1.1 -Introduction to Polynomial Functions

A **polynomial function** is a series of terms where each term is the product of a constant and power of x. It has the form: $f(x) = a_v x^n + a_{s-1} x^{n-1} + a_{n-2} x^{n-2} + ... a_3 x^3 + a_2 x^2 + a_1 x + a_0$ where 'a' is a constant and 'n' is a nonnegative integer.

Example

EX 1 - Identify the following as polynomial functions or not.

a) $f(x) = 2x^3$ Polynomial	b) $g(x) = \sin x + 5$ No-> Sizusodial	c) $h(x) = 4^x + x + 1$
d) $y = x^4 + 6x^2 - x$ $polyna_{bal} d$	e) $j(x) = \frac{-6}{x} + 5x + 2$	$k(x) = \frac{x^2}{3} + 1$ $\rho_{olynomial}$

A **power function** (simplest form of a polynomial function) has the form $y = ax^n$. Where 'a' is a constant and 'n' is a nonnegative integer.

EX 2 - State the type of each of the following power functions:

a) $y=a$	b) $y = ax$	c) $y = ax^2$
Constant power	linear power	Quadratic
d) $y = ax^3$ $Cubic$	e) $y = ax^4$ Quartic	

Polynomial functions have the following characteristics:

Degree: n - exponent of the greatest power of x

Leading Coefficient: ^a_n - the coefficient of the greatest power of x
* Polynomial functions are typically written in descending powers of x

EX 3 – State the degree and leading coefficient of the following polynomials:

Polynomial Functions	Degree	Leading Coefficient
a) $f(x) = 13x^6 - 2x^2 + 14$	6	15
b) $f(x) = -\frac{1}{2}x^3 + 8x + 1$	3	- 12
c) $f(x) = 2x^3 - 5x^8 - 14$	8	- S
d) $f(x) = \frac{3x}{2} + 9$	1	3/2

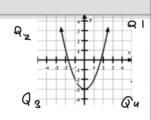
End behaviour describes what happens to the y-values of a function as the x-values get very large or

GUYATT MHF4U Unit 1: Page 2

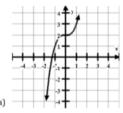
very small for a polynomial function.

End behaviour can be described in two ways:

2) graph extends from: Q 3 to Q 1



EX 4 - State the end behaviour (in two ways) of the following functions:



b)

. 93 to Q1

. 93 to Q4

· X -> -> , Y -> -> 00

· y-> 00, y -> - 20

Interval Notation

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Notes

• Polynomial function: An expression containing variable (x, a, y) raised to a series of positive whole nu exponents.

Librereral form: anx" + a(n-1) x(n-1) + a(n-2))

ex ponents decrease

Lo Degrees: The highest power present in a po

L> Ex: Sx-2x+7=0

2nd degree polynomial
"Quadratic polynomial"

Ex: 3x + 2x² - 7 = 0

3rd degree polynomial
"Cubic polynomial"

4th degree = quartic 5th degree = quintic

-> Side Nate: not all terms must be present

Ex: 4 x² +7=0 = 2 ad degree polynomial

L> End behaviour:

a mber

... a₁x + a₀

ynomial is called a degree.

Interval Notation

Recall:

The *domain* of a function is the set of all values of the independent variable (ie:)

The range of a function is the set of all values of the dependent variable (ie: ,)

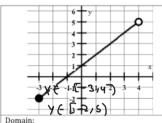
These sets can be described in:

· Set notation: OR interval notation:

Interval Notation

- · Square brackets show the end value is in the interval
- Round brackets show the end value is not in the interval
- · Intervals that are infinite use the symbols: (infinity) or (negative infinity)
- · Round brackets are always used at infinity

EX 6 - For the following functions, state the domain and range using interval notation



Range:

Range:

Definitions:

A $\pmb{\textit{Local Minimum}}$ is a point with the smallest v-value on some interval close to that point

A *Local Maximum* is a point with the largest y-value on some interval close to that point

Global Maxima/Minima are the <u>absolute</u> max or min points of the function (and are also considered local maxima/minima)

Turning Points are $\underline{\text{all}}$ local maxima/minima points

EX 7 - Label the above key features on the graph to the right:

Practice

Questions

1. Identify whether each of the following are polynomials or not:

- a) $f(x) = \cos x$
 - No

- b) $g(x) = 8^x + 2$
 - No
- $h(x) = \frac{1}{2}x^{3} + x^{2} + 1$ $\frac{\text{polynomia}}{\text{f)}}$ $k(x) = x^{2} + \frac{4}{x}$

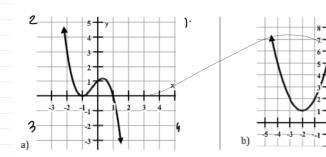
- d) $y = 2x^6$
 - polynomial
- e) $j(x) = x^{-3}$
 - ho

hο

2. State the degree and leading coefficient of the following polynomials:

Polynomial Functions	Degree	Leading Coefficient	
$f(x) = 5x^4 - 3x^3 + 4$	ч	S	
$f(x) = -\frac{x}{4} + 1$	1	- 3	
f(x) = x + 2	1	1	
$f(x) = 3x^2 + 15x^8 + 7$	8	۱۶	
f(x)=1	Q	1	





- · 92 to 94
- γ→∞, γ→ ∞ γ→ο, γ→ ∞
- . Q2 to Q1
- ×->- о, у-эф
- 5. State the domain and range in set notation and interval notation

Graph:	7 - y 6 - 5 - 4 - 3 - 2 - 1 - 1 2 3 4 5 - 2 - 1 - 1 2 3 4 5	7 y 6 6 5 4 4 3 2 2 1 1 1 2 3 4 4 5 5 6 6 6 7 5 7 7 7 7 7 7 7 7 7 7 7 7 7
Set Notation	Domain: EXER X = 23	Domain: {xekl X 7 -3}
	Range: S YERL V2 03	
	Range: { YER Y> 0 }	2/EKI//03
Interval Notation	Domain: x (-\omega , 2]	Domain: X ∈ (3, ∞)
	Domain:	Range: y ∈ (o, ∞)
Equation:	?	?
Set Notation	Domain:	Domain:
	Range:	Range:
Interval Notation	Domain:	Domain:
	Range:	Range:

