

# Life is short

But unlimited?

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## Human life is unlimited – but short

Holger Rootzén<sup>1</sup>  · Dmitrii Zholud<sup>1</sup> 

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Received from: [Zentralblatt für Mathematik](#).

**Rootzén, Holger; Zholud, Dmitrii**

**Human life is unlimited – but short.** (English) Zbl 1387.62120

**Extremes 20, No. 4, 713-728 (2017).**

The question whether the human lifespan has a finite limit or not is an old controversy, and the authors' contribution to the subject is that they provide a precise definition of the concept of a finite limit. They argue that there are three possibilities founded in extreme value theory: (i) The force of mortality tends to infinity at a finite age, and survival beyond that age is impossible, (ii) the force of mortality is constant after a certain age, e.g., 110 years of age, and life is unlimited but short, and (iii) the force of mortality is decreasing with age (after age 110), and life is unlimited. Furthermore, the authors claim that (ii) is the correct conclusion, given information available today, and they argue that recent contributions in the field that argues for alternative (i) do so based on inappropriate use of statistics, especially inadequate treatment of size-biased sampling. They come to their conclusions by handling the size-biased sampling correctly and by using the Generalized Pareto (GP) distribution as a model for supercentenarian life: Now available data points to the result that the special case of a GP distribution, the exponential (ii), with mean 1.34 years, is the distribution that fits data best. Furthermore, there is no sign of variation in this result with respect to sex, genetic background, lifestyle, etc. However, ten times more women than men reach the age of 110.

Reviewer: Göran Broström (Umea)

**MSC:**

- 62P10** Applications of statistics to biology and medical sciences
- 62N01** Censored data models
- 60G70** Extreme value theory; extremal processes (probability theory)
- 62G32** Statistics of extreme values; tail inference

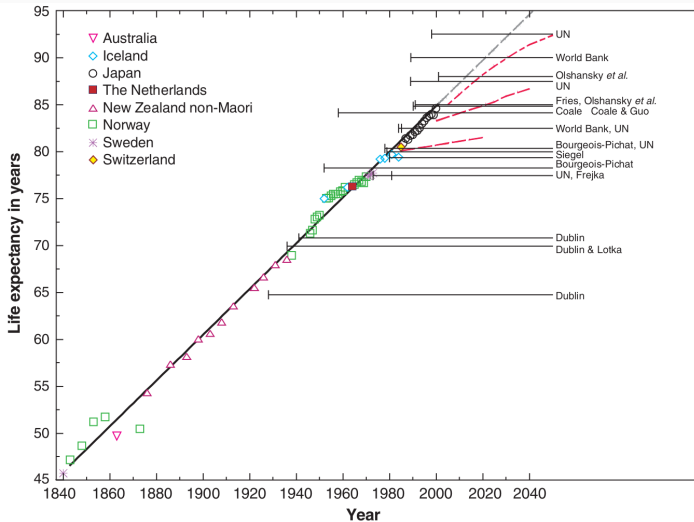
**Keywords:**

extreme human life lengths; no influence of lifestyle on survival at extreme age; no influence of genetic background on survival at extreme age; future record ages; supercentenarians; Jeanne Calment; limit for human life span; force of mortality; size-biased sampling; IDL; generalized Pareto distribution

# What it is about

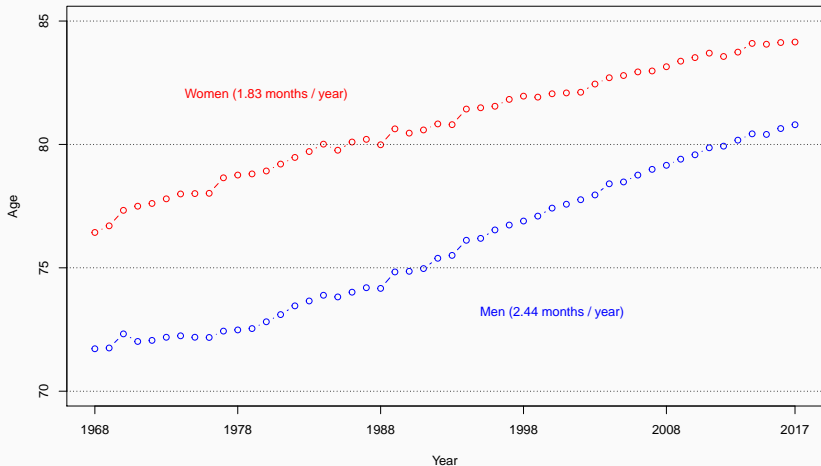
- Is human life **unlimited**?
- Are there any **differences in survival** at extreme age between
  - women and men,
  - different socioeconomic groups,
  - etc?

