

CS2700 Homework 1

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Question 1.

2.2 Consider two different machines, with two different instruction sets, both of which have a clock rate of 200 MHz. The following measurements are recorded on the two machines running a given set of benchmark programs:

Instruction Type	Instruction Count (millions)	Cycles Per Instruction
Machine A		
Arithmetic and logic	8	1
Load and store	4	3
Branch	2	4
Others	4	3
Machine B		
Arithmetic and logic	10	1
Load and store	8	2
Branch	2	4
Others	4	3

- (a) Determine the effective CPI, MIPS rate, and execution time for each machine.

Solution:

$$CPI_A = \frac{\sum CPI_i * I_i}{I_c} = \frac{(8 * 1 + 4 * 3 + 2 * 4 + 4 * 3) * 10^6}{(8 + 4 + 2 + 4) * 10^6} = 2.2\overline{2}$$

$$MIPS_A = \frac{f}{CPI_A * 10^6} = \frac{200 * 10^6}{2.22 * 10^6} = 90$$

$$CPU_A = \frac{I_c * CPI_A}{f} = \frac{18 * 10^6 * 2.2}{200 * 10^6} = .2 \text{ seconds}$$

$$CPI_B = \frac{\sum CPI_i * I_i}{I_c} = \frac{(10 * 1 + 8 * 2 + 2 * 4 + 4 * 3) * 10^6}{(10 + 8 + 2 + 4) * 10^6} = 1.91\overline{6}$$

$$MIPS_B = \frac{f}{CPI_B * 10^6} = \frac{200 * 10^6}{1.92 * 10^6} = 104$$

$$CPU_B = \frac{I_c * CPI_B}{f} = \frac{24 * 10^6 * 1.92}{200 * 10^6} = .23 \text{ seconds}$$

(b) Comment on the results.

Solution:

Machine B takes more CPU time to finish its benchmark even though it has a higher MIPS than Machine A

Question 2.

2.5 The following table, based on data reported in the literature [HEAT84], shows the execution times, in seconds, for five different benchmark programs on three machines.

Benchmark	Processor		
	R	M	Z
E	417	244	134
F	83	70	70
H	66	153	135
I	39449	35527	66000
K	771	368	369

(a) Compute the speed metric for each processor for each benchmark, normalized to machine R. That is, the ratio values for R are all 1.0. Other ratios are calculated using Equation (2.5) with R treated as the reference system. Then compute the arithmetic mean value for each system using Equation (2.3). This is the approach taken in [HEAT84].

Solution:

$$\text{Arithmetic Mean} = \frac{1}{n} \sum_{i=1}^n x_i$$

Normal to R

	R	M	Z
E	$417/417 = 1$	$417/244 = 1.71$	$417/134 = 3.11$
F	$83/83 = 1$	$83/70 = 1.186$	$80/70 = 1.186$
H	$66/66 = 1$	$66/153 = .431$	$66/135 = .488$
I	$39449/39449 = 1$	$39449/35527 = 1.11$	$39449/66000 = .598$
K	$772/772 = 1$	$772/368 = 2.098$	$772/369 = 2.092$
AM	$\frac{(1 * 5)}{5} = 1$	$\frac{1.71 + 1.186 + .431 + 1.11 + 2.098}{5} = 1.307$	$\frac{3.11 + 1.186 + .488 + .598 + 2.092}{5} = 1.4948$

- (b) Repeat part (a) using M as the reference machine. This calculation was not tried in [HEAT84].

Solution:

	R	M	Z
E	.585	1	1.821
F	.843	1	1
H	2.318	1	1.133
I	.899	1	.538
K	.477	1	.997
AM	1.0244	1	1.0978

- (c) Which machine is the slowest based on each of the preceding two calculations?

Solution: Z is slowest in both

- (d) Repeat the calculations of parts (a) and (b) using the geometric mean, defined in Equation (2.6). Which machine is the slowest based on the two calculations?

Solution:

$$\text{Geometric Mean (GM)} = e^{\frac{1}{n} \sum_{i=1}^n \ln(x_i)}$$

Normal R

$$GM_R = e^{1/5 * (\ln(1)) * 5} = 1$$

$$GM_M = e^{1/5 * (\ln(1.71 * 1.186 * .431 * 1.11 * 2.098))} = 1.153$$

$$GM_Z = e^{1/5 * (\ln(3.11 * 1.186 * .488 * .598 * 2.092))} = 1.176$$

Normal M

$$GM_R = e^{1/5 * (\ln(.585 * .843 * 2.318 * .899 * .477))} = .867$$

$$GM_M = e^{1/5 * (\ln(1)) * 5} = 1$$

$$GM_Z = e^{1/5 * (\ln(.585 * .843 * 2.318 * .899 * .477))} = 1.020$$

Based on these calculations, Machine R is the slowest

Question 3.

