Note: The Elements of Computing Systems

September 12, 2020

# Preface

This is my study note for The Elements of Computing Systems (ISBN: 978-0262640688) by Noam Nisan and Shimon Schocken.

## Chapter 1

# Boolean Logic

Boolean Algebra

$$x \text{ or } y = \bar{x}y + x\bar{y} + xy$$

$$= \bar{x}y + x(y + \bar{y})$$

$$= x + \bar{x}y$$

$$= x + x + y = x + x + y = x + x + y = x + x + y = x + x + y = x + x + y = x + x + y = x + x + y = x + x + y = x + x + y = x + x + y = x + y + y = x + y + y = x + y + y = x + y + y = x + y + y = x + y + y = x + y$$

## Chapter 5

# Computer Architecture

### 5.1 Memory

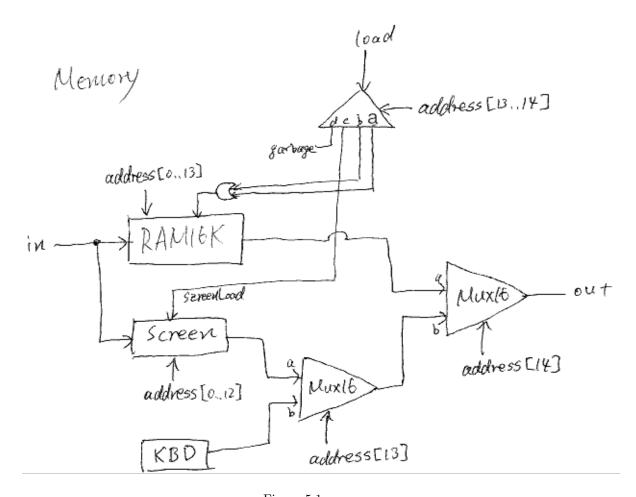


Figure 5.1: memory

#### 5.2 CPU

C-instruction =  $111ac_1c_2c_3c_4c_5c_6d_1d_2d_3j_1j_2j_3$ 

- $d_1$ : destination A
- $d_2$ : destination D
- $d_3$ : destination M

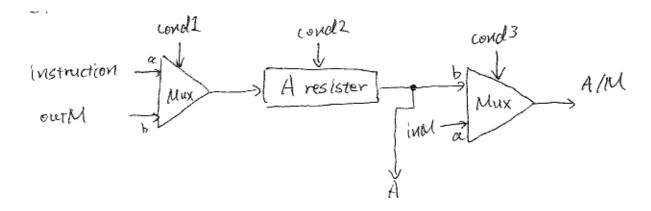


Figure 5.2: memory

cond1 = instruction[15] cond2 = (not instruction[15]) or (instruction[15]) and instruction[5])cond3 = instruction[15] and not instruction[12]

- instruction[15]: opcode
- instruction[12]: C-instruction's a. If a is 1, comp includes A, otherwise, comp includes M.
- instruction[5]: destination A.

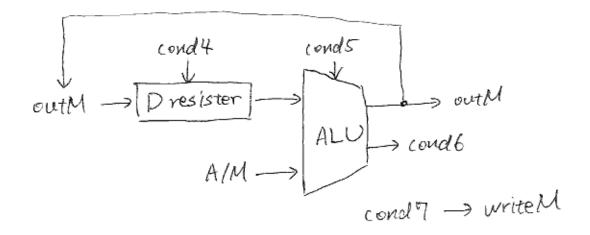


Figure 5.3: memory

$$\operatorname{cond4} = \operatorname{instruction}[15] \text{ and } \operatorname{instruction}[4]$$
 
$$\operatorname{cond5} = \begin{cases} \operatorname{zx} = \operatorname{instruction}[11] = c_1 \\ \operatorname{nx} = \operatorname{instruction}[10] = c_2 \\ \operatorname{zy} = \operatorname{instruction}[9] = c_3 \\ \operatorname{ny} = \operatorname{instruction}[8] = c_4 \\ \operatorname{f} = \operatorname{instruction}[7] = c_5 \\ \operatorname{no} = \operatorname{instruction}[6] = c_6 \end{cases}$$
 
$$\operatorname{cond6} = (\operatorname{zr}, \operatorname{ng})$$
 
$$\operatorname{cond7} = \operatorname{instruction}[15] \text{ and } \operatorname{instruction}[3]$$

• instruction[3]:  $d_3$ , destination M

5.2. *CPU* 9

• instruction[4]:  $d_2$ , destination D

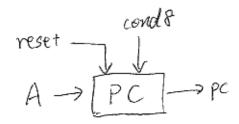


Figure 5.4: memory

$$\begin{aligned} & \operatorname{cond8} = & \overline{\operatorname{zr}} \cdot \overline{\operatorname{ng}} \cdot \overline{j_1} \cdot \overline{j_2} \cdot \overline{j_3} & (\operatorname{JGT}) \\ & + \overline{\operatorname{zr}} \cdot \overline{j_1} \cdot j_2 \cdot j_3 & (\operatorname{JEQ}) \\ & + \overline{\operatorname{ng}} \cdot \overline{j_1} \cdot j_2 \cdot j_3 & (\operatorname{JGE}) \\ & + \operatorname{ng} \cdot j_1 \cdot \overline{j_2} \cdot \overline{j_3} & (\operatorname{JLT}) \\ & + \overline{\operatorname{zr}} \cdot j_1 \cdot \overline{j_2} \cdot j_3 & (\operatorname{JNE}) \\ & + (\operatorname{zr} + \operatorname{ng}) \cdot j_1 \cdot j_2 \cdot \overline{j_3} & (\operatorname{JLE}) \\ & + j_1 \cdot j_2 \cdot j_3 & (\operatorname{JMP}) \end{aligned}$$