# Broken Limits to Life Expectancy: Science 2002

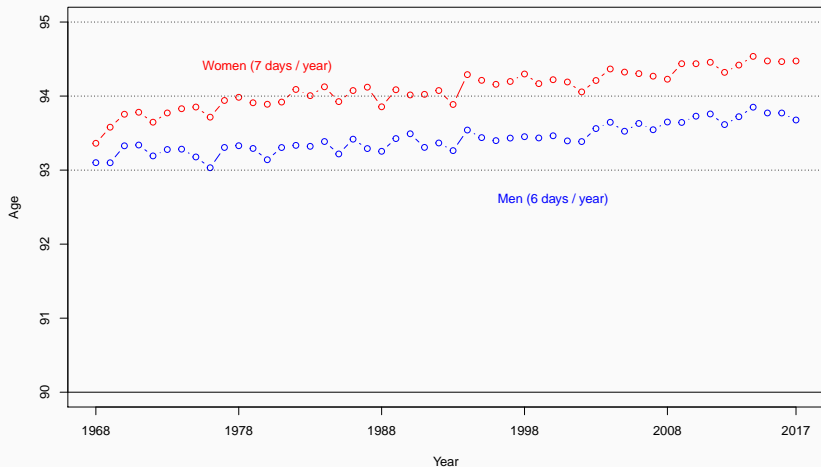


Authors: James Vaupel and Jim Oeppen. Gain / year: 3 months.

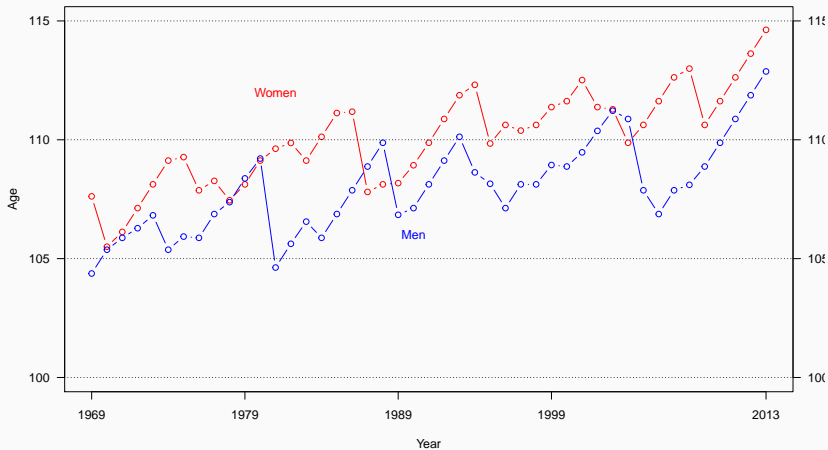
# Sweden 1968-2014: Remaining life at birth



# Sweden 1968-2014: Remaining life at age 90



# Sweden 1969-2013: Maximum life





## Chiyo Miyako, Japan



World's oldest person since 21 April, 2018. Age: 117.

(Age on picture: 114.)



## Världens äldsta person har dött – blev 117 år

► Japanskan Chiyo Miyako har avlidit ✓ "Pratglad och vänlig person"

Now oldest: [Kane Tanaka](#), Japan (115 years and 205 days).

## SCB data on old age mortality

Deaths by age and year

|      | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 | 2013 | 2014 |
|------|------|------|------|------|------|------|------|------|
| 97   | 916  | 910  | 934  | 947  | 1015 | 1058 | 1018 | 1060 |
| 98   | 662  | 662  | 694  | 691  | 760  | 757  | 740  | 724  |
| 99   | 430  | 479  | 485  | 449  | 489  | 540  | 591  | 513  |
| 100+ | 712  | 764  | 778  | 845  | 822  | 953  | 908  | 983  |

Not very useful (100+).

<https://www.supercentenarians.org>

<http://www.grg.org>



## GERONTOLOGY RESEARCH GROUP

### GRG World Supercentenarian Rankings List

Last Updated On: Jul 18 2018 3:45PM

#### Numbers of Living Supercentenarians as of Last Update

|         |    |
|---------|----|
| Females | 34 |
| Males   | 2  |
| Total   | 36 |

#### Validated Living Supercentenarians

Avg Age: 113 Years, 115 Days (Decimal: 113.3142)

# The Human Mortality Database

<https://www.mortality.org>

- Contains no individual data.
- But very [useful tables](#).



Människans livslängd är programmerad i arvsmassan och svår att påverka visar en ny amerikansk studie. Det finns alltså en genetiskt bestämd gräns för våra liv. Foto: TT

## 120 år – människans "maximala" livslängd

Kan en människa bli hur gammal som helst eller finns det en övre gräns för vårt åldrande? Det menar forskarna bakom en ny studie som visar att människans livslängd har en naturlig gräns som är svår att överskrida.

# Jeanne Calment, age 122.

SCIENCE

The New York Times

MATTER

## *What's the Longest Humans Can Live? 115 Years, New Study Says*



Jeanne Calment died in 1997 in France at the age of 122. Pascal Parrot/Sygma, via Getty Images

By Carl Zimmer

Oct. 5, 2016



On Aug. 4, 1997, Jeanne Calment passed away in a nursing home in France.




