under thermal equilibrium at 300 K. The electron and hole lifetimes are  $2 \mu\text{s}$  and  $0.5 \mu\text{s}$ , respectively and are the same in both the  $p$  and  $n$  regions. The cross-sectional area is  $2.5 \times 10^{-4} \text{ cm}^2$  and the critical electric field is  $1.1 \times 10^5 \text{ V} \cdot \text{cm}^{-1}$ .

**Figure 2**

Note: Question No. 3 continues on page 4.

- (i) Determine the built-in voltage and the doping concentrations of the  $p$  and  $n$  regions.
- (ii) A reverse-bias voltage of 50 V is applied across the diode. Calculate the maximum electric field under this condition. Is it safe to operate the diode at this voltage? Briefly justify your answer.
- (iii) Assuming that the diode is ideal, calculate the hole drift current at the edge of the space-charge region on the  $p$ -side at a forward-bias voltage of 0.19 V.

(14 Marks)

- (b) The following table lists the work function of three metals, A, B and C.

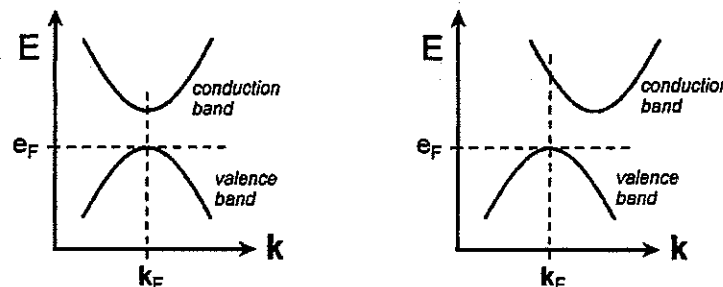
Metal	Work Function (eV)
A	2.21
B	4.10
C	4.75

- (i) What metal(s) is(are) suitable for forming a Schottky contact on an  $n$ -type Si doped uniformly to a concentration of  $5 \times 10^{16} \text{ cm}^{-3}$  at 300 K? Justify your answer.
- (ii) For one of the suitable metal(s) identified in part (b)(i), sketch a labelled energy band diagram of the contact at thermal equilibrium, indicating clearly the barriers on the metal and semiconductor sides.
- (iii) For the metal chosen in part (b)(ii), what is the junction capacitance per unit area of the contact at a reverse-bias voltage of 5 V?

(11 Marks)

4. (a) Figure 3 shows the energy band diagrams of two semiconductors in the  $E$ - $k$  space. Which one (left or right) is a direct bandgap semiconductor and which one is an indirect bandgap semiconductor? Briefly explain why it is unlikely to obtain direct electron-hole recombination in an indirect bandgap semiconductor?

(5 Marks)

**Figure 3**

Note: Question No. 4 continues on page 5.

- (b) A photodetector whose active area is  $5 \times 10^{-2} \text{ cm}^2$  is irradiated by yellow light ( $\lambda = 600 \text{ nm}$ ) with an intensity of  $2 \text{ mW/cm}^2$ . Assuming that the quantum efficiency of the detector  $\eta = 85\%$ , calculate:
- (i) The number of electron-hole pairs (EHPs) generated per second.
  - (ii) The photocurrent generated in the detector.
  - (iii) The responsivity of the photodetector.
- (9 Marks)
- (c) Consider a GaAs light emitting diode (LED). The bandgap  $E_g$  of GaAs at 300 K is 1.42 eV, which decreases with temperature as  $\frac{dE_g}{dT} = -4.5 \times 10^{-4} \text{ eV} \cdot \text{K}^{-1}$ . What would be the change in the emission wavelength if the temperature of the GaAs LED is increased by  $10^\circ \text{C}$ ?
- (7 Marks)
- (d) A  $p$ - $n$  junction photodiode can be operated under photovoltaic condition similar to a solar cell. State three major differences between a photodiode and a solar cell.
- (4 Marks)

