

P1. (15 points) Fill-out the edit distance table for the words **NONSTOP** and **ROUND**. An empty table is provided below. Fill-out however much you need.

	"	N	O	N	S	T	O	P	
"	0	1	2	3	4	5	6	7	
R	1↑	1↖	2↖	3↖	4↖	5↖	6↖	7↖	
O	2↑	2↖	1↖	2↖	3↖	4↖	5↖	6↖	
U	3↑	3↖	2↖	2↖	3↖	4↖	5↖	6↖	
N	4↑	3↖	3↑	2↖	3↖	4↖	5↖	6↖	
D	5↑	4↖	4↖	3↑	3↖	4↖	5↖	6↖	

P2. (10 points)

a) (4 points) Show the solution path on the table (bold, highlight or circle the cells). If two directions give the optimal cost, give preference in this order: diagonal, left, up

		a	s	t	e	r	n
	0	1	2	3	4	5	6
s	1	1	1	2	3	4	5
t	2	2	2	1	2	3	4
r	3	3	3	2	2	2	3
e	4	4	4	3	2	3	3
n	5	5	5	4	3	3	3
g	6	6	6	5	4	4	4
t	7	7	7	6	5	5	5
h	8	8	8	7	6	6	6

b) In the table below the symbols indicate: \ - diagonal, ^ - up arrow, < - left arrow

		r	e	g	r	e	s	s	i	o	n
	<	<	<	<	<	<	<	<	<	<	<
s	^	\	\	\	\	\	\	\	<	<	<
e	^	\	\	<	<	\	<	\	\	\	\
g	^	\	^	\	<	<	<	<	<	<	<
m	^	\	^	^	\	\	\	\	\	\	\
e	^	\	\	^	\	\	<	<	<	<	<
n	^	\	^	^	\	^	\	\	\	\	\
t	^	\	^	^	\	^	\	\	\	\	\

b1) (2 points) Show in the symbols table the path you followed (e.g. bold, highlight, circle).

b2) (3 points) Show all 3 strings: the 2 strings that show the word alignments and the 3rd one showing the cost.

REGRESSION
 1 1 0 1 0 1 1 0 1 1 1 1 1 1
 SEGMENT - - -
 Distance = 7

REGRESSION
 1 1 1 1 1 1 1 1 1 1 1 1 1 1
 - - - - SEGMENT
 Distance = 9

b3) (1 point) Using the 3rd string, what is the edit distance between these 2 strings?

Edit distance between 2 strings : 2

P3 (10 points) (Stair climbing with gain)

The jump sizes below have the given gain (e.g. health points). You can assume that any other jump size is allowed, but has 0 health points.

Jump size:	4	6	10	12
Gain (Health points):	10	21	33	36

a) (7 points) Fill out the solution array, sol, using bottom-up dynamic programming. Follow the style we did in class: for each work-out box (in rows for jump sizes 4,6,10,12) show the remaining stairs and the optimal value obtained by using that jump size Fill-out all the table (starting from 0).

	0	1	2	3	4	5	6	7	8	9	10	11	12
Sol:	0	0	0	0	10	10	21	21	21	21	33	33	42
Picked	-	-	-	-	4	4	6	6	6	6	10	10	6
4, 10	-	-	-	-	0, 10	1, 10	2, 10	3, 10	4, 20	5, 20	6, 31	7, 31	8, 31
6, 21	-	-	-	-	-	-	0, 21	1, 21	2, 21	3, 21	4, 31	5, 31	6, 42
10, 33	-	-	-	-	-	-	-	-	-	-	0, 33	1, 33	2, 33
12, 36	-	-	-	-	-	-	-	-	-	-	-	-	0, 36

b) (3 points) Use the table above to recover the jumps that achieve the optimal value for 12 stairs.

For size 12, Remaining Weight = $12 - 6 = 6$
 For size 6, Remaining Weight = $6 - 6 = 0$

Jumps that achieve optimal value for 12 stairs = 6, 6
 Total health points gained = $21 + 21 = 42$

P3 (15 pts) Solve the Weighted Job Scheduling problem below. Recover the solution.

a) (10 pts) Use Dynamic Programming to solve the Weighted Job Scheduling below for jobs 1-6 with job values given by v_i .

b) (5 pts) Backtrack the solution (fill in in the rightmost column).

P3)

i	1	2	3	4	5	6	7	8
1								
2								
3								
4								
5								
6								

i	v_i	p_i	$m(i)$	$m(i)$ used i: Y/N	In opt solution: Y/N
0	0	0	0	-	-
1	4	0	4	Yes	yes
2	3	0	4	No	-
3	4	1	8	Yes	yes
4	5	2	9	Yes	-
5	3	2	9	No	-
6	2	3	10	Yes	yes

Maximum value picked : \$10

Jobs picked : 6, 3, 1