**nature**

International journal of science

Letter | Published: 05 October 2016

# Evidence for a limit to human lifespan

Xiao Dong, Brandon Milholland & Jan Vijg 

*Nature* **538**, 257–259 (13 October 2016) | [Download Citation](#) 

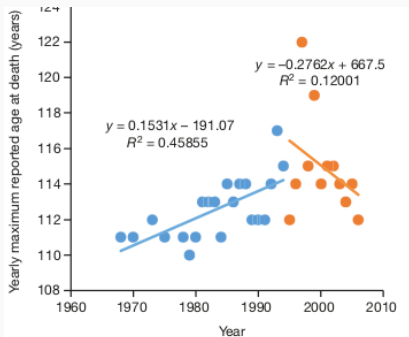


Figure 2 | Reported age at death of supercentenarians

- International Database on Longevity
- Highest age at death each year
- Linear regression with breakpoint
- Increasing trend broken!

Any **problems** with this "statistical analysis"?

# Dong, Milholland & Vijg, Nature 2016: Problems.

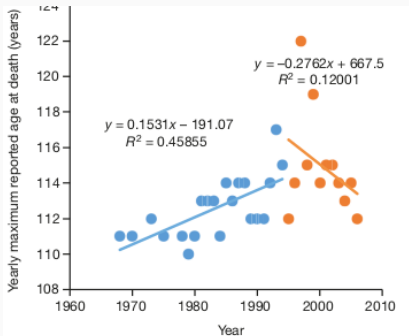
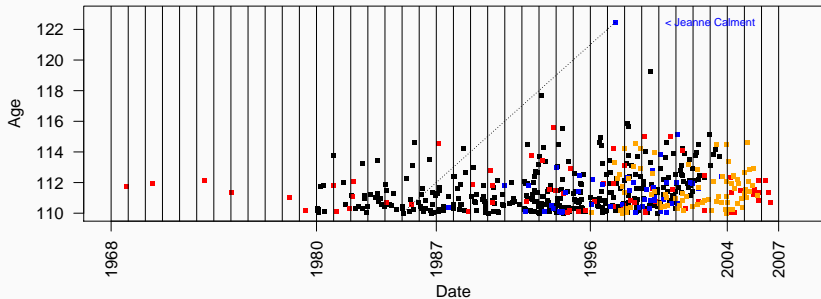


Figure 2 | Reported age at death of supercentenarians

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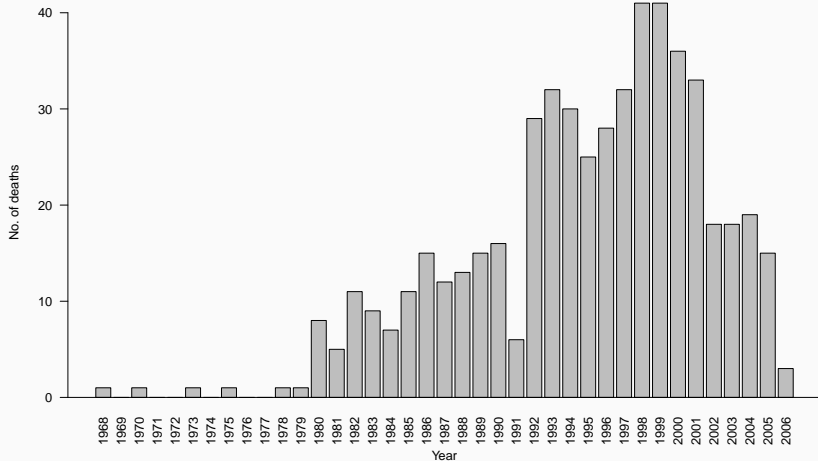
- Ad hoc choice of cutpoint.
- Very short time series to confirm a trend break.
- What about the survivors?
- Data are extreme values: full data?

# The full data



| Country | First | Last |
|---------|-------|------|
| UK      | 1968  | 2006 |
| USA     | 1980  | 2003 |
| France  | 1987  | 2003 |
| Japan   | 1996  | 2005 |

# Number of deaths by year




**nature**  
International journal of science

Brief Communications Arising | Published: 28 June 2017

# Questionable evidence for a limit to human lifespan

Adam Lenart & James W. Vaupel 

*Nature* **546**, E13–E14 (29 June 2017) | [Download Citation](#) 

## **Contesting the evidence for limited human lifespan**

Nicholas J. L. Brown, Casper J. Albers & Stuart J. Ritchie

### **Dong *et al.* reply**

Xiao Dong, Brandon Milholland & Jan Vijg

## **Many possible maximum lifespan trajectories**

Bryan G. Hughes & Siegfried Hekimi

### **Dong *et al.* reply**

Xiao Dong, Brandon Milholland & Jan Vijg

## **Is there evidence for a limit to human lifespan?**

Maarten P. Rozing, Thomas B. L. Kirkwood & Rudi G. J. Westendorp

### **Dong *et al.* reply**

Xiao Dong, Brandon Milholland & Jan Vijg

## **Questionable evidence for a limit to human lifespan**

Adam Lenart & James W. Vaupel

### **Dong *et al.* reply**

Xiao Dong, Brandon Milholland & Jan Vijg

## **Maximum human lifespan may increase to 125 years**

Joop de Beer, Anastasios Bardoutsos & Fanny Janssen

### **Dong *et al.* reply**

Xiao Dong, Brandon Milholland & Jan Vijg

Two serious blows:

1. **Extreme values** do **not** behave like “normal” data.
2. The data suffer from **length bias**.

