

Aim:

Given a graph G and source vertex S , Dijkstra's shortest path algorithm is used to find the shortest paths from source S to all vertices in the given graph.

The Dijkstra algorithm is also known as the single-source shortest path algorithm. It is based on the greedy technique. A little variation in the algorithm can find the shortest path from the source nodes to all the other nodes in the graph.

The function `void dijkstra(int G[MAX][MAX], int n, int startnode)` computes and prints the shortest path distances and corresponding paths from the given source node to all other nodes in a weighted directed graph using Dijkstra's algorithm. It outputs the distance or "INF" if unreachable, along with the path or "NO PATH" for each node.

Note:

- Vertices are numbered from 1 through V .
- All input values are separated by spaces and/or newlines.

Sample Input and Output:

```
Enter the number of vertices : 4
Enter the number of edges : 5
Enter source : 1
Enter destination : 2
Enter weight : 4
Enter source : 1
Enter destination : 4
Enter weight : 10
Enter source : 1
Enter destination : 3
Enter weight : 6
Enter source : 2
Enter destination : 4
Enter weight : 5
Enter source : 3
Enter destination : 4
Enter weight : 2
Enter the source :1
```

Node	Distance	Path
2	4	2<-1
3	6	3<-1
4	8	4<-3<-1

Source Code:

Dijkstras.c

```
#include <limits.h>
#include <stdio.h>
#define MAX 20
int V, E;
int graph[MAX][MAX];
```

```

#define INFINITY 99999
void printPath(int parent[], int j) {
    int path[MAX];
    int pathIndex = 0;

    // Collect path from destination to source
    while (j != -1) {
        path[pathIndex++] = j;
        j = parent[j];
    }

    // Now print in reverse: destination <- ... <- source
    for (int i = 0; i < pathIndex; i++) {
        printf("%d", path[i]);
        if (i < pathIndex - 1) {
            printf("<-");
        }
    }
}

void dijkstra(int G[MAX][MAX], int n, int startnode) {
    int distance[MAX];
    int visited[MAX] = {0};
    int parent[MAX];

    for (int i = 1; i <= n; i++) {
        distance[i] = INFINITY;
        parent[i] = -1;
    }
    distance[startnode] = 0;

    for (int count = 1; count <= n - 1; count++) {
        int min = INFINITY, u = -1;
        for (int i = 1; i <= n; i++) {
            if (!visited[i] && distance[i] <= min) {
                min = distance[i];
                u = i;
            }
        }

        if (u == -1) break;

        visited[u] = 1;

        for (int v = 1; v <= n; v++) {
            if (!visited[v] && G[u][v] != 0 && distance[u] != INFINITY &&
                distance[u] + G[u][v] < distance[v]) {
                distance[v] = distance[u] + G[u][v];
                parent[v] = u;
            }
        }
    }

    // write your code here
    printf("Node\tDistance\tPath\n");
    for (int i = 1; i <= n; i++) {
        if (i == startnode) continue;

```

```

// Print node with 3 leading spaces and arrow
printf("   %d\t", i);

if (distance[i] == INFINITY) {
    // 7 spaces after arrow
    printf("      INF\tNO PATH\n");
} else {
    // Print distance followed by 7 spaces, then arrow and path
    printf("      %d\t", distance[i]);
    printPath(parent, i);
    printf("\n");
}
}
}

int main() {
    int s, d, w, i, j;
    printf("Enter the number of vertices : ");
    scanf("%d", &V);
    printf("Enter the number of edges : ");
    scanf("%d", &E);
    for(i = 1 ; i <= V; i++) {
        for(j = 1; j <= V; j++) {
            graph[i][j] = 0;
        }
    }
    for(i = 1; i <= E; i++) {
        printf("Enter source : ");
        scanf("%d", &s);
        printf("Enter destination : ");
        scanf("%d", &d);
        printf("Enter weight : ");
        scanf("%d", &w);
        if(s > V || d > V || s <= 0 || d <= 0) {
            printf("Invalid index. Try again.\n");
            i--;
            continue;
        } else {
            graph[s][d] = w;
        }
    }
    printf("Enter the source :");
    scanf("%d", &s);
    dijkstra(graph, V, s);
    return 0;
}

```

Execution Results - All test cases have succeeded!

Test Case - 1
User Output
Enter the number of vertices : 4
Enter the number of edges : 5
Enter source : 1
Enter destination : 2

Enter weight : 4
Enter source : 1
Enter destination : 4
Enter weight : 10
Enter source : 1
Enter destination : 3
Enter weight : 6
Enter source : 2
Enter destination : 4
Enter weight : 5
Enter source : 3
Enter destination : 4
Enter weight : 2
Enter the source : 1
Node Distance Path
2 4 2<-1
3 6 3<-1
4 8 4<-3<-1

Test Case - 2		
User Output		
Enter the number of vertices : 5		
Enter the number of edges : 6		
Enter source : 1		
Enter destination : 2		
Enter weight : 2		
Enter source : 1		
Enter destination : 5		
Enter weight : 3		
Enter source : 2		
Enter destination : 4		
Enter weight : 4		
Enter source : 2		
Enter destination : 3		
Enter weight : 7		
Enter source : 4		
Enter destination : 3		
Enter weight : 2		
Enter source : 5		
Enter destination : 4		
Enter weight : 1		
Enter the source : 2		
Node	Distance	Path
1	INF	NO PATH
3	6	3<-4<-2
4	4	4<-2
5	INF	NO PATH

Test Case - 3		
User Output		
Enter the number of vertices : 4		

Enter the number of edges : 5		
Enter source : 1		
Enter destination : 2		
Enter weight : 4		
Enter source : 3		
Enter destination : 2		
Enter weight : 5		
Enter source : 4		
Enter destination : 1		
Enter weight : 1		
Enter source : 4		
Enter destination : 2		
Enter weight : 3		
Enter source : 4		
Enter destination : 3		
Enter weight : 8		
Enter the source : 1		
Node	Distance	Path
2	4	2<-1
3	INF	NO PATH
4	INF	NO PATH