Gov 50: 6. Causality

Matthew Blackwell

Harvard University

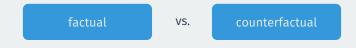
Roadmap

- 1. What is causality?
- 2. Randomized experiments
- 3. Calculating effects

1/ What is causality?



Two roads diverged in a yellow wood, And sorry I could not travel both And be one traveler, long I stood And looked down one as far as I could To where it bent in the undergrowth;



• Does increasing the minimum wage increase the unemployment rate?



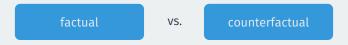
- Does increasing the minimum wage increase the unemployment rate?
 - Unemployment rate went up after the minimum wage increased



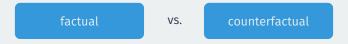
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- · Does having girls affect a judge's rulings in court?



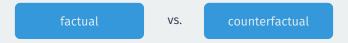
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- Fundamental problem of causal inference:
 - Can never observe counterfactuals, must be inferred.



POLITICAL SCIENCE

Durably reducing transphobia: A field experiment on door-to-door canvassing

David Broockman¹* and Joshua Kalla²

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Trans rights conversations focused on "perspective taking"



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 - Trans rights conversations focused on "perspective taking"

· Outcome of interest: support for trans rights policies.

A tale of two respondents

	Conversation Script	Support for Nondiscrimination Law
Respondent 1	Recycling	No
Respondent 2	Trans rights	Yes

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Did the second respondent support the law **because** of the perspective-taking conversation?

Translating into math

Useful to have **compact** notation for referring to **treatment variable**:

$$T_i = \begin{cases} 1 & \text{if respondent } i \text{ had trans rights conversation} \\ 0 & \text{if respondent } i \text{ had recycling conversation} \end{cases}$$

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Similar notation for the outcome variable:

$$Y_i = \begin{cases} 1 & \text{if respondent } i \text{ supports trans nondiscrimination laws} \\ 0 & \text{if respondent } i \text{ doesn't support nondiscrimination laws} \end{cases}$$

i is a placeholder to refer to a generic unit/respondent: Y_{42} is the outcome for the 42nd unit.

A tale of two respondents (redux)

	Conversation Script	Support for Nondiscrimination Law
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becomes...

T_{i}	Y_{i}
0	0
1	1

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i	T_{i}	Y_{i}	$Y_i(1)$	$Y_i(0)$
Respondent 1	0	0	???	0
Respondent 2	1	1	1	???

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 - · We only observe one of the two potential outcomes.
 - Observe $Y_i = Y_i(1)$ if $T_i = 1$ or $Y_i = Y_i(0)$ if $T_i = 0$
- To infer causal effect, we need to infer the missing counterfactuals!

How can we figure out counterfactuals?



• Find a similar unit! \rightsquigarrow matching



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- Does respondent support law because of the trans rights script?
 - \rightsquigarrow find a identical respondent who got the recycling script.
- NJ increased the minimum wage. Causal effect on unemployment?
 - \rightsquigarrow find a state similar to NJ that didn't increase minimum wage.



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- Selection Bias: $Y_i(1) \neq Y_j(1)$
- Those who take treatment may be different that those who take control.
- · How can we correct for that?

2/ Randomized experiments



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 - Similar on both observable and unobservable characteristics.

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• $\Sigma_{i=1}^n$ means sum each value from Y_1 to Y_n

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• Suppose we surveyed 6 people and 3 supported nondiscrim. laws:

$$\overline{Y} = \frac{1}{6} (1 + 1 + 1 + 0 + 0 + 0) = 0.5$$

• We want to estimate the average causal effects over all units:

Sample Average Treatment Effect (SATE)
$$=\frac{1}{n}\sum_{i=1}^n\{Y_i(1)-Y_i(0)\}$$

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Difference in means =
$$\overline{Y}_{treated} - \overline{Y}_{control}$$

• $\overline{Y}_{treated}$: sample average outcome for treated group

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- + $\overline{Y}_{\text{treated}}$: sample average outcome for treated group
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- When will the difference-in-means is a good estimate of the SATE?

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· Average in the control group will be similar to average if all untreated:

$$\overline{Y}_{\text{control}} \approx \frac{1}{n} \sum_{i=1}^{n} Y_i(0)$$

• Implies difference-in-means should be close to SATE:

$$\overline{Y}_{\text{treated}} - \overline{Y}_{\text{control}} \approx \frac{1}{n} \sum_{i=1}^{n} Y_i(1) - \frac{1}{n} \sum_{i=1}^{n} Y_i(0) = \frac{1}{n} \sum_{i=1}^{n} \{Y_i(1) - Y_i(0)\} = \text{SATE}$$

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· Hawthorne effects:

Respondents act differently just knowing that they are under study.

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 - Under randomization, $\overline{X}_{\text{treated}} \overline{X}_{\text{control}} pprox 0$

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- If treatment arms are randomly assigned, these differences will be good estimators for each causal contrast.

