CS426 Project 2 - Parallel Conjugate Gradient

# Introduction

This report presents performance results for a dense, MPI-parallel Conjugate Gradient (CG) solver implemented as part of CS426/525 Project 2. We measure elapsed times on the ORFOZ cluster for varying core counts and problem sizes to evaluate. All timings use MPI\_Wtime() with appropriate barriers.

* Strong scaling: fixed problem size, increasing cores.
* Weak scaling: problem size grows proportionally with cores.

Timings were extracted from the output files produced by each run.

# Experimental Setup

Hardware: ORFOZ cluster nodes.

Software: MPI-based CG solver (dense SPD matrix).

Strong scaling:

where is the problem size describing the matrix which has a size of and vector which has a size of .

Weak scaling:

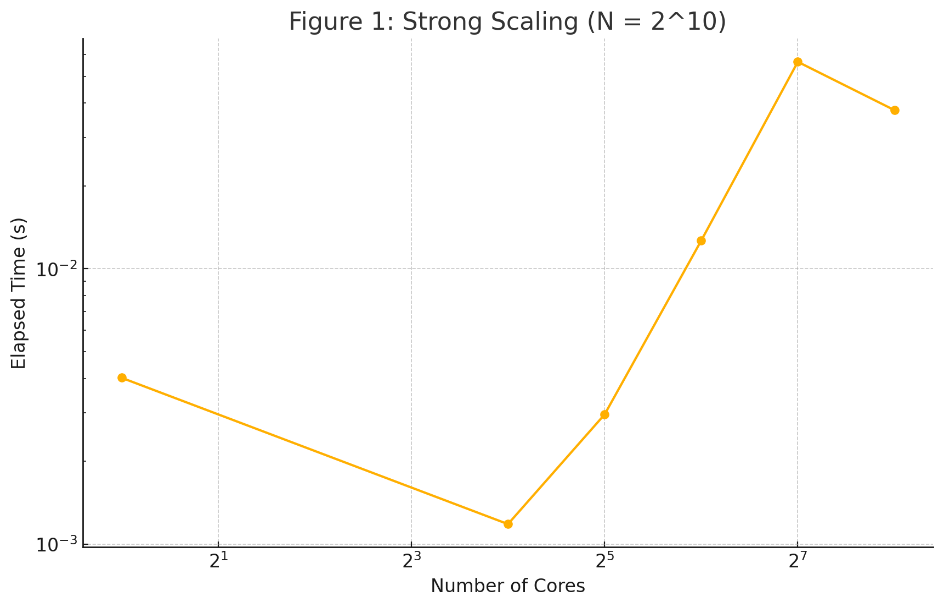
# Results

Diminishing returns beyond 16 cores meaning communication latency and synchronization dominate, causing execution time to rise for cores .

## Table 1: Strong Scaling Curve with

|  |  |
| --- | --- |
|  | |
| Core Count | Elapsed Time (s) |
| 1 | 0.004023 |
| 16 | 0.001184 |
| 32 | 0.002960 |
| 64 | 0.012656 |
| 128 | 0.056406 |
| 256 | 0.037674 |

