

# NUMBER SYSTEMS

## 1. Introduction:

In your earlier classes, you have learnt about the number line and how to represent various types of numbers on it.

The number line

Just imagine you start from zero and go on walking along this number line in the positive direction.

As far as your eyes can see, there are numbers, numbers and numbers!

## 2. Notes:

- There are infinitely many rational numbers between any two given rational numbers.
- A number 's' is called irrational, if it cannot be written in the form  $\frac{p}{q}$ , where p and q are integers and  $q \neq 0$ .
- The decimal expansion of an irrational number is non-terminating non-recurring. Moreover, a number whose decimal expansion is non-terminating non-recurring is irrational.

## 3. Example Sums:

\*Find five rational numbers between 1 and 2. We can approach this problem in at least two ways. Solution 1 :

Recall that to find a rational number between r and s, you can add r and s and divide the sum by 2, that is  $\frac{r+s}{2}$  lies between r and s. So,  $\frac{1+2}{2} = \frac{3}{2}$  is a number between 1 and 2. You can proceed in this manner to find four more rational numbers between 1 and 2. These four numbers are  $\frac{5}{4}$ ,  $\frac{11}{8}$ ,  $\frac{13}{8}$  and  $\frac{7}{4}$ .

\* :Locate  $\sqrt{2}$  on the number line. Solution :

It is easy to see how the Greeks might have discovered  $\sqrt{2}$ . Consider a square OABC, with each side 1 unit in length (see Fig. 1.6). Then you can see by the Pythagoras theorem that  $OB = \sqrt{1^2 + 1^2} = \sqrt{2}$ . How do we represent  $\sqrt{2}$  on the number line? This is easy. Transfer Fig. 1.6 onto the number line making sure that the vertex O coincides with zero (see Fig. 1.7). Fig. 1.7 We have just seen that  $OB = \sqrt{2}$ . Using a compass with centre O and radius OB, draw an arc intersecting the number line at the point P. Then P corresponds to  $\sqrt{2}$  on the number line.

\*Show that  $0.\overline{3} = \frac{1}{3}$  can be expressed in the form  $\frac{p}{q}$ , where  $p$  and  $q$  are integers and  $q \neq 0$ .

Solution : Since we do not know what  $\frac{1}{3}$  is, let us call it 'x' and so  $x = 0.\overline{3}$ . Now here is where the trick comes in. Look at  $10x = 10 \times (0.\overline{3}) = 3.\overline{3}$ . Now,  $3.\overline{3} = 3 + x$ , since  $x = 0.\overline{3}$ . Therefore,  $10x = 3 + x$ . Solving for  $x$ , we get  $9x = 3$ , i.e.,  $x = \frac{1}{3}$ .

#### 4. Practice sums:

\*Find five rational numbers between  $\frac{3}{5}$  and  $\frac{4}{5}$ .

\*Show how  $\sqrt{5}$  represents on number line.

\* Express the following in the form  $\frac{p}{q}$ , where  $p$  and  $q$  are integers and  $q \neq 0$ . (i)  $0.\overline{6}$ . (ii)  $0.\overline{47}$