# **Gov 50: 7. Randomized Experiments**

Matthew Blackwell

Harvard University

## Roadmap

- 1. Randomized experiments
- 2. Calculating effects

• What does " $T_i$  causes  $Y_i$ " mean?  $\rightsquigarrow$  counterfactuals, "what if"

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| i            | $T_i$ | $Y_i$ | $Y_i(1)$ | $Y_i(0)$ |
|--------------|-------|-------|----------|----------|
| Respondent 1 | 0     | 0     | ???      | 0        |
| Respondent 2 | 1     | 1     | 1        | ???      |

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- To infer causal effect, we need to infer the missing counterfactuals!



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- NJ increased the minimum wage. Causal effect on unemployment?
  - → find a state similar to NJ that didn't increase minimum wage.



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- Those who take treatment may be different that those who take control.
- · How can we correct for that?

## 1/ Randomized experiments



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  - Similar on both observable and unobservable characteristics.

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### A little more notation

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$$\sum_{i=1}^{n} Y_i = Y_1 + Y_2 + Y_3 + \dots + Y_n$$

•  $\Sigma_{i=1}^n$  means sum each value from  $Y_1$  to  $Y_n$ 

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Suppose we surveyed 6 people and 3 supported nondiscrim. laws:

$$\overline{Y} = \frac{1}{6} (1 + 1 + 1 + 0 + 0 + 0) = 0.5$$

• We want to estimate the average causal effects over all units:

Sample Average Treatment Effect (SATE) 
$$=\frac{1}{n}\sum_{i=1}^n\{Y_i(1)-Y_i(0)\}$$
  
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• Implies difference-in-means should be close to SATE:

$$\overline{Y}_{\text{treated}} - \overline{Y}_{\text{control}} \approx \frac{1}{n} \sum_{i=1}^{n} Y_i(1) - \frac{1}{n} \sum_{i=1}^{n} Y_i(0) = \frac{1}{n} \sum_{i=1}^{n} \{Y_i(1) - Y_i(0)\} = \text{SATE}$$

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#### · Hawthorne effects:

Respondents act differently just knowing that they are under study.

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  - Under randomization,  $\overline{X}_{\text{treated}} \overline{X}_{\text{control}} pprox 0$

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  - $\overline{Y}_{\text{treated, B}} \overline{Y}_{\text{control}}$
  - $\overline{Y}_{\text{treated, A}} \overline{Y}_{\text{treated, B}}$
- If treatment arms are randomly assigned, these differences will be good estimators for each causal contrast.

# 2/ Calculating effects

## **Transphobia study data**

## reinstall gov50data if necessary
library(gov50data)

| Variable Name   | Description   |
|-----------------|---|
| age             | Age of the R in years                                   |
| female          | 1=R marked "Female" on voter reg., 0 otherwise          |
| voted_gen_14    | 1 if R voted in the 2014 general election               |
| vote_gen_12     | 1 if R voted in the 2012 general election               |
| treat_ind       | 1 if R assigned to trans rights script, 0 for recycling |
| racename        | name of racial identity indicated on voter file         |
| democrat        | 1 if R is a registered Democrat                         |
| nondiscrim_pre  | 1 if R supports nondiscrim. law at baseline             |
| nondiscrim_post | 1 if R supports nondiscrim. law after 3 months          |

### Peak at the data

#### trans

```
## # A tibble: 565 x 9
##
       age female voted_gen_14 voted_gen_12 treat_ind racename
##
     <dbl> <dbl>
                                      <dbl>
                         <dbl>
                                                 <dbl> <chr>
##
        29
                                                     0 African~
   1
   2 59
                                                     1 African~
##
##
   3 35
                                                     1 African~
                                                     1 African~
##
   4 63
                                                     1 African~
        65
##
##
   6
        51
                                                     O Caucasi~
                                                     0 African~
##
        26
##
        62
                                                     1 African~
   8
##
        37
                                                     O Caucasi~
##
  10
      51
                                                     0 Caucasi~
  # i 555 more rows
  # i 3 more variables: democrat <dbl>, nondiscrim pre <dbl>,
      nondiscrim post <dbl>
## #
```

### Calculate the average outcomes in each group

```
treat_mean <- trans |>
  filter(treat_ind == 1) |>
  summarize(nondiscrim_mean = mean(nondiscrim_post))
treat_mean
```

```
## # A tibble: 1 x 1
## nondiscrim_mean
## <dbl>
## 1 0.687
```

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treat mean
## # A tibble: 1 x 1
##
    nondiscrim mean
               <dh1>
##
               0.687
## 1
control mean <- trans |>
  filter(treat ind == 0) |>
  summarize(nondiscrim mean = mean(nondiscrim post))
control mean
```

## # A tibble: 1 x 1

nondiscrim mean

<dbl>

##

##

## 1

```
17 / 24
```

### Calculating the difference in means

#### treat\_mean - control\_mean

```
## nondiscrim_mean
## 1 0.039
```

We'll see more ways to do this throughout the semester.

### **Checking balance on numeric covariates**

We can use group\_by to see how the mean of covariates varies by group:

```
trans |>
  group_by(treat_ind) |>
  summarize(age_mean = mean(age))
```

```
## # A tibble: 2 x 2
## treat_ind age_mean
## <dbl> <dbl>
## 1 0 48.2
## 2 1 48.3
```

### **Checking balance on categorical covariates**

Or we can group by treatment and a categorical control:

```
trans |>
  group_by(treat_ind, racename) |>
  summarize(n = n())
```

```
# A tibble: 9 x 3
  # Groups: treat ind [2]
## treat_ind racename
                                 n
## <dbl> <chr>
                            <int>
            O African American
                                58
## 2
            0 Asian
                                2
           0 Caucasian
                                77
           0 Hispanic
## 4
                               150
           1 African American
                               68
## 5
           1 Asian
                                4
           1 Caucasian
## 7
                               75
           1 Hispanic
                               130
## 8
           1 Native American
##
  9
```

Hard to read!

### pivot\_wider

pivot\_wider() takes data from a single column and moves it into multiple columns based on a grouping variable:

```
trans |>
  group_by(treat_ind, racename) |>
  summarize(n = n()) |>
  pivot_wider(
   names_from = treat_ind,
   values_from = n
)
```

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)
```

names\_from tells us what variable will map onto the columns
values\_from tell us what values should be mapped into those columns

58 68

77 75

150 130

NA

2 4

## 1 African American

## 2 Asian

## 3 Caucasian

## 4 Hispanic

## 5 Native American

### Calculating diff-in-means by group

```
trans |>
 mutate(
    treat ind = if else(treat ind == 1, "Treated", "Control"),
    party = if else(democrat == 1, "Democrat", "Non-Democrat")
  group by(treat ind, party) |>
  summarize(nondiscrim mean = mean(nondiscrim post)) |>
 pivot wider(
   names from = treat ind,
    values from = nondiscrim mean
 mutate(
   <u>diff in means = Treated - Control</u>
```