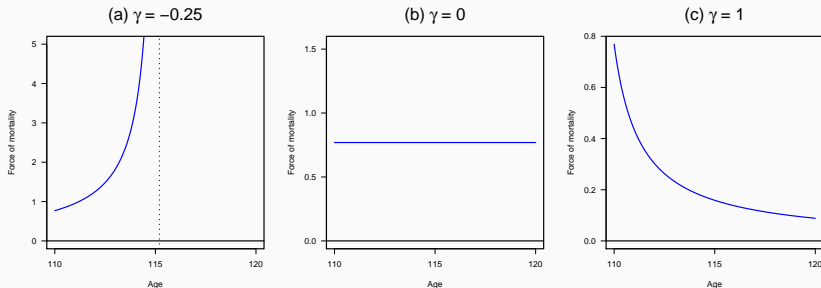
and one conclusion:

1. There is **no aging** after age 110!



# The Generalized Pareto (GP) distribution

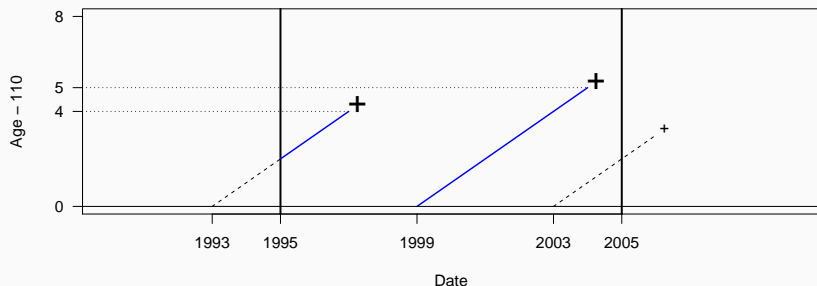
$$h(x; (\gamma, \sigma)) = \frac{1}{\sigma(1 + \gamma x/\sigma)_+}$$



1. “Life is short”; (b) “Life is unlimited but short”; (c) “Life is unlimited”.

# Length-biased sampling

Data are *left-truncated* and *right-truncated*:



$$\mathcal{L} = \frac{\mathcal{P}(X_1 = 4)}{\mathcal{P}(2 < X_1 \leq 12)} \times \frac{\mathcal{P}(X_2 = 5)}{\mathcal{P}(X_2 \leq 6)}$$

*Inverse Probability Weighting* (Horwitz-Thomson, *JASA* 1952.)

# Critique of Dong et. al. by Rootzen & Zholud

- The apparent trend break in the figure is an artifact caused by **inappropriate combination of data** from different time periods.
- The conclusion “our data strongly suggest that the duration of life is limited” is based on **wrong and misleading analysis**.

- “Life is unlimited but short”:  $\gamma = 0$ ,  $\sigma = 1.34$ 
  - No aging after age 105.
  - Expected remaining life at age  $t$ ,  $t > 105$ : 1.34 years.
  - Probability of surviving one year: 47 per cent.
- *Interpretation*: At each birthday after 105, flip a coin. If heads, survive until next birthday, if tails, die before next birthdate.
- No difference between countries, sexes, birth cohorts.

“I was outraged that Nature, a journal I highly respect, would publish such a travesty.”

# How could this happen?

Not uncommon:

- No statisticians involved.
  - Demographic research is performed by people from sociology, psychology, economy, etc. with inadequate statistical training.
  - the same holds for editors of journals from the same fields.
- Too powerful statistical software.
  - "Who needs a statistician?"
  - "I have read the manual."
- Failure to understand the GIGO principle ("Garbage In, Garbage Out").
  - There is always some Garbage Out.

See <http://capa.ddb.umu.se/ds>

# Data from FOB and Lisa

**Birth** information (11 566 545 individuals):

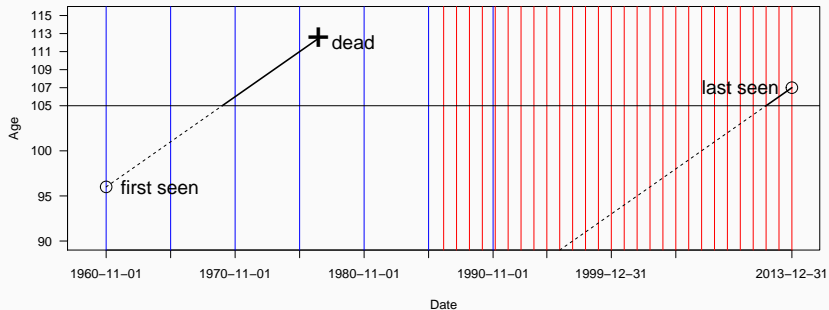
| LINNEID  | FODELSEAR | FODELSEKVARTAL | KON |
|----------|-----------|----------------|-----|
| 10001430 | 1940      | 2              | 1   |
| 12424305 | 1945      | 3              | 2   |
| 10966939 | 1946      | 1              | 1   |