**List of Selected Formulae**

$$\xi = \frac{1}{q} \frac{dE}{dx}, \quad E_{ph} = h\nu = \frac{hc}{\lambda}, \quad \frac{1}{m^*} = \frac{1}{\hbar^2} \frac{d^2 E}{dk^2}, \quad E_n = -\frac{q^4}{2(4\pi\hbar)^2} \left( \frac{m_n^*}{\epsilon_r^2 \epsilon_0^2} \right) \frac{1}{n^2},$$

$$f(E) = \frac{1}{1 + \exp\left[\frac{E - E_F}{k_B T}\right]}, \quad g_c(E) = \frac{4\pi (2m_n^*)^{3/2}}{h^3} \sqrt{E - E_c}, \quad g_v(E) = \frac{4\pi (2m_p^*)^{3/2}}{h^3} \sqrt{E_v - E},$$

$$n_0 = N_c \exp\left[-\frac{E_c - E_F}{k_B T}\right], \quad N_c = 2 \left( \frac{2\pi m_n^* k_B T}{h^2} \right)^{3/2},$$

$$p_0 = N_v \exp\left[-\frac{E_F - E_v}{k_B T}\right], \quad N_v = 2 \left( \frac{2\pi m_p^* k_B T}{h^2} \right)^{3/2},$$

$$p_0 + N_d = n_0 + N_a, \quad E_{thermal (3-D)} = \frac{3}{2} k_B T, \quad v_{dp} = \mu_p \xi, \quad \mu_p = \frac{q \tau_{cp}}{m_p^*},$$

$$v_{dn} = -\mu_n \xi, \quad \mu_n = \frac{q \tau_{cn}}{m_n^*}, \quad J_{p \text{ drift}} = q p \mu_p \xi, \quad J_{n \text{ drift}} = q n \mu_n \xi,$$

$$J_{\text{drift}} = J_{n \text{ drift}} + J_{p \text{ drift}} = \sigma \xi, \quad \sigma = q \mu_n n + q \mu_p p, \quad \rho = \frac{1}{\sigma}, \quad J = \frac{I}{A}, \quad \xi = \frac{V}{l},$$

$$R_R = \rho \frac{l}{A}, \quad l = v_{th} \tau_{cn}, \quad v_{th} l = D_n, \quad J_{n \text{ diff}} = q D_n \frac{dn}{dx}, \quad J_{p \text{ diff}} = -q D_p \frac{dp}{dx},$$

$$J_n = J_{n \text{ drift}} + J_{n \text{ diff}}, \quad J_p = J_{p \text{ drift}} + J_{p \text{ diff}}, \quad J_{\text{total}} = J_n + J_p,$$

$$D_n = \frac{k_B T}{q} \mu_n, \quad D_p = \frac{k_B T}{q} \mu_p$$

$$n_0 = n_i \exp\left(\frac{E_F - E_i}{k_B T}\right), \quad p_0 = n_i \exp\left(\frac{E_i - E_F}{k_B T}\right)$$

$$n_0 p_0 = n_i^2$$

**List of Selected Formulae (cont'd)**

$$R = \alpha_r n p, \quad G_{th} = \alpha_r n_i^2, \quad \tau_n = \frac{1}{\alpha_r p_0}, \quad \tau_p = \frac{1}{\alpha_r n_0}$$

$$\frac{dn}{dt} = \frac{d\Delta n}{dt} = G_L + G_{th} - R = G_L - \frac{\Delta n}{\tau_n}, \quad \Delta n_{ss} = G_L \tau_n, \quad \Delta n(t) = \Delta n(t=0) \exp\left(-\frac{t}{\tau_n}\right)$$

$$\frac{\partial n(x,t)}{\partial t} = \frac{1}{q} \frac{\partial J_n(x,t)}{\partial x} + G_L - \frac{\Delta n}{\tau_n}, \quad \Delta n(x) = \Delta n(x=0) \exp\left(-\frac{x}{L_n}\right), \quad L_n = \sqrt{D_n \tau_n}$$

$$\frac{dp}{dt} = \frac{d\Delta p}{dt} = G_L + G_{th} - R = G_L - \frac{\Delta p}{\tau_p}, \quad \Delta p_{ss} = G_L \tau_p, \quad \Delta p(t) = \Delta p(t=0) \exp\left(-\frac{t}{\tau_p}\right)$$

$$\frac{\partial p(x,t)}{\partial t} = -\frac{1}{q} \frac{\partial J_p(x,t)}{\partial x} + G_L - \frac{\Delta p}{\tau_p}, \quad \Delta p(x) = \Delta p(x=0) \exp\left(-\frac{x}{L_p}\right), \quad L_p = \sqrt{D_p \tau_p}$$

