

# RAJIV GANDHI INSTITUTE OF PETROLEUM TECHNOLOGY, JAIS AMETHI

**B. Tech. – I<sup>st</sup> Year (Even Semester)**  
**End Semester Examination**  
**Question Paper for Modern Physics (PY-112)**  
**SECTION - B**

TIME: 1 hour

[MAX. MARKS: 30]

- **Instructions: Attempt all questions**

1. The normalized ground state wavefunction of the electron in the hydrogen atom is

$$\psi(r\theta\Phi) = \frac{1}{\sqrt{\pi}} \left( \frac{1}{a_0} \right)^{3/2} e^{-r/a_0}$$

- (a) Calculate the probability of finding the electron in the range  $a_0/2 < r < 3a_0/2$ .  
(b) Sketch the probability density as a function of  $r$ . At what value of  $r$ , it is maximum.  
What would be the corresponding probability for a classical orbit?  
(c) Calculate the average radius of hydrogen atom? **[10 MARKS]**

2. The  $J = 0 \rightarrow J = 1$  rotational absorption line occurs at  $1.153 \times 10^{11}$  cycles/sec in  $^{12}\text{C } ^{16}\text{O}$  and at  $1.102 \times 10^{11}$  cycles/sec in  $^x\text{C } ^{16}\text{O}$ . Calculate the mass number ( $x$ ) of the unknown carbon isotope. (Consider that the internuclear distance remains unchanged on the isotopic substitution). **[6 MARKS]**

3. (a) Calculate the uncertainty in the measurement of momentum of an electron if the uncertainty in its location is  $1 \text{ \AA}$ . **[4 MARKS]**

- (b) What is the de Broglie wavelength of thermal neutron at 300 K? **[4 MARKS]**

4. Sketch the wavefunction  $\psi(x)$  and probability density  $P(x)$  of the particle of energy ( $E < V_0$ ) penetrating through the barrier ( $V_0$ ) in region I, region II & region III as shown in figure below: **[6 MARKS]**

