# Template to prepare preprints and manuscripts using markdown and github actions

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Abstract: TBD

## **Introduction**

- 2 Earth's ecosystems are changing due to human activity.
- 3 However, we currently lack the data collected in a systematic way to adaquetly attribute change in
- 4 biodiversity to particular drivers, and to filter out inherent temporal variation in ecological processes from
- 5 deviations toward non-stationarity (TODO: wording) (AndyDNAPaper?).
- 6 Sampling is expensive.
- What is a BON? Talk about other important aspects of this framework. We want the data to be open. We
- 8 want to encourage colloboration across scales. Not top-down.

### 9 Methods

#### 10 Combining many geospatial layers into a priority map

- A set of geospatial layers, which potentially represent many different types of information. Here we
- consider each layer to fall into one of three categories: (1) ecological layers, which represent information
- about biological processes, e.g. species richness, trend in abundance, uncertainty in species occurrence,
- etc. (2) environmental layers, which represent information about the abiotic environment, e.g. climatic
- information, land-cover, elevation, climate velocity and uniqueness, and son. Finally, (3) cost layers:
- e.g. the physical accessability of certain locations, the amount of money per unit of time spend sampling a
- given location, etc. We denote the value of an arbitrary layer  $L_i$  at the coordinate (x, y) as  $L_i^{(x,y)}$ . We also
- denoted a generic function  $g(L_i)$  where returns the group (ecological, environmental, cost) that the
- particular  $L_i$  belongs to. We also define a set of targets, which are the objective information to be obtained
- via sampling. (examples here).
- The fundemental objects here are the weights matrix **W**, and mixing vectors  $\gamma$  and  $\phi$ . The weights matrix
- $_{22}$  **W** is an  $\mathcal{L} \times \mathcal{T}$  matrix, where  $\mathcal{L}$  and  $\mathcal{T}$  are the number of layers and targets respectively. The value of  $\mathbf{w}_{i,t}$
- is the relative importance of the i-th layer to the t-th target compared to all of the other layers in the group
- the *i*-th layer is in,  $g(L_i)$ . From this, and the layer group mixing vector  $\phi$ , we can compute single layers for
- each target, where we similarly denote the value *i*-th target at location (x, y) as  $T_i^{(x,y)}$ . This can be

26 computed as

$$T_i^{(x,y)} = \sum_j \gamma_{g(L_j)} \cdot \mathbf{w}_{j,i} \cdot L_j^{(x,y)}$$

or in slightly more compact matrix form

$$\vec{\mathbf{T}}^{(x,y)} = \mathbf{W}^T(\vec{\gamma}^* \circ \vec{\mathbf{L}}^{(x,y)})$$

- where  $\vec{\gamma}^*$  is a vector of length  $\mathcal L$  where  $\gamma_i^*=g(L_i)$ .
- 29 Finally, these target layers can then be combined into a single map as a weighted average based on the
- target mixing weights  $\phi$ , i.e. the priorty map **P** at (x, y) can be computed as

$$\mathbf{P}^{(x,y)} = \sum_{i} \phi_i T_i^{(x,y)}$$

or in its complete matrix form

$$\mathbf{P}^{(x,y)} = \mathbf{W}^T(\vec{\gamma}^* \circ \mathbf{L}^{(x,y)}) \cdot \phi$$

where  $\circ$  is the element-wise product and  $\cdot$  is the inner product

[Figure 1 about here.]

#### 34 Point selection algorithms

- There is a long history of discourse in the literature about choosing a set of coordinates within a spatial
- 36 domain that will result in a "best" sample.
- Environmental uniqueness
- Spatial balance

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- Whatever the fuck cube sampling is doing
- Particular scale-dependence weirdness in ecology

#### 41 Choosing and optimizing weights

- There are a lot of caveats here.
- Rarely is there relevant available data from which to derive an evidence-based choice of the relative importance of each layer toward sampling targets.
- Often knowledge of species life-history matters for this, requires experts on particular species
- There is no a priori reason to believe there will be a positive trade-off possible between two targets.
- A particular choice of weight matrix may produce a priority map that is very sensitive to minor changes in the weights
- We should try to validate that our sampling sites work well, but this is a chicken and egg problem
  with our current data. So we want a max-entropy approach to real distributions from which we
  sample possible realized sampling outcomes and compare as we tweak weights.
  - Need to assert the constraint that

$$\frac{\partial \mathbb{L}_i}{\partial T_i} > 0$$

or otherwise that means the weights are not actually suited toward targets

Target tradeoffs

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[Figure 2 about here.]

- 56 Sensitivity analysis
- 57 Validation through simulation of the sampling process
- 58 Case study: bird (or perhaps non migratory?) species TBD in Quebec
- 59 Discussion

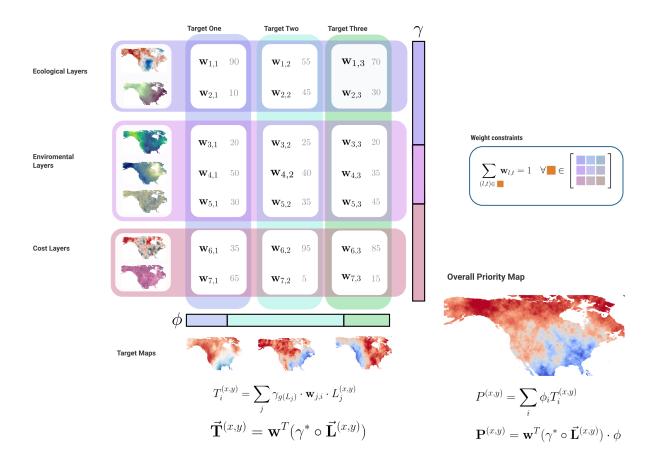


Figure 1: todo

# **Error trade-off across targets**

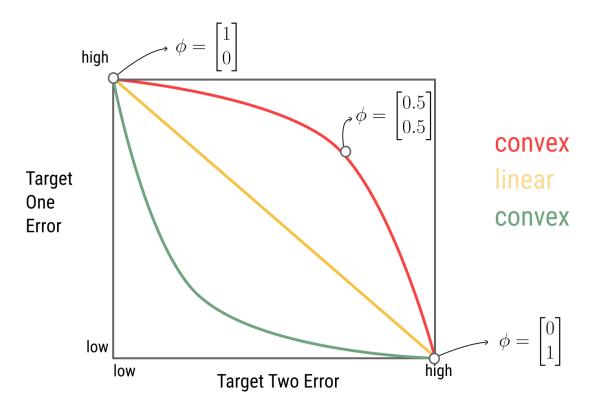


Figure 2: todo