$$\frac{d^2 V(x)}{dx^2} = -\frac{d\xi(x)}{dx} = -\frac{\rho_c}{\epsilon_r \epsilon_0} = -\frac{q}{\epsilon_r \epsilon_0} (p - n + N_d - N_a)$$

$$V_{bi} = \frac{kT}{q} \ln\left(\frac{p_{p0}}{p_{n0}}\right) = \frac{kT}{q} \ln\left(\frac{N_a N_d}{n_i^2}\right), \quad \frac{p_{p0}}{p_{n0}} = \frac{n_{n0}}{n_{p0}} = \exp\left(\frac{qV_{bi}}{kT}\right)$$

$$N_d x_n = N_a x_p, \quad \xi_{max} = -\frac{qN_d x_n}{\epsilon_r \epsilon_0} = -\frac{qN_a x_p}{\epsilon_r \epsilon_0}, \quad W = \left[ \frac{2\epsilon_r \epsilon_0 (V_{bi} - V_a)}{q} \left( \frac{1}{N_a} + \frac{1}{N_d} \right) \right]^{1/2}$$

$$\frac{p_{p0}}{p_n(x_n)} = \frac{n_{n0}}{n_p(-x_p)} = \exp\left[\frac{q}{kT}(V_{bi} - V_a)\right], \quad \frac{p_n(x_n)}{p_{n0}} = \frac{n_p(-x_p)}{n_{p0}} = \exp\left(\frac{qV_a}{kT}\right)$$

$$\Delta n_p(x) = \Delta n_p(-x_p) \exp\left(-\frac{x}{L_n}\right) = n_{p0} \left[ \exp\left(\frac{qV_a}{kT}\right) - 1 \right] \exp\left(-\frac{x}{L_n}\right)$$

$$\Delta p_n(x) = \Delta p_n(x_n) \exp\left(-\frac{x}{L_p}\right) = p_{n0} \left[ \exp\left(\frac{qV_a}{kT}\right) - 1 \right] \exp\left(-\frac{x}{L_p}\right)$$

$$I = I_0 \left[ \exp\left(\frac{qV_a}{kT}\right) - 1 \right], \quad I_0 = qA \left( \frac{D_p}{L_p} p_{n0} + \frac{D_n}{L_n} n_{p0} \right), \quad C_j = \left| \frac{dQ_j}{dV_a} \right| = \frac{\epsilon_r \epsilon_0 A}{W}$$

$$C_s = \left| \frac{dQ_n}{dV_a} \right| = \frac{q}{kT} |Q_n| = \frac{q}{kT} I \tau_n \text{ (n}^+ \text{p diode)}, \quad C_s = \frac{dQ_p}{dV_a} = \frac{q}{kT} Q_p = \frac{q}{kT} I \tau_p \text{ (p}^+ \text{n diode)}$$

$$Q_n = -qAL_n \Delta n_p, \quad Q_p = qAL_p \Delta p_n$$

**List of Selected Formulae (cont'd)**

$$I(x) = I_0 \exp(-\alpha x), \quad G = R_1 R_2 \exp(2(k - \gamma)L), \quad k_{th} = \gamma + \frac{1}{2L} \ln \left( \frac{1}{R_1 R_2} \right)$$

$$\frac{n\lambda}{2} = L, \quad f = \frac{nc}{2L}, \quad \Delta f = \frac{\Delta nc}{2L}, \quad \frac{hc}{\lambda} = E_{ph}$$

$$\text{Reflectivity, } r = \left( \frac{n_1 - n_2}{n_1 + n_2} \right)^2, \quad I_t = (1 - r) I_o, \quad I = RP, \quad R = \eta \frac{e}{E_{ph}}, \quad \eta = \frac{N_e}{N_p}$$

$$i_C = \frac{-e D_n A_{BE}}{x_B} \times n_{B0} \exp \left( \frac{e V_{BE}}{kT} \right), \quad \frac{i_C}{i_E} \equiv \alpha, \quad \frac{i_C}{i_B} \equiv \beta, \quad \frac{1}{\alpha} = \frac{1}{\beta} + 1,$$

