

**Qa.**

1st plot shows the every random generated number U, and its corresponding  $X_a$  value.

2nd plot shows the histogram of both U and  $X_a$  for every value of U and  $X_a$

3rd plot show the cumulative sum of both U and  $X_a$  for every value of U and  $X_a$

If we were to make this simulation with 9 values:

U values are (0.1,0.2,0.3,0.4,0.5,0.6,0.7,0.8,0.9)

Corresponding  $X_a$  values would be (square root of U values)(0.31,0.44,0.54,0.63,0.7,0.77,0.83,0.89,0.94)

Sum of these values are 6.05

Divide this by 9 to get the average  $6.05/9 = 0.67 =$  Expected value of  $X_a$

Subtract the  $X_a$  values from 0.67 (0.36,0.23,0.13,0.04,0.03,0.1,0.16,0.22,0.27)

Take the squares of these values (0.1296,0.0529,0.016,0.0016,0.0009,0.01,0.025,0.0484,0.0729)

Sum of these values are 0.3564 , Then divide this by n-1 which is 8

$0.3564/8 = 0.044 =$  Variance of  $X_a$ .

In simulation we both find the same numbers more or less. Expected value and Variance holds.

**Qb.**

1st plot shows the accepted values for  $X_b$  value.

2nd plot shows the cumulative sum for the  $X_b$  values

Variance is more than it was in a since the range of our operation is now wider resulting in more different and discrete values which makes the variance larger.

Average is as expected larger than 0.5 and it is almost equal to avg  $X_a$