9.5 Convert the following binary numbers to their decimal equivalents

(a) $001100 = 2^6 * 0 + 2^5 * 0 + 2^4 * 1 + 2^3 * 1 + 0 + 0 = 16 + 8 = 24$

(b) $000011 = 0 + 0 + 0 + 0 + 2^2 * 1 + 2^1 * 1 = 6$

(c) $011100 = 0 + 2^5 * 1 + 2^4 * 1 + 2^3 * 1 + 0 + 0 = 56$

(d) $111100 = 2^6 + 2^5 + 2^4 + 2^3 + 0 + 0 = 120$

(e) $101010 = 2^6 + 0 + 2^4 + 0 + 2^2 + 0 = 84$

Question 4.

9.7 Convert the following decimal numbers to their binary equivalents

(a) $64 \rightarrow 64/2 = 32R0 \mid 32/2 = 16R0 \mid 16/2 = 8R0 \mid 8/2 = 4R0 \mid 4/2 = 2R0 \mid 2/2 = 1R0 \mid 1/2 = 0R1$
 $= 1000000$

(b) $100 \rightarrow 50R0 \mid 25R0 \mid 12R1 \mid 6R0 \mid 3R0 \mid 1R1 \mid 0R1$
 $= 1100100$

(c) $111 \rightarrow 55R1 \mid 27R1 \mid 13R1 \mid 6R1 \mid 3R0 \mid 1R1 \mid 0R1$
 $= 1101111$

(d) $145 \rightarrow 72R1 \mid 36R0 \mid 18R0 \mid 9R0 \mid 4R1 \mid 2R0 \mid 1R0 \mid 0R1$
 $= 10010001$

(e) $255 \rightarrow 127R1|63R1|31R1|15R1|7R1|3R1|1R1|0R1$
 $=1111111$

Question 5.

9.11 Convert the following hexadecimal numbers to their decimal equivalents

(a) $C \rightarrow 12 * 16^0 = 12$

(b) $D3.E \rightarrow 13 * 16^1 + 3 * 16^0 + 14 * 16^{-1} = 211.875$

(c) $D52 \rightarrow 13 * 16^2 + 5 * 16^1 + 2 * 16^0 = 3410$

(d) $67E \rightarrow 6 * 16^2 + 7 * 16^1 + 14 * 16^0 = 1662$

(e) $ABCD \rightarrow 10 * 16^3 + 11 * 16^2 + 12 * 16^1 + 13 * 16^0 = 43981$

Question 6.

9.13 Convert dec to hex

(a) $16 \rightarrow 16/16 = 1R0 \rightarrow 1 * 16^1 + 0 * 16^0 = 10_{16}$

(b) $80 \rightarrow 80/16 = 5R0 \rightarrow 5 * 16^1 + 0 * 16^0 = 50_{16}$

(c) $2560 \rightarrow 2560/16 = 160R0 \rightarrow 160/16 = AR0$
 $= A00_{16}$

(d) $3000 \rightarrow 3000/16 = 187R8 \rightarrow 187/16 = 11R11$
 $= BB8_{16}$

(e) $625000 \rightarrow 62500/16 = 3906R4 \rightarrow 3906/16 = 244R2 \rightarrow 244/16 = 15R4$
 $= F424_{16}$

Question 7.

10.11 Find the following differences using two's compliment arithmetic

- (a) $111000 - 110011 \rightarrow 111000 + 001101 = 000101$
- (b) $11001100 - 00101110 \rightarrow 11001100 + 11101110 = 00111010$
- (c) $111100001111 - 110011110011 \rightarrow 111100001111 + 001100001101 = 001000011100$
- (d) $11000011 - 111010000 \rightarrow 11000011 + 00011000 = 11011011$

Question 8.

10.15 $23 * 29$ in binary

$$23 * 29 = 667$$

$$23 = 010111, 29 = 011101$$

$$A \leftarrow 000000$$

$$Q \leftarrow 011101$$

$$Q_{-1} \leftarrow 0$$

$$M \leftarrow 010111$$

$$-M = 101001$$

Count	A	Q	Q_{-1}	M	Step
6	000000	011101	0	010111	init
6	101001	011101	0	010111	$A \leftarrow A - M$
5	110100	101110	1	010111	shift
5	001011	101110	1	010111	$A \leftarrow A + M$
4	000101	110111	0	010111	shift
4	101110	110111	0	010111	$A \leftarrow A - M$
3	110111	011011	1	010111	shift
2	111011	101101	1	010111	shift
1	010100	110110	1	010111	$A \leftarrow A + M$
0	001010	011011	0	010111	shift

$$010111 * 011101 = 001010011011 = 667$$

10.15) 23 x 29

010111 011101

-m = 101001

	A	Q	Q _{i-1}	M	
6	000000	011101	0	010111	init
5	+101001		0	010111	A ← A-m
4	101001	011101	1	010111	shift
3	110100	101110	1	010111	A ← A+m
2	+010111		0	010111	shift
1	001011	101110	0	010111	A ← A-m
0	100101	110111	1	010111	shift
	+101001		0	010111	A ← A-m
	000101	110111	0	010111	shift
	101110	011011	1	010111	shift
	110111	011011	1	010111	shift
	111011	101101	1	010111	shift
	111101	110110	1	010111	shift
	010111		1	010111	A ← A+m
	001010	110110	1	010111	shift
	001010	011011	0	010111	shift