

# CS 7910 Computational Complexity

## Final Exam

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1. What is  $NP$ ? What is  $NP - Complete$ ?

$NP$  stands for Non-Deterministic Polynomial.  $NP$  is the set of all problems for which algorithms run in polynomial time on a non-deterministic machine. This machine can be thought of one that can take all possible paths in parallel. On a real machine with finite resources, all  $NP$  algorithms will not run in polynomial time (unless if  $P = NP$ , which is highly unlikely). The set of problems for which algorithms run in polynomial time is called  $P$  and  $P \subseteq NP$ . Another property of  $NP$  algorithms is that even though they cannot all run in polynomial time, given a certificate that is a solution to an  $NP$  problem, it can be verified in polynomial time that the certificate is correct.

$NP - Complete$  is the set of the hardest problems in  $NP$ . All  $NP$  problems can be reduced to  $NP - Complete$  problems in polynomial time. Actually if an  $NP$  problem can be reduced to another problem, then the resulting problem is said to be in the set  $NP - Hard$ . The intersection of the sets  $NP$  and  $NP - Hard$  is the set  $NP - Complete$ .