$$V_B + I \times R_L + V = 0$$



**Table of Physical Constants**

	Symbol	Value	Unit
Planck's constant	$h$	$6.626 \times 10^{-34}$	J-s
Speed of light	$c$	$3.0 \times 10^8$	m/s
Electronic charge	$e$ (or $q$ )	$1.6 \times 10^{-19}$	C
Boltzmann's constant	$k_B$ (or $k$ )	$1.38 \times 10^{-23}$	J/K
Free electron rest mass	$m_0$	$9.1 \times 10^{-31}$	kg
Proton rest mass	$m_p$	$1.67 \times 10^{-27}$	kg
Avogadro's number	$N_A$	$6.02 \times 10^{23}$	mol <sup>-1</sup>
Permeability of free space	$\mu_0$	$4\pi \times 10^{-7}$	H/m
Permittivity of free space	$\epsilon_0$	$8.85 \times 10^{-12}$	F/m
Rydberg constant	$R_d$	$1.097 \times 10^7$	m <sup>-1</sup>
Bohr radius	$a_0$	$5.292 \times 10^{-11}$	m
Gas constant	$R$	8.31	Jmol <sup>-1</sup> K <sup>-1</sup>
Electron-volt	1 eV	$1.6 \times 10^{-19}$	J
Thermal voltage ( $T = 300$ K)	$k_B T/q$	0.0259	V

**Properties of Silicon, Gallium Arsenide, and Germanium ( $T = 300$  K)**

Property	Si	GaAs	Ge
Atomic density ( $\text{cm}^{-3}$ )	$5.00 \times 10^{22}$	$4.42 \times 10^{22}$	$4.42 \times 10^{22}$
Atomic weight	28.09	144.63	72.60
Crystal structure	Diamond	Zincblende	Diamond
Density ( $\text{g/cm}^3$ )	2.33	5.32	5.33
Lattice constant ( $\text{\AA}$ )	5.43	5.65	5.65
Melting point ( $^{\circ}\text{C}$ )	1415	1238	937
Dielectric constant	Si: 11.7 SiO <sub>2</sub> : 3.8	13.1	16.0
Bandgap energy (eV)	1.12	1.42	0.66
Electron affinity (V)	4.01	4.07	4.13
Effective density of states in conduction band, $N_c$ ( $\text{cm}^{-3}$ )	$2.8 \times 10^{19}$	$4.7 \times 10^{17}$	$1.04 \times 10^{19}$
Effective density of states in valence band, $N_v$ ( $\text{cm}^{-3}$ )	$1.04 \times 10^{19}$	$7.0 \times 10^{18}$	$6.0 \times 10^{18}$
Intrinsic carrier concentration ( $\text{cm}^{-3}$ )	$1.5 \times 10^{10}$	$1.8 \times 10^6$	$2.4 \times 10^{13}$
Mobility ( $\text{cm}^2/\text{V-s}$ ) Electron, $\mu_n$ Hole, $\mu_p$	1350 480	8500 400	3900 1900

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EE2003 PYP Solution

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No.

1a. i) Distance between atom A & B =  $\sqrt{\left(\frac{a}{4}\right)^2 + \left(\frac{a}{4}\right)^2 + \left(\frac{a}{4}\right)^2} = \frac{a}{4}\sqrt{3}$

$r_B = 0.75 r_A$

$\frac{a}{4}\sqrt{3} = r_A + r_B$

$= 1.75 r_A$

$r = r_A = 0.247 a$

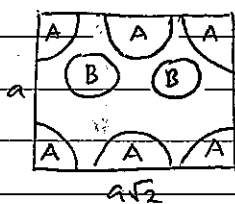
ii) % volume occupied =  $\frac{4 \left(\frac{4}{3}\pi r_A^3\right) + 4 \left(\frac{4}{3}\pi r_B^3\right)}{a^3}$

$= 4 \left(\frac{4}{3}\pi\right) (0.247)^3 + 4 \left(\frac{4}{3}\pi\right) (0.247)^3 (0.75)^3$

$= 0.3609$

$= 36.09\%$

iii)



(110) plane

Surface density =  $\frac{\text{no. of atoms}}{\text{area}}$

$5.4 \times 10^{14} = \frac{4}{a^2\sqrt{2}}$

$a = 7.237 \text{ \AA}$

1b.  $T = 350 \text{ K}$

$n_i = 3.3 \times 10^{14} / \text{cm}^3$

i)  $E_F$  is closer to  $E_c$  : n-type.