## Chapter 7

## Virtual Machine I: Stack Arithmetic

### 7.1 Arithmetic

```
// SP--
@SP
M=M-1

// D = y
A=M
D=M

// SP--
@SP
M=M-1

// *SP = y + x (add) / x - y (sub)
A=M
M=D+M (add) / M=M-D (sub)

// SP++
@SP
M=M+1
```

```
 \begin{cases} \  \  \, // \  \, \text{SP--} \\ \  \  \, \text{@SP} \\ \  \  \, \text{@M=M-1} \\ \  \  \, \  \, // \  \, \text{-M} \\ \  \  \, \text{A=M} \\ \  \  \, \text{M=-M (neg) / M=!M (not)} \\ \  \  \, \  \, \  \, \  \, // \  \, \text{SP++} \\ \  \  \, \text{@SP} \\ \  \  \, \text{M=M+1} \\ \end{cases}
```

```
// SP--
                   @SP
                   M=M-1
                   // D = y
                   D=M
                   // SP--
                   @SP
                   M=M-1
                   // x - y
                   A = M
                   D=M-D
eq, gt, lt \Rightarrow
                   // if condition then -1 else 0 end
                   @then
                   D;jEQ (eq), D;JGT (gt), D:JLT (lt)
                   @SP
                   A=M
                   M=O
                   @end
                   0;JMP
                (then)
                   @SP
                  A=M
                   M = -1
                (end)
                   @SP
                   M=M+1
```

### 7.2 logical command

where segment = local, argument, this, that.

$$\text{push temp i} \Rightarrow \left\{\begin{array}{l} *\text{SP} = *(\text{R5} + \text{i}) \\ \text{@R(5 + i)} \\ \text{D=M} \end{array}\right. \\ \Rightarrow \left\{\begin{array}{l} // *\text{SP} = *(\text{R5} + \text{i}) \\ \text{@SP} \\ \text{A=M} \\ \text{M=D} \end{array}\right.$$

$$\text{push static i} \Rightarrow \left\{\begin{array}{l} *\text{SP} = *\text{Xxx.i} \\ \text{0SP} \\ \text{A=M} \\ \text{M=D} \\ \text{0SP} \\ \text{M=M+1} \end{array}\right.$$

where this vm program name is Xxx.vm.

// SEG=SEG+i

@SEG

$$\begin{array}{c} D=M \\ @i \\ D=D+A \\ @SEG \\ M=D \\ \\ // SP-- \\ @SP \\ M=M-1 \\ \\ SP-- \\ *sEG = *SP \\ SEG = SEG - i \\ \\ \end{array} \Rightarrow \begin{cases} SEG = SEG + i \\ SP-- \\ *SEG = *SP \\ SEG = SEG - i \\ \\ \\ \end{pmatrix} // *SP \\ A=M \\ D=M \\ \\ // *SEG = *SP \\ @SEG \\ A=M \\ M=D \\ \\ // SEG=SEG-i \\ @i \\ D=A \\ @SEG \\ M=M-D \\ \end{array}$$

where segment = local, argument, this, that.

$$\begin{array}{l} \text{pop pointer } i \Rightarrow \left\{ \begin{array}{l} \text{SP--} \\ \text{*SP} \\ \text{*(R3 + i)} = \text{*SP} \end{array} \right. \Rightarrow \left\{ \begin{array}{l} \text{// SP--} \\ \text{@SP} \\ \text{M=M-1} \end{array} \right. \\ \text{@R(3 + i)} \\ \text{M=D} \end{array} \right. \\ \\ \text{pop temp } i \Rightarrow \left\{ \begin{array}{l} \text{SP--} \\ \text{*SP} \\ \text{*(R5 + i)} = \text{*SP} \end{array} \right. \Rightarrow \left\{ \begin{array}{l} \text{// SP--} \\ \text{@SP} \\ \text{M=M-1} \end{array} \right. \\ \text{// *SP} \\ \text{A=M} \\ \text{D=M} \end{array} \right. \\ \\ \text{@R(5 + i)} \\ \text{M=D} \end{array}$$

$$\text{pop static i} \Rightarrow \left\{ \begin{array}{l} \text{SP--} \\ \text{@SP} \\ \text{M=M-1} \end{array} \right. \\ \Rightarrow \left\{ \begin{array}{l} \text{M=M-1} \\ \text{M=M} \\ \text{D=M} \\ \text{@Xxx.i} \\ \text{M=D} \end{array} \right.$$