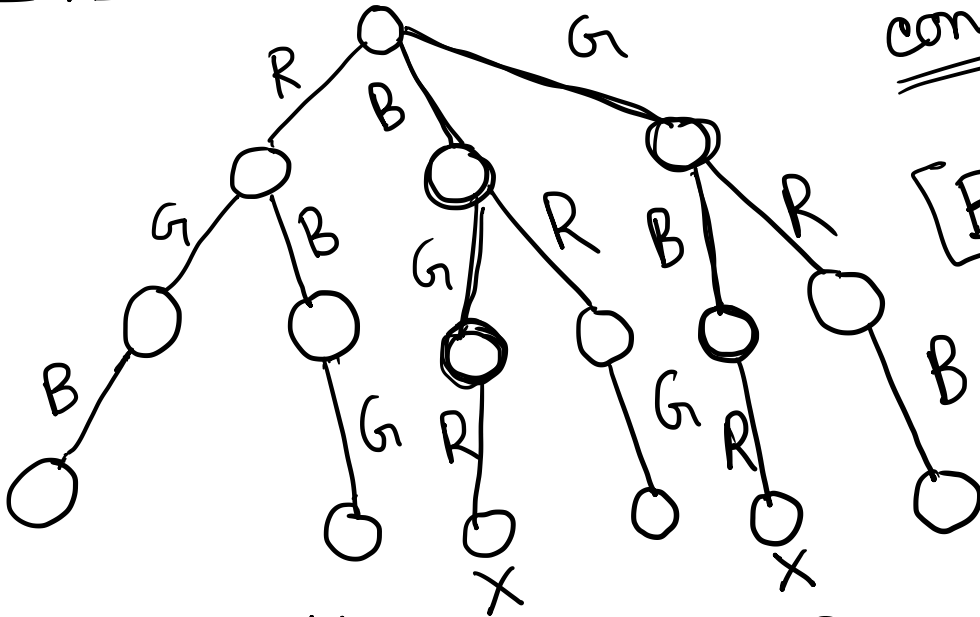


↙ Backtracking → Another algorithm design technique

We will find all solutions.
(Brute force approach)

Balls: R G B

State space tree:



Backtracking
↓
constraint
⇓
[Bounding
function]

N-Queen's problem: Place n -queens in a $n \times n$ chessboard so that no two of them can attack.
i.e. no two of them are on the same row, column or diagonal.

	1	2	3	4	5	6	7	8
1				Q				
2						Q		
3								Q
4		Q						
5								
6	Q							
7				Q				
8						Q		

8x8 chessboard

$n=8$

Solution: (4,6,8,2,7,1,3,5)

(3,1) (4,2) (5,3) (6,4)
Let, (i,j) & (k,l)
are in same
diagonal.

(5,8) (6,7) (7,6) (8,5)
Let, (i,j) & (k,l)
are in same
diagonal.

$$\begin{aligned} \rightarrow (i-j) &= (k-l) \\ \Rightarrow (j-l) &= (i-k) \end{aligned}$$

$$\begin{aligned} \rightarrow (i+j) &= (k+l) \\ \Rightarrow (j-l) &= (k-i) \end{aligned}$$

$$\begin{aligned} \text{abs}(j-l) &= \text{abs}(i-k) \end{aligned}$$

4x4 chessboard:

	1	2	3	4
1	1			
2				
3				
4				

	1			
	.	.	2	

	1			
.	.	2		
.	.	.	.	

	1			
.	.	.	2	
.	3	.	.	
.	.	.	.	

.	1			
.	.	.	2	

.	1			
.	.	.	2	
3				

	1	2	3	4
1	.	1		
2	.	.	.	2
3	3			
4	.	.	4	

(2,4,1,3) \Rightarrow Solution 1
(3,1,4,2) \Rightarrow Solution 2

Algorithm NQueens(k, n)

{ // print all possible solutions using
// backtracking

for $i := 1$ to n do

{ if (Place(k, i)) then

Global solution array \rightarrow { $x[k] := i$
if ($k = n$) then
print ($x[1:n]$)
else
NQueens($k+1, n$)
}

}

Algorithm Place(k, i)

{ // returns true if Q is placed at k -th row
// and i -th column, otherwise returns false

for $j := 1$ to $(k-1)$ do // check for all previous queens.

{ if ($(x[j] = i)$ // in the same column
or ($\text{Abs}(x[j] - i) = \text{Abs}(j - k)$)) then
// in the same diagonal
return false

}
return true

}