$N_D \approx n_0 = n_i \exp\left(\frac{E_F - E_i}{k_B T}\right) = 3.3 \times 10^{14} \exp\left(\frac{\left(\frac{0.91}{2} - 0.4\right) \times 1.6 \times 10^{-19}}{(1.38 \times 10^{-23})(350)}\right)$

$N_D = 2.04 \times 10^{15} / \text{cm}^3$

ii)  $E_F$  is closer to  $E_v$  : p-type.

$p_0 = n_i \exp\left(\frac{E_i - E_F}{k_B T}\right) = 3.3 \times 10^{14} \exp\left(\frac{\left(\frac{0.91}{2} - 0.35\right) \times 1.6 \times 10^{-19}}{(1.38 \times 10^{-23})(350)}\right)$

$p_0 = 1.07 \times 10^{16} / \text{cm}^3$

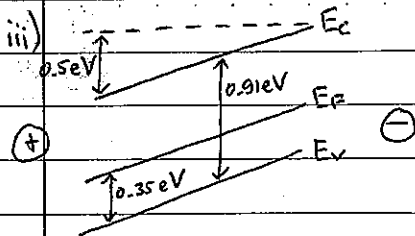
$p_0 + N_D = n_0 + N_A$

$N_A \approx p_0 + N_D = 1.27 \times 10^{16} / \text{cm}^3$



Date

No.



2 a.

$$L = 30 \mu\text{m}$$

$$d = 12 \mu\text{m}$$

$$N_A(x) = N_{A0} \exp\left(-\frac{x}{d}\right) \text{ cm}^{-3}$$

$$\mu_p = 750 \text{ cm}^2/\text{V}\cdot\text{s}$$

$$T = 300 \text{ K}$$

$$N_{A0} = 2.6 \times 10^{16} / \text{cm}^3$$

i) At thermal equilibrium,  $J_p = J_{p\text{drift}} + J_{p\text{diff}} = 0$ .

$$J_{p\text{drift}} = -J_{p\text{diff}} = q D_p \frac{dp}{dx}$$

$$D_p = \frac{k_B T}{q} \mu_p = 0.0259 (750) = 19.425$$

$$\frac{dp}{dx} = \frac{dN_A(x)}{dx} = -\frac{N_{A0}}{d} \exp\left(-\frac{x}{d}\right)$$

$$J_{p\text{drift}}(x = 15 \mu\text{m}) = q D_p \frac{dN_A(x=15 \mu\text{m})}{dx}$$

$$= (1.6 \times 10^{-19}) (19.425) \left( \frac{-2.6 \times 10^{16}}{12 \times 10^{-4}} \exp\left(-\frac{15 \times 10^{-4}}{12 \times 10^{-4}}\right) \right)$$

$$= \boxed{-19.293 \text{ A/cm}^2}$$

$$\xi(x) = \frac{J_{p\text{drift}}(x)}{q N_A(x) \mu_p} = \frac{-19.293}{(1.6 \times 10^{-19}) (2.6 \times 10^{16}) \left( \exp\left(-\frac{15 \times 10^{-4}}{12 \times 10^{-4}}\right) \right) (750)}$$

$$= \boxed{-21.583 \text{ V/cm}}$$

ii)  $J_p = J_{p\text{drift}} + J_{p\text{diff}} = 15 \text{ A/cm}^2$

As derived in part (i),  $J_{p\text{diff}} = -q D_p N_{A0} \frac{\exp(-x/d)}{d}$

$$\xi(x) = \frac{J_{p\text{drift}}}{q N_A \mu_p} = \frac{15 + \frac{q D_p N_{A0}}{d} \exp\left(-\frac{x}{d}\right)}{q \mu_p (N_{A0} \exp(-x/d))}$$

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$$\xi(x) = \frac{15}{q \mu_p N_{A0} \exp(-\frac{x}{d})} + \frac{k_B T}{q} \frac{1}{d}$$

$$= \frac{15}{(1.6 \times 10^{-19})(750)(2.6 \times 10^{16})} \exp\left(\frac{x}{d}\right) + \frac{0.0259}{12 \times 10^{-4}}$$

$$\xi(x) = 4.808 \exp\left(\frac{x}{d}\right) + 21.583 \text{ V/cm}; d = 12 \mu\text{m}$$

b.  $N_A = 2 \times 10^{16} / \text{cm}^3$   $\tau_n = 2 \mu\text{s}$   $n_i = 1.5 \times 10^{12} / \text{cm}^3$

