

MMAE 350: Computational Mechanics

Spring 2026

Department of Mechanical, Materials, and Aerospace Engineering
Illinois Institute of Technology

Instructor Information

- **Instructor:** Dr. Michael Gosz
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- **Office Hours:** TBA
- **Class Meetings:** Tue, Thur (11:25am -12:40pm) Stuart Building 113

Prerequisites

MATH 251 (Multivariate and Vector Calculus), MATH 252 (Intro to Differential Equations), MMAE 202 (Mechanics of Solids II). Programming background recommended.

Textbook

M. Gosz, *Computational Mechanics: A Modern Introduction with Machine Learning and AWS Workflows*, 1st edition. Other resources and handouts will be posted on the course Canvas site.

Course Description

This course introduces computational methods used in mechanical and aerospace engineering, with an emphasis on numerical solution of engineering governing equations. Students develop computational fluency using Python and Jupyter notebooks, apply finite-difference, finite-volume, and introductory finite-element methods, and connect numerical algorithms to physical conservation laws in heat transfer, wave propagation, and transport phenomena.

Learning Objectives

Upon successful completion of this course, students will be able to:

1. Develop and execute engineering computations using Python, NumPy, SymPy, and Jupyter notebooks.
2. Formulate and solve systems of linear algebraic equations arising from discretized engineering problems.
3. Apply numerical root-finding techniques, including Newton's method, to nonlinear equations and systems encountered in engineering analysis.
4. Derive finite-difference approximations for spatial and temporal derivatives and implement them for transient and steady-state problems.
5. Analyze the stability and accuracy of explicit and implicit numerical schemes for time-dependent partial differential equations.
6. Solve one- and two-dimensional heat conduction problems using finite-difference methods and matrix-based solution strategies.
7. Model wave propagation in elastic solids using explicit time-marching finite-difference schemes.
8. Apply finite-volume concepts to conservation laws and implement numerical solutions of advection–diffusion equations.
9. Distinguish between strong and weak formulations of governing equations and construct simple finite element approximations for one-dimensional problems.
10. Interpret numerical results in the context of physical behavior, assess solution quality, and communicate computational findings clearly.

Topics Covered

1. Introduction to computational mechanics and engineering workflows using Python and Jupyter notebooks
2. Matrix and vector algebra for engineering applications
3. Numerical solution of nonlinear equations and systems using Newton's method
4. Direct and iterative methods for solving systems of linear algebraic equations
5. Governing equations of heat transfer, wave propagation, and transport phenomena
6. Finite-difference methods for steady and transient partial differential equations
7. Stability and accuracy analysis of time-marching numerical schemes

8. Finite-volume methods for conservation laws and advection–diffusion problems
9. Introduction to weak formulations and one-dimensional finite element methods

Computer Usage

Students will use Python Jupyter Notebooks to complete assignments.

Grading Policy

Student performance in this course will be evaluated using the following components:

- **Homework Assignments (30%)**
Weekly or biweekly problem sets focused on analytical derivations, numerical methods, and short computational exercises.
- **Computational Notebooks and Labs (25%)**
Jupyter notebook assignments emphasizing implementation of numerical algorithms, interpretation of results, and clear documentation of computational workflows.
- **Midterm Exams (20% total; 10% each)**
Two in-class midterm exams, equally spaced throughout the semester, assessing conceptual understanding, mathematical formulation, and problem-solving skills for numerical methods covered up to each exam.
- **Final Exam or Final Project (25%)**
A comprehensive assessment or project evaluating students' ability to integrate numerical methods, physical modeling, and computational implementation for an engineering problem.

Course Calendar — Spring 2026

| Date | Day | Topic |
|--------|-----|---|
| Jan 13 | Tue | Course overview; role of computation in engineering; Python, Jupyter, and course workflow |
| Jan 15 | Thu | Arrays, vectors, and matrices in Python; numerical vs. symbolic computation |
| Jan 20 | Tue | Matrix algebra for engineering systems; solving linear systems |
| Jan 22 | Thu | Direct methods for linear systems: Gaussian elimination and LU decomposition |
| Jan 27 | Tue | Matrix structure and sparsity; tridiagonal systems and the Thomas algorithm |
| Jan 29 | Thu | Iterative solvers for linear systems; Gauss–Seidel method |
| Feb 03 | Tue | Nonlinear equations of one variable; Newton’s method |
| Feb 05 | Thu | Newton’s method for systems of equations; engineering examples |
| Feb 10 | Tue | Applications of nonlinear systems; conditioning and convergence |
| Feb 12 | Thu | Review and problem-solving session (Chapters 1–2) |
| Feb 17 | Tue | Exam 1 |
| Feb 19 | Thu | Derivation of the heat equation; boundary and initial conditions |
| Feb 24 | Tue | Finite-difference discretization of the 1D heat equation; FTCS method |
| Feb 26 | Thu | Stability analysis; CFL condition; von Neumann analysis |
| Mar 03 | Tue | Implicit time integration; Crank–Nicolson method |
| Mar 05 | Thu | Matrix formulation of transient heat conduction problems |
| Mar 10 | Tue | Two-dimensional heat conduction; five-point stencil |
| Mar 12 | Thu | Steady vs. transient 2D heat conduction; computational examples |
| Mar 17 | Tue | SPRING BREAK — No Class |