**Death** information (4 772 378 individuals):

| LINNEID | DODSDAT  |
|---------|----------|
| 6       | 20130127 |
| 26      | 20130923 |
| 32      | 20051001 |

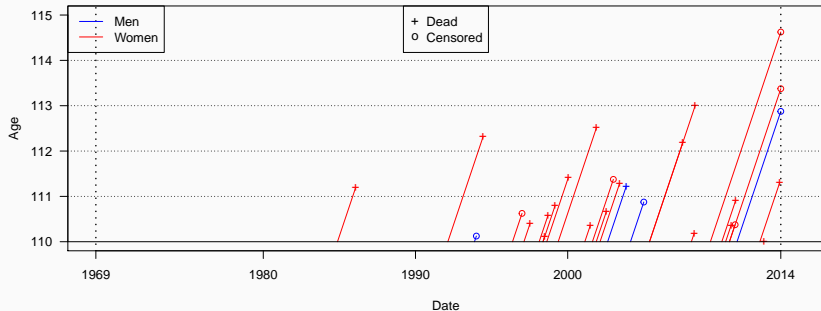
**Presence** information?

# Presence information





## Swedish data, 110+



There are 23 women and 4 men.

# The Gompertz distribution

Hazard function:

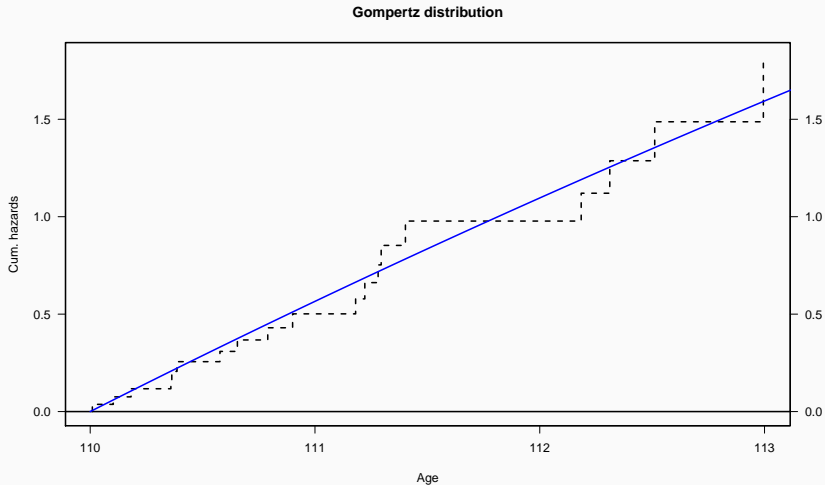
$$h(t; \alpha, r) = \alpha \exp(rt), \quad t > 0$$

If  $r = 0$ :

$$h(t; \alpha, 0) = \alpha, \quad t > 0$$

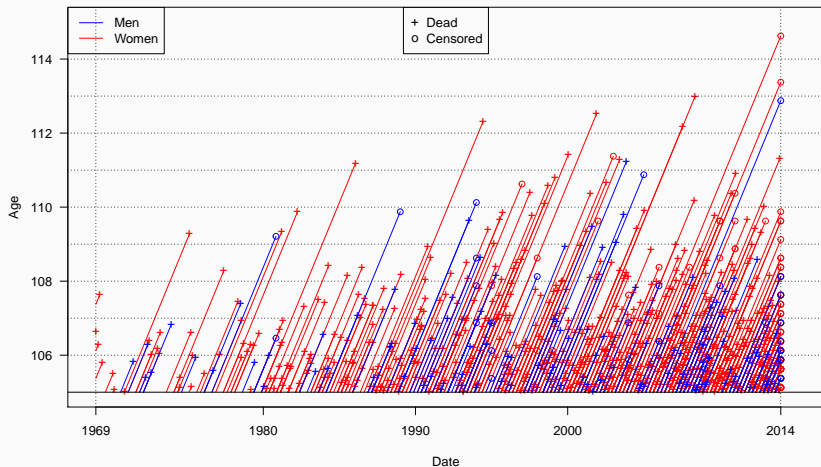
$$H(t; \alpha, 0) = \alpha t, \quad t > 0.$$