$J_{\text{diff}}(x=0) = -50 \text{ mA/cm}^2$   $\mu_n = 950 \text{ cm}^2/\text{V}\cdot\text{s}$   $T = 300 \text{ K}$

i)  $L_n = \sqrt{D_n \tau_n} = \sqrt{\frac{k_B T}{q} \frac{\mu_n \tau_n}{q}} = \sqrt{(0.0259)(950)(2 \times 10^{-6})} = 7.015 \times 10^{-3}$

$$\Delta n(x) = \Delta n(x=0) \exp\left(-\frac{x}{L_n}\right)$$

$$\frac{d\Delta n(x)}{dx} = \frac{-\Delta n(x=0)}{L_n} \exp\left(-\frac{x}{L_n}\right)$$

$$J_{\text{diff}}(x) = q D_n \frac{d\Delta n(x)}{dx}$$

$$D_n = \frac{k_B T}{q} \mu_n = (0.0259)(950) = 24.605$$

At  $x=0$ ,  $J_{\text{diff}} = -50 \times 10^{-3}$

$$\frac{d\Delta n(x)}{dx} = \frac{-\Delta n(x=0)}{7.015 \times 10^{-3}} \exp\left(-\frac{x}{L_n}\right)$$

$$\Delta n(x=0) = \frac{-J_{\text{diff}}(x=0)}{q D_n} (7.015 \times 10^{-3})$$

$$= \frac{(50 \times 10^{-3})(7.015 \times 10^{-3})}{(1.6 \times 10^{-19})(24.605)}$$

$$= 1.270 \times 10^{15} / \text{cm}^3$$

ii)  $\Delta n(x=0) = 1.27 \times 10^{15} > 0.1 N_A = 2 \times 10^{15}$

Hence, low-level injection condition is not valid.

iii)  $J_{\text{diff}}(x') = 0.5 J_{\text{diff}}(x=0) = -25 \text{ mA/cm}^2$

$$\frac{-\Delta n(x=0)}{L_n} \exp\left(-\frac{x'}{L_n}\right) q D_n = -25 \times 10^{-3}$$

$$x' = -L_n \ln\left(\frac{25 \times 10^{-3} L_n}{q D_n \Delta n(x=0)}\right) = -(7.015 \times 10^{-3}) \ln\left(\frac{25 \times 10^{-3} (7.015 \times 10^{-3})}{(1.6 \times 10^{-19})(24.605)(1.27 \times 10^{15})}\right)$$



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$$x' = 0.088 \text{ cm}$$

2c.  $N_{d, \text{emitter}} = 3 \times 10^{18} / \text{cm}^3$   $W_b = 1 \text{ mm}$   $\mu_n = 1250 \text{ cm}^2/\text{V}\cdot\text{s}$   $T = 300 \text{ K}$   
 $N_{a, \text{base}} = 5 \times 10^{16} / \text{cm}^3$   $A = 10^{-3} \text{ mm}^2$   $\mu_p = 350 \text{ cm}^2/\text{V}\cdot\text{s}$   
 $N_{d, \text{collector}} = 5 \times 10^{15} / \text{cm}^3$   $\tau_p = \tau_n = 0.1 \mu\text{s}$   $V_{be} = 0.5 \text{ V}$

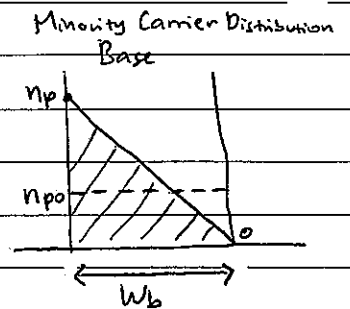
i)  $V_{bi} \text{ (between emitter and base)} = \frac{kT}{q} \ln \left( \frac{N_{a, \text{base}} \cdot N_{d, \text{emitter}}}{n_i^2} \right)$   
 $= 0.0259 \ln \left( \frac{5 \times 10^{16} \times 3 \times 10^{18}}{(1.5 \times 10^{10})^2} \right)$

