Independent Component Analysis (ICA): An Introduction

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Overview

The following will be introduced:

- 1 The Cocktail Party Problem
 - also known as Blind Source Separation (BSS).
- Independent Component Analysis (ICA)
 - the model for solving BSS.
- My interest in ICA and BSS.

The Cocktail Party Problem

Picking a voice out of a crowd

- You attend a busy cocktail party...
- Lots of guests speaking simultaneously.
- You focus on each voice.
- How can a computer do this? (ICA)

Demonstration



Web demo: Cocktail Party Problem

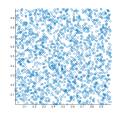
Independent Component Analysis (ICA)

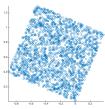
Latent variable model:

$$\mathbf{x} = \mathbf{A}\mathbf{s} \tag{1}$$

- s: source signals.
- x: mixtures (observations).
- A: mixing matrix.
 Determines how much of each source is in each mixture.

ICA Principles





Assume the sources are...

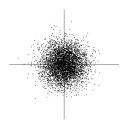
- Statistically independent.
- Non-Gaussian (due to Central Limit Theorem).

Retrieve sources by...

• Rotating mixtures to *maximize independence*.



Problems with ICA



- For Gaussian sources, rotation will not work!
- Linear, noiseless model: what about distortions?

ICA Applications

Image denoising

Original



Noisy



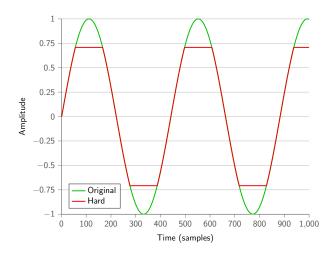


ICA filter

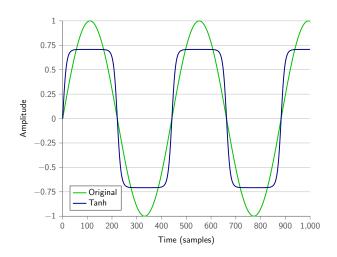
Distortion

- What if the mixtures are distorted?
- Now, we don't have a linear mixture.
- Peak clipping: a common distortion encountered in signal processing.

Clipped sine wave Hard clipping example



Clipped sine wave Soft clipping example



For Further Reading

- Hyvärinen, A., Karhunen, J. and Oja, E. Independent component analysis. New York: J. Wiley, 2001.
- Hyvärinen, A., Oja, E. Independent component analysis: algorithms and applications. *Neural networks*, 13(4):411–430, 2000.