# Cumulative hazards beyond age 110



$r = -0.064$  (0.239), mean = 1.713

# Sweden, 105+

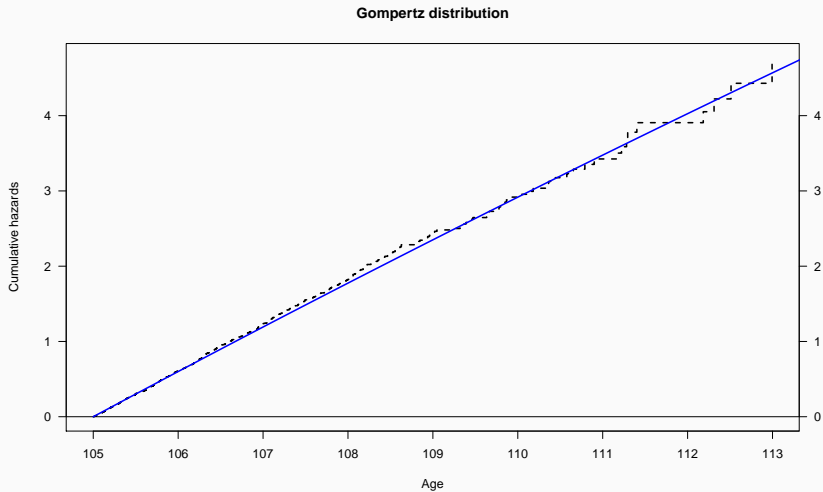


| Covariate           | Mean   | Coef   | Risk Ratio | S.E.        | L-R $p$ |
|---------------------|--------|--------|------------|-------------|---------|
| sex                 |        |        |            |             | 0.093   |
| <i>woman</i>        | 0.851  | 0      | 1          | (reference) |         |
| <i>man</i>          | 0.149  | -0.169 | 0.844      | 0.103       |         |
| l(birthdate - 1900) | -5.284 | -0.005 | 0.995      | 0.003       | 0.193   |
| Baseline parameters |        |        |            |             |         |
| rate                |        | -0.014 | 0.986      | 0.026       | 0.583   |
| log(level)          |        | -0.503 | 0.605      | 0.054       | 0.000   |
| Events              | 846    | TTR    | 1426       |             |         |
| Max. Log Likelihood | -1285  |        |            |             |         |

Constant hazard = 0.605.

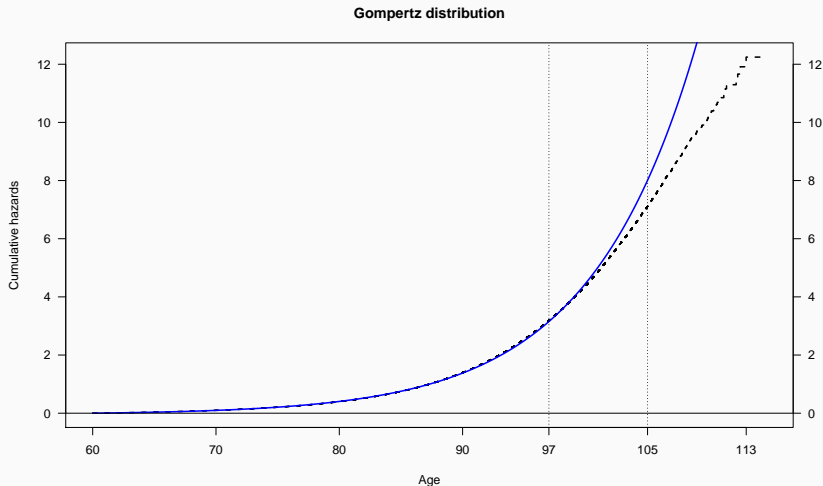
Mean =  $1/0.605 = 1.65$  years.

## Baseline hazard, 105+



$$r = -0.014 (0.026)$$

## In perspective, 60+



$$r = 0.115, \exp(r) = 1.122.$$

HUMAN DEMOGRAPHY

# The plateau of human mortality: Demography of longevity pioneers

Elisabetta Barbi<sup>1\*</sup>, Francesco Lagona<sup>2</sup>, Marco Marsili<sup>3</sup>,  
James W. Vaupel<sup>4,5,6,7</sup>, Kenneth W. Wachter<sup>8</sup>

Theories about biological limits to life span and evolutionary shaping of human longevity depend on facts about mortality at extreme ages, but these facts have remained a matter of debate. Do hazard curves typically level out into high plateaus eventually, as seen in other species, or do exponential increases persist? In this study, we estimated hazard rates from data on all inhabitants of Italy aged 105 and older between 2009 and 2015 (born 1896–1910), a total of 3836 documented cases. We observed level hazard curves, which were essentially constant beyond age 105. Our estimates are free from artifacts of aggregation that limited earlier studies and provide the best evidence to date for the existence of extreme-age mortality plateaus in humans.