$$= 0.884 \text{ V}$$

$$n_p = n_{p0} \exp \left( \frac{q}{kT} (V_{bi} - V_a) \right); \quad n_{p0} = \frac{n_i^2}{N_{a, \text{base}}}$$

$$= \frac{(1.5 \times 10^{10})^2}{5 \times 10^{16}} \exp \left( \frac{0.884 - 0.5}{0.0259} \right)$$

$$= 1.239 \times 10^{10} / \text{cm}^3$$



Minority carrier charge in base region  $= q \cdot \frac{n_p \cdot W_b}{2} \cdot A$

$$= \frac{(1.6 \times 10^{-19}) (1.239 \times 10^{10}) (1 \times 10^{-4}) (10^{-7})}{2}$$

$$= 9.912 \times 10^{-21} \text{ C}$$

ii)  $I_c = \frac{-e D_n A_{BE}}{x_B} n_{p0} \exp \left( \frac{e V_{BE}}{kT} \right)$   
 $= \frac{-(1.6 \times 10^{-19}) (0.0259) (1250) (10^{-7})}{1 \times 10^{-4}} \frac{(1.5 \times 10^{10})^2}{5 \times 10^{16}} \exp \left( \frac{0.5}{0.0259} \right)$

$$I_c = -5.64 \text{ nA}$$

3a.  $\tau_n = 2 \mu\text{s}$   $A = 2.5 \times 10^{-4} \text{ cm}^2$   $T = 300 \text{ K}$   
 $\tau_p = 0.5 \mu\text{s}$   $E_{\text{critical}} = 1.1 \times 10^5 \text{ V/cm}$

i)  $V_{bi} = \text{area under } E-x \text{ graph} = \frac{1}{2} \times 2.8 \times 10^4 \times 0.2 \times 10^{-4} = 0.28 \text{ V}$

$$N_d x_n = N_a x_p$$

$$\frac{N_d}{N_a} = \frac{0.15}{0.05} = \frac{3}{1}$$



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$$V_{bi} = \frac{kT}{q} \ln \left( \frac{N_A N_D}{n_i^2} \right) \rightarrow N_A N_D = \exp \left( \frac{V_{bi}}{\frac{kT}{q}} \right) \cdot n_i^2$$

$$N_A (3N_A) = \exp \left( \frac{0.28}{0.0259} \right) \times (2.4 \times 10^{13})^2$$

$$N_A = 3.085 \times 10^{15} / \text{cm}^3$$

$$N_D = 3N_A = 9.254 \times 10^{15} / \text{cm}^3$$

$$\begin{aligned} \text{ii) } W &= \left[ \frac{2 \epsilon_r \epsilon_0 (V_{bi} - V_a)}{q} \left( \frac{1}{N_A} + \frac{1}{N_D} \right) \right]^{1/2} \\ &= \left[ \frac{2 \times 16 \times 8.85 \times 10^{-14} (0.28 + 50)}{1.6 \times 10^{-19}} \left( \frac{1}{3.085 \times 10^{15}} + \frac{1}{9.254 \times 10^{15}} \right) \right]^{1/2} \\ &= 6.202 \text{ } \mu\text{m} \end{aligned}$$

$$\frac{N_D}{N_A} = \frac{x_p}{x_n} = \frac{3}{1}$$

$$x_n = \frac{1}{3} W = 1.551 \text{ } \mu\text{m}$$

$$E_{\text{max}} = \frac{q N_A x_n}{\epsilon_r \epsilon_0} = \frac{(1.6 \times 10^{-19})(9.254 \times 10^{15})(1.551 \times 10^{-4})}{16 \times 8.85 \times 10^{-14}} = 162.128 \text{ kV/cm}$$

As  $E_{\text{max}} = 1.6 \times 10^5 > E_{\text{critical}} = 1.1 \times 10^5$ , it is not safe to operate at this voltage.  
The diode will experience breakdown.

