

Tutorial

Predicate Logic and
Propositional Logic

Every child loves Santa.

$$\forall x (CHILD(x) \rightarrow LOVES(x, Santa))$$

- Everyone who loves Santa loves any reindeer.

Everyone who loves Santa loves any reindeer.

$$\forall x, \forall y (LOVES(x, Santa) \wedge REINDEER(y) \rightarrow LOVES(x, y))$$

Rudolph is a reindeer, and Rudolph
has a red nose.

*REINDEER(Rudolph) \wedge
REDNOSE(Rudolph)*

Anything which has a red nose is
weird or is a clown.

$$\forall x$$
$$REDNOSE(x) \rightarrow WEIRD(x) \vee$$
$$CLOWN(x)$$

No reindeer is a clown.

$$\neg \exists x (REINDEER(x) \wedge CLOWN(x))$$

Scrooge does not love anything which
is weird.

$$\forall x (WEIRD(x) \rightarrow \neg LOVES(Scrooge, x))$$

Anyone whom Mary loves is a
football star.

$$\forall x (LOVES(Mary, x) \rightarrow STAR(x))$$

Any student who does not pass does
not play.

$$\forall x (STUDENT(x) \wedge \neg PASS(x) \\ \rightarrow \neg PLAY(x))$$

John is a student.

STUDENT(John)

Any student who does not study
does not pass.

$$\forall x (STUDENT(x) \wedge \neg STUDY(x) \\ \rightarrow \neg PASS(x))$$

Anyone who does not play is not a
football star.

$$\forall x (\neg \text{PLAY}(x) \rightarrow \neg \text{STAR}(x))$$

Anyone who rides a Harley is a
rough character.

$$\forall x: \text{rides}(x, \text{Harley})$$
$$\rightarrow \text{roughcharacter}(x)$$

Every biker rides either Harley or
bmw.

$\forall x: \text{biker}(x) \rightarrow \text{rides}(x, \text{Harley}) \vee$
 $\text{rides}(x, \text{bmw})$

Anyone who rides a bmw is a
yuppie.

$$\forall x: \text{rides}(x, \text{bmw}) \rightarrow \text{yuppie}(x)$$

Every yuppie is a lawyer.

$\forall x: \text{yuppie}(x) \rightarrow \text{lawyer}(x)$

Any nice girl does not date anyone
who is a rough character.

$$\begin{aligned} & \forall x: \forall y: \\ & \textit{nicegirl}(x) \wedge \textit{roughcharacter}(y) \\ & \rightarrow \sim \textit{date}(x,y) \end{aligned}$$

Mary is a nice girl and John is a biker.

$\text{Nicegirl}(\text{mary}) \wedge \text{biker}(\text{john})$

Thank you