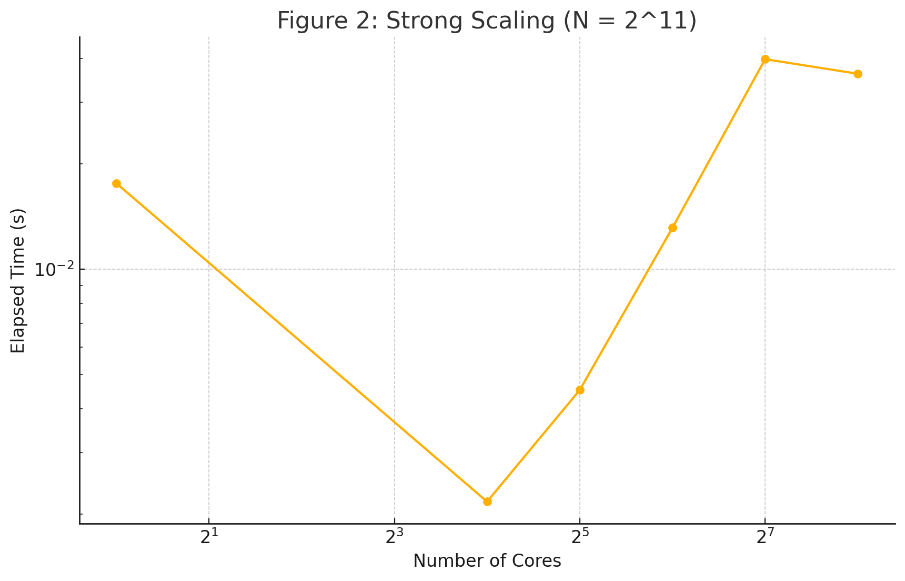
## Figure 1: Strong Scaling Curve with



## Table 2: Strong Scaling Curve with

|  |  |
| --- | --- |
|  | |
| Core Count | Elapsed Time (s) |
| 1 | 0.017609 |
| 16 | 0.002168 |
| 32 | 0.004520 |
| 64 | 0.013138 |
| 128 | 0.039841 |
| 256 | 0.036201 |

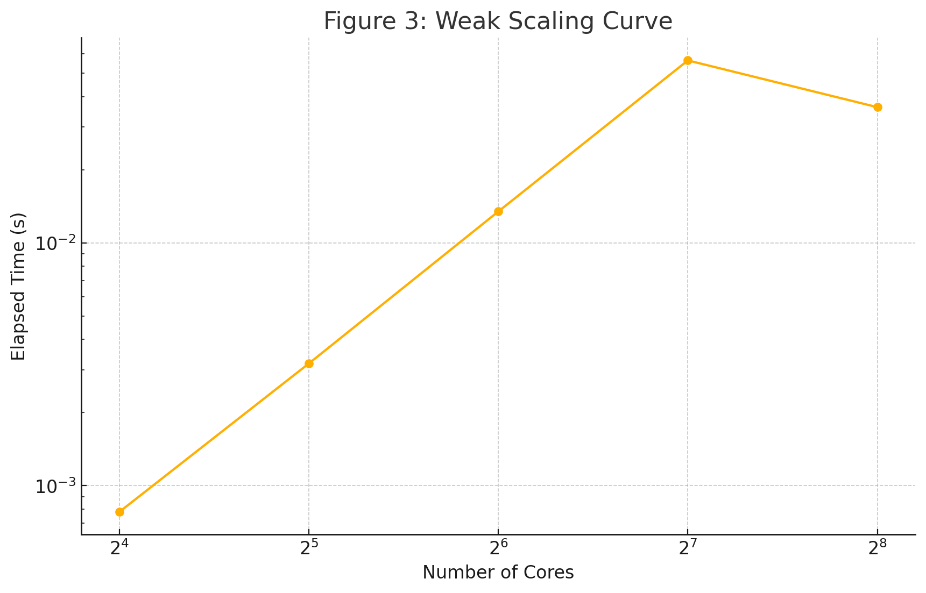
## Figure 2: Strong Scaling Curve with



## Table 3: Weak Scaling Curve with

|  |  |
| --- | --- |
|  | |
| N, Core Count | Elapsed Time (s) |
|  | 0.000779 |
|  | 0.003183 |
|  | 0.013461 |
|  | 0.056406 |
|  | 0.036201 |

## Figure 3: Weak Scaling Curve with



Ideal weak scaling keeps time nearly constant; here it increases from 0.78 ms (16 cores) to 56.4 ms (128 cores), then slightly improves at 256 cores (36.2 ms). The steep rise indicates that as the problem/processor ratio stays fixed, communication (point-to-point exchanges and global reductions) overhead grows super linearly.

# Discussion

## Strong Scaling

For both and , best speedup occurs at 16-32 cores. Beyond 32 cores, elapsed time increases markedly, communication/latency dominates over per-core computation. The overhead of exchanging vector segments and reductions outweighs local SpMV gains.

## Weak Scaling

Ideal weak scaling maintains constant runtime as both problem size and cores increase. Here, elapsed time grows over an order of magnitude from 16 to 256 cores, indicating significant overhead in distributed matrix-vector multiple times and global reductions.

## Overheads

P2P communication during SpMV and MPI\_Allreduce for dot-products contributes to the non-ideal scaling. For small to moderate core counts, computation dominates; at high counts, communication latency and load imbalance are limiting factors.

# Conclusion

The MPI-parallel CG solver shows modest strong scaling up to 32 cores. However, communication overhead severely limits both strong and weak scaling at larger scales. Future optimizations might include overlapping communication and computation, using nonblocking collectives, exploring hybrid MPI+OpenMP to reduce inter-node messages, and using topology-aware process mapping to minimize network hops.