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3b. i) Schottky contact :  $q\phi_m > q\phi_s$

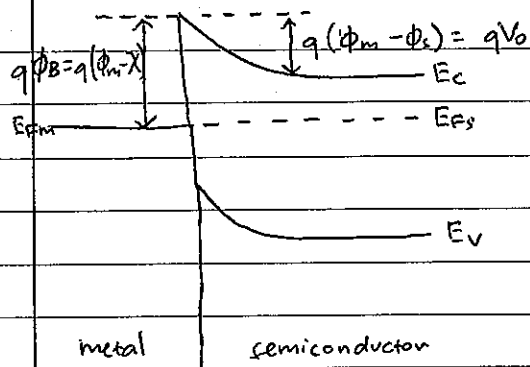
For  $N_b = 5 \times 10^{16} / \text{cm}^3$ ,

$$E_c - E_F = \frac{-k_B T \ln \left( \frac{N_b}{N_c} \right)}{q} = \frac{-(1.38 \times 10^{-23})(300) \ln \left( \frac{5 \times 10^{16}}{2.8 \times 10^{19}} \right)}{1.6 \times 10^{-19}} = 0.164 \text{ eV}$$

$$q\phi_s = q\chi + E_c - E_F = 4.01 + 0.164 = 4.174 \text{ eV}$$

Metal C is suitable since  $q\phi_m$  metal C is higher than 4.174 eV.

ii)



$$\text{iii) } W = \left[ \frac{2 \epsilon_r \epsilon_0 (V_{bi} - V_a)}{q} \left( \frac{1}{N_a} + \frac{1}{N_d} \right) \right]^{1/2} ; N_a \gg N_d$$

$$W = \left[ \frac{2 (11.7) (8.85 \times 10^{-14}) (4.75 - 4.174 + 5)}{(1.6 \times 10^{-19}) (5 \times 10^{16})} \right]^{1/2} = 0.380 \text{ } \mu\text{m}$$

$$\frac{C_j}{A} = \frac{\epsilon_r \epsilon_0}{W} = \frac{11.7 \times 8.85 \times 10^{-14}}{0.38 \times 10^{-4}} = \boxed{2.725 \times 10^{-8} \text{ F/cm}^2}$$

4a. Direct bandgap semiconductor : left figure

Indirect bandgap semiconductor : right figure

In an indirect bandgap semiconductor, more energy is needed for electron-hole recombination.

$$4b. A = 5 \times 10^{-2} \text{ cm}^2 \quad I = 2 \text{ mW/cm}^2$$

$$\lambda = 600 \text{ nm} \quad \eta = 85\%$$

$$\text{i) } E_{ph} = N \cdot \frac{hc}{\lambda}$$

$$N = \frac{I \cdot A \cdot \lambda}{h \cdot c} = \frac{2 \times 10^{-3} \times 5 \times 10^{-2} \times 600 \times 10^{-9}}{(6.626 \times 10^{-34}) (3 \times 10^8)} = \boxed{3.018 \times 10^{14} \text{ EHP/s}}$$





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$$ii) I = RP = \eta \frac{e}{E_{ph}} \cdot I \cdot A ; E_{ph} = \frac{1240}{\lambda(\text{nm})} \quad (\text{in eV})$$

$$I = 0.85 \times \frac{600}{1240} \times 2 \times 10^{-3} \times 5 \times 10^{-2} = \boxed{41.13 \text{ } \mu\text{A}}$$

$$iii) R = \frac{\eta e}{E_{ph}} = 0.85 \times \frac{600}{1240} = \boxed{0.411}$$

$$4c. \frac{dE_g}{dT} = -4.5 \times 10^{-4} \text{ eV/K}$$

$$E_{g1} = 1.42 \text{ eV at } T_1 = 300 \text{ K}$$

$$\text{For } T_2 = 310 \text{ K, } E_{g2} = E_{g1} + \frac{dE_g}{dT} \cdot \Delta T$$

$$= 1.42 - 4.5 \times 10^{-4} \times 10$$

$$= 1.4155 \text{ eV}$$

$$\lambda_1 = \frac{1240}{E_{g1}} = \frac{1240}{1.42} = 873.24 \text{ nm}$$

$$\lambda_2 = \frac{1240}{E_{g2}} = \frac{1240}{1.4155} = 876.02 \text{ nm}$$

$$\Delta\lambda = \lambda_2 - \lambda_1 = \boxed{2.78 \text{ nm}}$$

4d. Refer to lecture notes.

All the best for your exams!



No.