Paired t-test for dobberence of Mean

Consider the case when O the sample sizes are equal ie n = n = n (say), and (i) the two samples are not independent but sample observations are paired together, ie, the pair or observations (xi/yi) (8=1,2,- n) corresponds to the Same (ith) sample unit. The problem is to feet et the sample means debber significantly or not. For example, suppose we want to test the elbicacy of a particular drug, say, bus inducing sleep. Let xi and yi (1=1,2,-n) be the readings, on hours of sleep, on the ith individual before and abter the drug is given respectively. Here custiand at applying the delberence of mean fest disussed en previous class, we apply paired t-test given below

Here we consider the increments di=xi-fi (E=1,2-- 7)

Under the need hypothesis, Ho that increments are due to bluetuations of sampling, i.e., the drug is not responsible by these encrements

the statistic: d= d

where $d = \frac{1}{n} \frac{m}{i=1} di$ and $s^2 - 1 = \frac{n}{i-1} (di-\bar{d})^2$

bullows student's t-destribution with (n-1) degree ab treedom. Remark: Some students have contrusion with debberence of mean t-test and paired t-lest bur debberence of mean you need to be carebul to understand it EX 1) A cortain stimulus administered to each ab the 12 patients regulted in the bollowing increase at Blood processure: 5, 2, 8, -1, 3, 0, -2, 1, 5, 0, 4 and 6 Can we conclude that the stimulus, in general, be accompanied by an increase in blood pressure? (Remark: Betwee solving, et let us undorstand that here the increase in blood pressure corresponds to the same individual, i.e there gre 12 patients and the dibberence on blood pressure is given by each at them) Col: Here we are ginew the increments in blood pressure le di(=xi-yi) Null hypothesis Ho: Ux = lly ie, there is no significant debberence in the blood pressure residence ab the patients before and abter the drug. In other words the given increments are just by chance and not due to stimulus. Alternative hypothesis Hi: My < lly, ie the stimulus results in an increase on blood pressyre lest steefistic 1 - d 5/07

 $\overline{d} = \frac{1}{h} \sum d$ and s2 = 1 [\(\frac{2}{2}\d^2 - (\frac{1}{2}\d)^2\) d | 5 2 8 -1 3 0 -2 1 5 0 4 6 d 2 25 4 64 1 9 0 4 1 25 0 16 36 Id=31 and Id=185 $\overline{d} = 31 - 2.58$ $= \frac{1}{11} \left[185 - \frac{(31)^2}{12} \right] = 9.5382$ $t = \frac{d}{d} - \frac{2.58}{\sqrt{9.5382}} - \frac{2.58 \times \sqrt{12}}{\sqrt{9.5382}}$ = 2.89 Tabulated to.os for 11 d.f = 1.80 Calulated t 7 Tabulated t Null hypothesis is rejected

Hence use conclude that, the stimulus, will

an general be accompanied by an increase in

blood prossyre.

	Page		
- Andrew	Ex(2) In a contain experiment in		
	Ex(2) In a costain experiment to compare two		
	Tesult of increase in weights were observed in		
7 7 7	animals:		
1950.33	Animal number! 1 2 3 4 5 6 7 8 Total		
	Increase weight Food 1 49 53 51 52 47 50 52 53 407		
	en pound Foodis 52 55 52 53 50 54 54 53 423		
	(1) Assuming that the two samples of animals are interpented		
	Independent, can we conducte that bood B is better		
Than bood HY			
	(1) Also examene. the case whom the same set at eight		
	animals were used in both the bields.		
	Colo Nell whollow Ho. If the increase in weights		
	Sol: Null hypothisis, Ho: If the increase in weign		
	respectively, then Ho: l/x = lly, re there is no		
	significant debberence in increase in weight due		
	to diets A and B.		
	Alternative Lypothisis H, : Mx < My		
	more of		
	1) PC tum camples are assumed to be independent		
	O If two samples are assumed to be independent are well apply t-test or difference at means		
	to feet 610		
	41 123 (1)		
	4 - 7		
	$f = \overline{\chi} - \overline{f}$		
	$\sqrt{s^2/\frac{1}{2}+\frac{1}{2}}$		
	V (7 3)		

		classmate Date Page		
	FoodA	, Food B		
1000	x d=x-50 d2	Y D=Y-52 02		
1 1 1 1 1 1 1 1	49 -1	52 0 0		
3.61	53 3 9	55 3 9		
	5/ / /	52, 0		
	52 2 4	53		
	47 -3 9	50 -2 4		
	50 0 0	54 2 4		
	52 2 4	54 2 4		
	53 3 9	53		
NAME OF	Total 7 37	Total 7 23		
	. X	F = 52 + 7.		
	= 50.875	= 52.875		
111	1 - , -, 2 - , 2	15 12) 27 49		
	and $\sum (x-\overline{x})^2 = \sum d^2 - (\sum d^2) = 37 - \frac{49}{8}$			
	= 30.875			
	and $12(y-y)^2 = 50^2 - (20)^2$			
	= 23-49 = 16.875			
	$S^2 = \frac{1}{n_1 + n_2 - 2} \left[\sum_{x \in \mathcal{X}} (x - \overline{x})^2 + \sum_{y \in \mathcal{Y}} (y - \overline{y})^2 \right]$			
	$S^{2} = \frac{1}{n_{1} + n_{1} - 2} \left[\sum (x - \overline{x})^{2} + \sum (y - \overline{y})^{2} \right]$ $= \frac{1}{14} \left[30.875 + 16.875 \right] = 3.41$			
	14			
	Tabulated toos for (8+8-2)=14 d-f=1.76			
	$t=\frac{x-y}{y}$:	= 30.8/5-52.0/5 = -2.17		
	$t = \overline{x} - \overline{y} = \frac{50.875 - 52.875}{\left(\frac{5}{h_1} + \frac{1}{h_2}\right)} = \frac{-2.17}{\left(\frac{3.41}{8} + \frac{1}{8}\right)}$			
	(1 (" 2) (to t in t < -1.76			
-	The critical region for leht tail test is t < -1.76 Since calculated t is list than -1.76 Mois			
1	rejected at 5% level at significance.			
1	so ace conclude that bood B is superior.			
1				