**S**urvival to extreme ages tests the limits of evolutionary demographic potential. Here we report a curve of death rates by age for

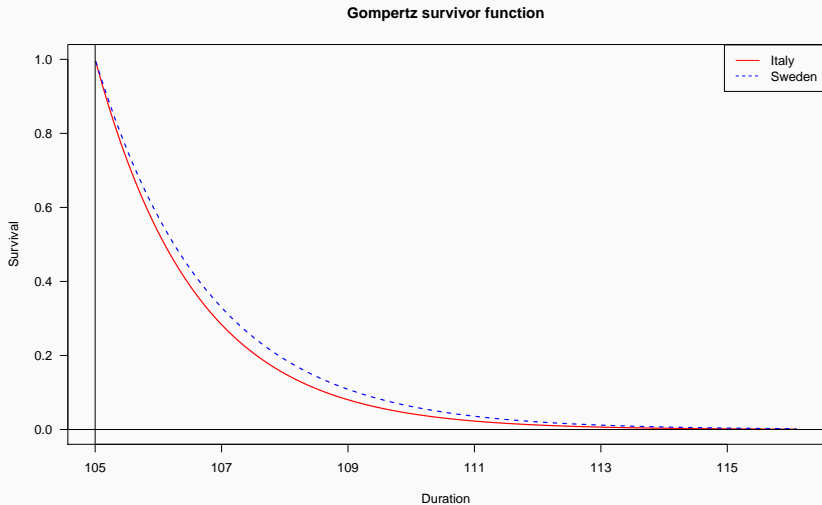
tality curve levels out, it is said to reach a plateau. The findings for humans are consistent with discoveries of plateauing mortality at extreme ages



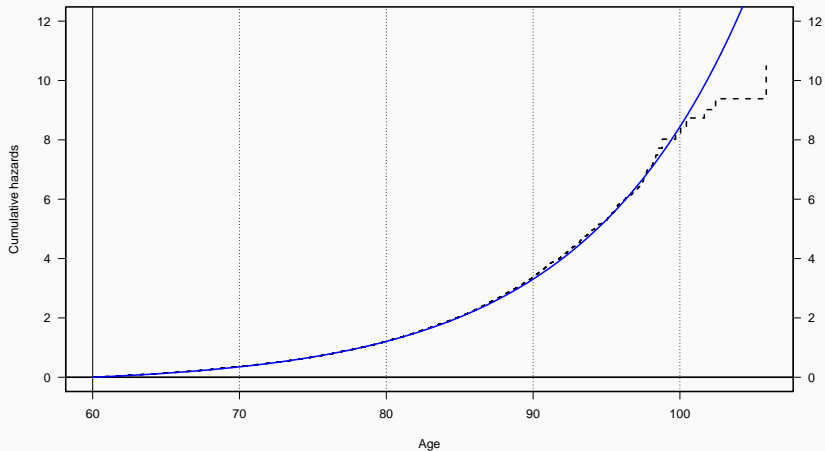
## Italy results

| Covariate           | Mean  | Coef   | Risk Ratio | S.E.        | L-R <i>p</i> |
|---------------------|-------|--------|------------|-------------|--------------|
| I(cohort - 1900)    | 6.120 | -0.016 | 0.984      | 0.009       | 0.076        |
| sex                 |       |        |            |             | 0.561        |
| <i>woman</i>        | 0.886 | 0      | 1          | (reference) |              |
| <i>man</i>          | 0.114 | 0.034  | 1.035      | 0.058       |              |
| Baseline parameters |       |        |            |             |              |
| rate                |       | 0.013  | 1.013      | 0.017       | 0.444        |
| log(level)          |       | -0.399 | 0.671      | 0.073       | 0.000        |
| Events              | 2883  | TTR    | 4639       |             |              |
| Max. Log Likelihood | -4250 |        |            |             |              |

