

$$\begin{array}{c}
\frac{}{\rho \vdash x : \text{int}} \text{P1} \quad \frac{}{\rho \vdash 10 : \text{int}} \text{P1} \quad \frac{\rho(f) = t_x \rightarrow \text{int}}{\rho \vdash f : t_x \rightarrow \text{int}} \text{P3} \quad \frac{}{\rho \vdash x : \text{int}} \text{P1} \quad \frac{}{\rho \vdash 1 : \text{int}} \text{P1} \\
\frac{}{\rho \vdash x < 10 : \text{bool}} \text{P5} \quad \frac{}{\rho \vdash 42 : \text{int}} \text{P1} \quad \frac{}{\rho \vdash x + 1 : \text{int}} \text{P4} \\
\frac{}{\rho \vdash f(x+1) : \text{int}} \text{P7} \quad \frac{}{\rho \vdash f : [t_x/\alpha]t_x \rightarrow \text{int}} \text{P3} \quad \frac{}{\rho \vdash 20 : \text{int}} \text{P1} \\
\frac{\rho[x \mapsto t_x, f \mapsto t_x \rightarrow \text{int}] \vdash \text{if } x < 10 \text{ then } 42 \text{ else } f(x+1) : \text{int}}{\rho \vdash \text{let } f \text{ } x = \text{if } x < 10 \text{ then } 42 \text{ else } f(x+1) \text{ in } f \text{ } 20 \text{ end} : \text{int}} \text{P8}
\end{array}$$