| Date | Day | Topic |
|--------|-----|--|
| Mar 19 | Thu | SPRING BREAK — No Class |
| Mar 24 | Tue | Wave propagation in elastic solids; 1D wave equation |
| Mar 26 | Thu | Explicit time-marching schemes; stability and the CFL condition |
| Mar 31 | Tue | Conservation laws and transport phenomena; integral vs. differential forms |
| Apr 02 | Thu | Finite-volume discretization of the advection–diffusion equation |
| Apr 07 | Tue | Upwind vs. central difference schemes; numerical diffusion |
| Apr 09 | Thu | Weak formulations; introduction to finite element concepts |
| Apr 14 | Tue | One-dimensional finite element method; shape functions and weak form |
| Apr 16 | Thu | Assembly of the global system; solution and interpretation |
| Apr 21 | Tue | Review for Exam 2 |
| Apr 23 | Thu | Exam 2 |
| Apr 28 | Tue | Computational project workshop; verification and validation |
| Apr 30 | Thu | Course synthesis; comparison of FD, FV, and FEM methods |
| May 05 | Tue | Final Exam or Project Presentations (Registrar-scheduled slot) |
| May 07 | Thu | Final Exam or Project Presentations (Registrar-scheduled slot) |

Course Policies

Attendance

Regular attendance is expected. Students are responsible for all material covered in class and all announcements made, regardless of attendance. Excessive unexcused absences may negatively impact your performance and grade.

Late Work

Assignments are due on the date and time specified. Late work will generally not be accepted unless prior arrangements are made with the instructor, or unless extraordinary cir-

cumstances can be documented. In such cases, partial credit may be given at the discretion of the instructor.

Academic Integrity

Illinois Tech expects all students to uphold the highest standards of academic honesty. Cheating, plagiarism, or any other form of academic dishonesty will not be tolerated. Violations will be reported and may result in failure of the assignment, failure of the course, and/or additional disciplinary action as outlined in the Illinois Tech Code of Conduct. For more information, see: <https://www.iit.edu/student-affairs/student-handbook>

Collaboration

Collaboration on homework assignments is permitted at the level of discussing concepts and approaches. However, all work turned in must be your own. Copying code, solutions, or written responses from another student or from online sources constitutes academic dishonesty.

Use of Technology

Students are encouraged to use Python, and other computational tools as required by the course. Any use of technology during quizzes or exams must be explicitly permitted by the instructor. Unauthorized use of technology during exams will be considered a violation of academic integrity.

Communication

Course announcements will be made in class and via email or the course LMS (Canvas). It is your responsibility to check email and the course site regularly. Email is the preferred method of communication outside of class hours.

Professional Conduct

Respectful behavior is expected in class, in labs, and in all course-related activities. Disruptive conduct will not be tolerated. Students should contribute to a learning environment that supports diversity of thought and experience.

Accessibility Statement

Illinois Tech is committed to providing an inclusive educational environment and making every effort to ensure equal access for all students. If you are a student with a documented disability and require reasonable academic accommodations, please contact the Center for Disability Resources (CDR) as soon as possible. Accommodations are determined on a case-by-case basis, considering the student's documented needs and the technical requirements of the course.

To request accommodations or learn more, contact:

- **Center for Disability Resources (CDR)**
Phone: 312-567-5744
Email: disabilities@illinoistech.edu

Students must submit documentation and meet with CDR to establish eligibility and receive an accommodation letter. Provide your letter to the instructor early in the semester to discuss appropriate implementation of accommodations.

For more information, visit: <https://www.iit.edu/cdr>

University Academic Calendar — Spring 2026

| Date | Event |
|-------------|--|
| January 12 | Spring Courses Begin |
| January 19 | Martin Luther King, Jr. Day — No Classes |
| January 20 | Last Day to Add/Drop for Full Semester Courses with No Tuition Charges |
| January 27 | Last Day to Request Late Registration |
| March 13 | Midterm Grades Due |
| March 16–21 | Spring Break Week — No Classes |
| March 30 | Last Day to Withdraw for Full Semester Courses |
| April 6 | Fall Registration Begins |
| May 2 | Last Day of Spring Courses |
| May 3 | Last Day to Request an Incomplete Grade |
| May 4–9 | Final Exam Week (Final Grading Begins May 4) |
| May 13 | Final Grades Due at Noon (CST) |