3/ Calculating effects

Transphobia study data

reinstall gov50data if necessary library(gov50data)

Variable Name	Description
age	Age of the R in years
female	1=R marked "Female" on voter reg., 0 otherwise
voted_gen_14	1 if R voted in the 2014 general election
vote_gen_12	1 if R voted in the 2012 general election
treat_ind	1 if R assigned to trans rights script, 0 for recycling
racename	name of racial identity indicated on voter file
democrat	1 if R is a registered Democrat
nondiscrim_pre	1 if R supports nondiscrim. law at baseline
nondiscrim_post	1 if R supports nondiscrim. law after 3 months

Peak at the data

trans

```
# A tibble: 565 x 9
##
       age female voted_gen_14 voted~1 treat~2 racen~3 democ~4
     <dbl> <dbl>
                                <dbl>
##
                        <dbl>
                                        <dbl> <chr>
                                                        <dbl>
##
        29
                0
                                    1
                                            0 Africa~
   1
   2 59
                                            1 Africa~
##
                                    0
   3 35
                             1
                                            1 Africa~
##
## 4 63
                                            1 Africa~
##
        65
                                            1 Africa~
##
   6 51
                                            0 Caucas~
        26
                                            0 Africa~
##
        62
                                            1 Africa~
##
   8
##
     37
                                            0 Caucas~
     51
##
  10
                                            0 Caucas~
    ... with 555 more rows, 2 more variables:
##
      nondiscrim pre <dbl>, nondiscrim post <dbl>, and
      abbreviated variable names 1: voted gen 12,
## #
##
      2: treat ind, 3: racename, 4: democrat
```

Calculate the average outcomes in each group

```
treat_mean <- trans |>
  filter(treat_ind == 1) |>
  summarize(nondiscrim_mean = mean(nondiscrim_post))
treat_mean
```

```
## # A tibble: 1 x 1
## nondiscrim_mean
## <dbl>
## 1 0.687
```

Calculate the average outcomes in each group

```
treat mean <- trans |>
  filter(treat ind == 1) |>
  summarize(nondiscrim_mean = mean(nondiscrim_post))
treat mean
## # A tibble: 1 x 1
##
    nondiscrim mean
               <dh1>
##
               0.687
## 1
control mean <- trans |>
  filter(treat ind == 0) |>
  summarize(nondiscrim mean = mean(nondiscrim post))
control mean
```

```
## # A tibble: 1 x 1
## nondiscrim_mean
## <dbl>
```

Calculating the difference in means

treat_mean - control_mean

```
## nondiscrim_mean
## 1 0.039
```

We'll see more ways to do this throughout the semester.

Checking balance on numeric covariates

We can use group_by to see how the mean of covariates varies by group:

```
trans |>
  group_by(treat_ind) |>
  summarize(age_mean = mean(age))
```

```
## # A tibble: 2 x 2
## treat_ind age_mean
## <dbl> <dbl>
## 1 0 48.2
## 2 1 48.3
```

Checking balance on categorical covariates

Or we can group by treatment and a categorical control:

```
trans |>
  group_by(treat_ind, racename) |>
  summarize(n = n())
```

```
# A tibble: 9 x 3
  # Groups: treat ind [2]
## treat_ind racename
                                 n
## <dbl> <chr>
                            <int>
            O African American
                                58
## 2
            0 Asian
                                2
           0 Caucasian
                                77
           0 Hispanic
## 4
                               150
           1 African American
                               68
## 5
           1 Asian
                                4
           1 Caucasian
## 7
                               75
           1 Hispanic
## 8
                               130
           1 Native American
##
  9
```

Hard to read!

pivot_wider

pivot_wider() takes data from a single column and moves it into multiple columns based on a grouping variable:

```
trans |>
  group_by(treat_ind, racename) |>
  summarize(n = n()) |>
  pivot_wider(
   names_from = treat_ind,
   values_from = n
)
```

pivot_wider

pivot_wider() takes data from a single column and moves it into multiple columns based on a grouping variable:

```
trans |>
  group_by(treat_ind, racename) |>
  summarize(n = n()) |>
  pivot_wider(
   names_from = treat_ind,
   values_from = n
)
```

names_from tells us what variable will map onto the columns
values_from tell us what values should be mapped into those columns

58 68

77 75

150 130

NA

2 4

1 African American

2 Asian

3 Caucasian

4 Hispanic

5 Native American

Calculating diff-in-means by group

```
trans |>
 mutate(
    treat ind = if else(treat ind == 1, "Treated", "Control"),
    party = if else(democrat == 1, "Democrat", "Non-Democrat")
  group by(treat ind, party) |>
  summarize(nondiscrim mean = mean(nondiscrim post)) |>
 pivot wider(
   names from = treat ind,
    values from = nondiscrim mean
 mutate(
   diff in means = Treated - Control
```