

# MST:

MST-PRIM( $G, w, r$ )

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1 for each  $u \in G.V$ 
2    $u.key = \infty$ 
3    $u.\pi = NIL$ 
4  $r.key = 0$ 
5  $Q = G.V$ 
6 while  $Q \neq \emptyset$ 
7    $u = \text{EXTRACT-MIN}(Q)$ 
8   for each  $v \in G.Adj[u]$ 
9     if  $v \in Q$  and  $w(u, v) < v.key$ 
10       $v.\pi = u$ 
11       $v.key = w(u, v)$ 

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$O(V)$  time  $\Rightarrow$  Line 1-5

BUILD-MIN-HEAP

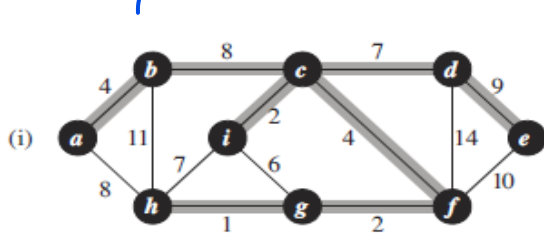
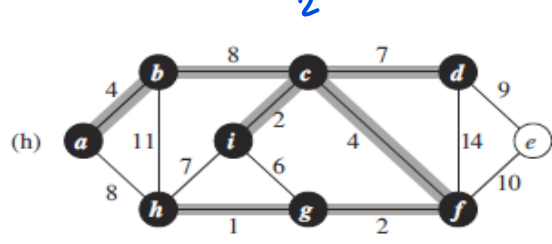
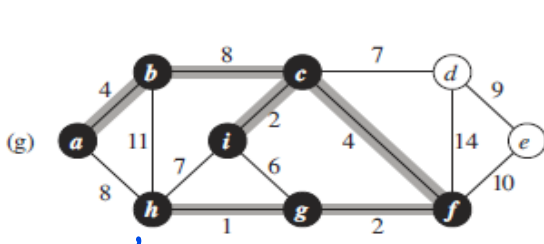
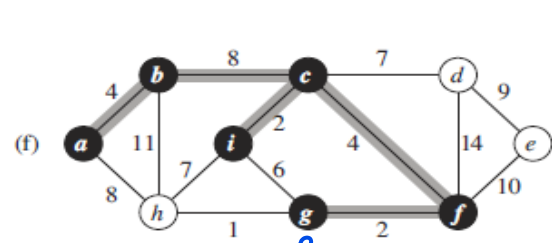
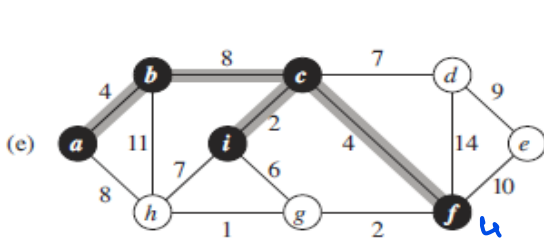
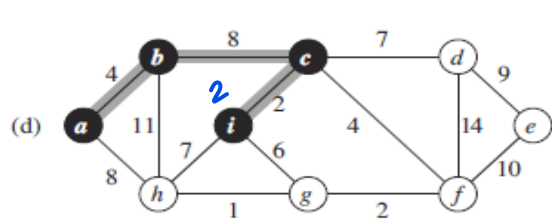
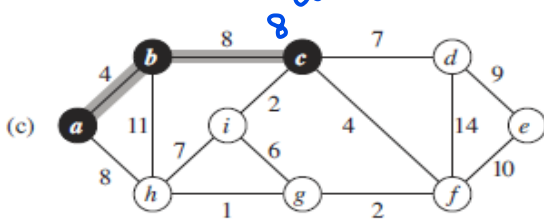
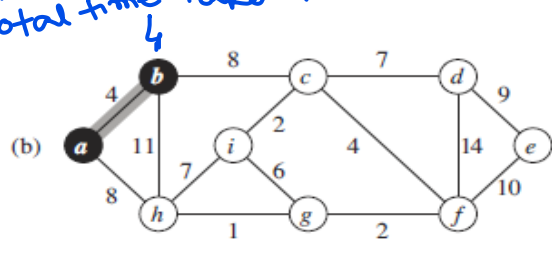
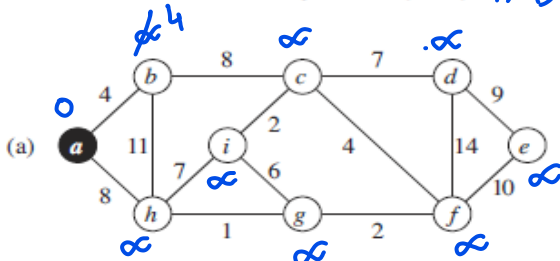
Each operation takes  $O(\log V)$   
Total time taken in EXTRACT-MIN for all vertices  $O(V \log V)$

Time complexity =  $O(E \log V + V \log V)$

$= O(E \log V)$   
(As  $|E| \geq |V| - 1$ )

$4 < \infty$

DECREASE-KEY  $\Rightarrow O(\log V)$   
Total time taken in this step =  $O(E \log V)$



MST: Total weight = 37

