

- Administrivia
 - HW2 due on Friday
 - Any other questions
 - Office hours canceled today to make sure we get enough time for grading
 - Will make up with 2x office hours at a high-demand time
- Last time
 - Talked about linked lists, something you learned about in depth in your lab
 - Checking in: things you should understand about abstract data types
 - They're abstract! Implementation separate from function.
 - Function of Lists
 - How to implement an array-backed list
 - How to implement a linked list
- Today: intro to algorithmic efficiency
 - Place add(E o), add (int index, E o), get(int index), E remove(int index), E set(int index, E o), int size() in terms of execution speed
 - 5 minutes
 - Right side of the room: ArrayLists or array-backed lists
 - Left side of the room: Linked lists
 - Teams of two
 - Don't want to see anyone on their laptop doing anything but this, this is important
 - Going to need a volunteer on each side to justify their decision
 - If the list gets bigger, what's the effect at the top of the rankings, bottom?
- Capture what we've seen so far
 - Constant time
 - Size, get, set for array-backed
 - What for linked list
 - Linear time
 - Add, remove, indexOf/contains for array-backed
 - Two key concepts here
 - Problem size: n! (number of operations)
 - Growth functions or O
- Let's get more complex
 - Hypothetical algorithm that implements countOccurrences
 - SLIDE:


```

2
3 public static void countOccurrences(int[] a) {
4     for (int i = 0; i < a.length; i++) {
5         int count = 1;
6         for (int j = 0; j < a.length; j++) {
7             if ( (j != i) && a[i] == a[j] )
8                 count++;
9         }
10
11         System.out.format("# of occurrences of %s = %d\n",
12                             a[i], count);
13     }
14 }
15
          
```
 - Walk through code
 - If n is the length of a, how many times does each line of code run?
 - 1 = N

- $2 = N$
 - $3 = N$
 - $4 = N * N$
 - $5 = N * (N-1)$
 - $6 = N$
- Adding everything up
 - $N^2 + N(N-1) + 4N$
 - $N^2 + N^2 - N + 4N$
 - $2N^2 + 3N$
- We say $O(N^2)$
 - Count only the “highest order” term
 - Ignore lower order terms, including constants
 - Ignore multiplier on the highest order term
- What if we said, only count up to five occurrences? What would be the effect on O ?
- To be clear
 - Why are
 - $5N^2$
 - $10N^2 + 1000N + 1,000,000$
 - $0.0001N^2$
 - The same? (Why do we just care about $O(N^2)$?)
 - And why is?
 - $F1(n) = 1000N$ faster than
 - $F2(n) = 0.01N^2$
- A: Big data
 - We only care about large problems (large N), and for large problems the higher order term dominates
 - For small problems, efficiency isn't that important
- So, what do we have here in terms of the concepts we discussed earlier?
 - New growth function
 - Polynomial
- Challenge problems
 - 5-min: Design an algorithm that counts the number of occurrences in a list in $O(n)$
 - 5-min: Returning to contains()...Introduce binary sort
 - Q: What is the efficiency of binary sort?