# Sweden and Italy



## Skellefteå-Umeå data, birth cohort 1810-1850, ages 60+

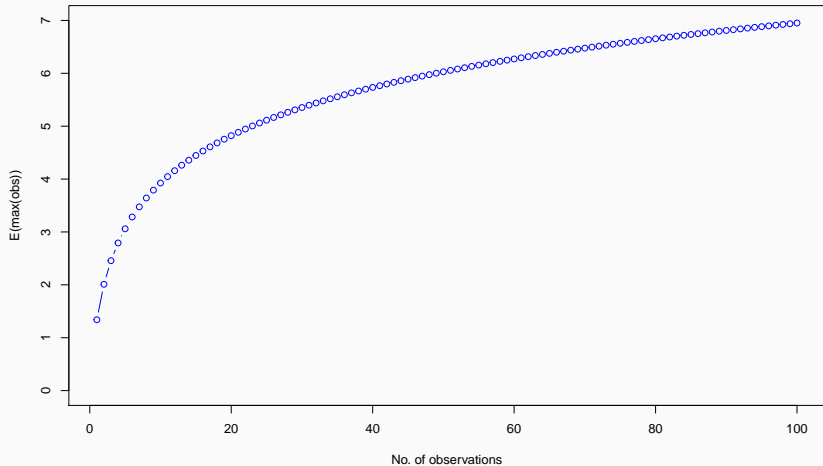


# Conclusion

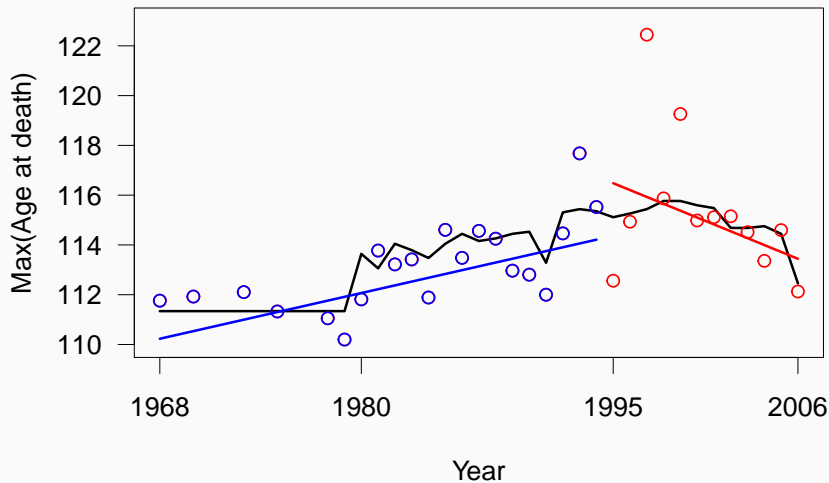
- No evidence of limits to human life
  - Not rejecting a null hypothesis means no information
- The mortality plateau after age 105 seems universal.
- Be aware of risks of sampling bias.
- Ditto of informative censoring.
- The aging process
  - begins at birth, and
  - ends at age 105



# Expectation of extremes



## The original plot, expectation added

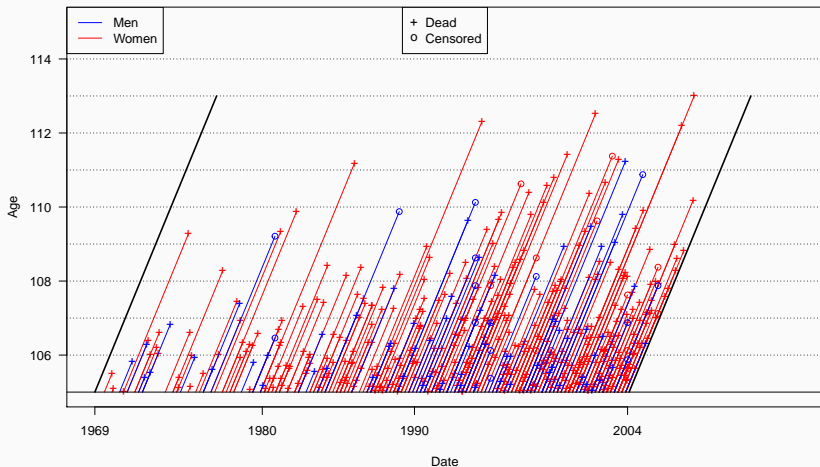


# Analysis, no censored observations, 105+

| Covariate           | Mean   | Coef  | Risk Ratio | S.E.        | L-R $p$ |
|---------------------|--------|-------|------------|-------------|---------|
| sex                 |        |       |            |             | 0.340   |
| <i>woman</i>        | 0.878  | 0     | 1          | (reference) |         |
| <i>man</i>          | 0.122  | 0.099 | 1.104      | 0.102       |         |
| I(birthdate - 1900) | -6.560 | 0.011 | 1.011      | 0.004       | 0.003   |
| Baseline parameters |        |       |            |             |         |
| log(scale)          |        | 0.287 | 1.332      | 0.040       | 0.000   |
| log(shape)          |        | 0.072 | 1.075      | 0.027       | 0.007   |
| Events              | 846    | TTR   | 1152       |             |         |
| Max. Log Likelihood | -1100  |       |            |             |         |



# Cohort version, 105+



432 women, 83 men.

# Cohort Analysis

| Covariate           | Mean  | Coef   | Risk Ratio | S.E.        | L-R <i>p</i> |
|---------------------|-------|--------|------------|-------------|--------------|
| cohort              |       |        |            |             | 0.086        |
| (1969,1985]         | 0.158 | 0      | 1          | (reference) |              |
| (1985,1995]         | 0.376 | -0.291 | 0.747      | 0.131       |              |
| (1995,2004]         | 0.465 | -0.166 | 0.847      | 0.124       |              |
| sex                 |       |        |            |             | 0.042        |
| woman               | 0.827 | 0      | 1          | (reference) |              |
| man                 | 0.173 | -0.259 | 0.772      | 0.131       |              |
| Baseline parameters |       |        |            |             |              |
| rate                |       | 0.041  | 1.041      | 0.033       | 0.217        |
| log(level)          |       | -4.617 | 0.010      | 3.498       | 0.187        |
| Events              | 487   | TTR    | 819        |             |              |
| Max. Log Likelihood | -735  |        |            |             |              |

## Cumulative hazards by period

