

**All the formulas listed below should be memorized.**  
**(Some of them may be found in Appendix A.)**  
**Also, you are required to know how to use them in calculations.**

(1) $\sum_{k=m}^n (ca_k + db_k) = c \sum_{k=m}^n a_k + d \sum_{k=m}^n b_k$	(4) Summarizing $n$ terms of geometrical progression with the first term $b$ and common ratio $r$ : $b + br + br^2 + \dots + br^{n-1} = b \frac{r^n - 1}{r - 1}$
(2) $\sum_{k=m}^n c = c \sum_{k=m}^n 1 = c(n - m + 1)$	(4a) Summarizing terms of infinite geometrical progression ( $ r  < 1$ ): $b + br + br^2 + \dots = \frac{b}{1 - r}$
(3) Summarizing $n$ terms of arithmetical progression with the first term $a_1$ and common difference $d$ : $a_1 + a_2 + \dots + a_n =$ $= a_1 + (a_1 + d) + (a_1 + 2d) + \dots + (a_1 + (n-1)d) =$ $= \frac{a_1 + a_n}{2} n$	(5) Telescoping: $\sum_{k=m}^n (a_k - a_{k-1}) =$ $= (a_m - a_{m-1}) + (a_{m+1} - a_m) + \dots + (a_n - a_{n-1})$ $=$ $= a_n - a_{m-1}$
(3a) $\sum_{k=m}^n k = m + (m+1) + (m+2) + \dots + n =$ $= \frac{m+n}{2} (n - m + 1)$	(5a) Telescoping: $\sum_{k=m}^n (a_k - a_{k+1}) =$ $=$ $(a_m - a_{m+1}) + (a_{m+1} - a_{m+2}) + \dots + (a_n - a_{n+1})$ $=$ $= a_m - a_{n+1}$
(3b) $\sum_{k=1}^n k = \frac{1+n}{2} n$	(6) Harmonic numbers: $H_n = \sum_{k=1}^n \frac{1}{k} = 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$ $\approx \ln n + \gamma + \frac{1}{12n},$ where $\gamma \approx 0.57721\dots$ (Euler's constant)
<i>Logarithms</i>	
$\log_a x^y = y \log_a x$	$\log_a \frac{x}{y} = \log_a x - \log_a y$ $\log_a (xy) = \log_a x + \log_a y$
$\log_a x = \frac{\log_b x}{\log_b a}$	$\log_a x = \frac{1}{\log_x a}$ $x^{\log_a y} = y^{\log_a x}$