# **Gov 50: 8. Summarizing Data**

Matthew Blackwell

Harvard University

## Roadmap

- 1. Descriptive Statistics
- 2. Missing data
- 3. Proportion tables

## 1/ Descriptive Statistics

## **Lots of data**

```
library(tidyverse)
library(gapminder)
gapminder
```

```
# A tibble: 1,704 x 6
##
##
     country continent
                           year lifeExp
                                            pop gdpPercap
##
     <fct>
                <fct>
                          <int>
                                  <dbl>
                                          <int>
                                                    <fdh>>
##
   1 Afghanistan Asia
                           1952 28.8 8425333
                                                     779.
##
   2 Afghanistan Asia
                           1957
                                   30.3 9240934
                                                     821.
   3 Afghanistan Asia
                           1962
                                   32.0 10267083
                                                     853.
##
##
   4 Afghanistan Asia
                           1967
                                   34.0 11537966
                                                     836.
   5 Afghanistan Asia
##
                           1972
                                   36.1 13079460
                                                     740.
   6 Afghanistan Asia
                                                     786.
##
                           1977
                                   38.4 14880372
   7 Afghanistan Asia
##
                           1982
                                   39.9 12881816
                                                     978.
##
   8 Afghanistan Asia
                           1987
                                   40.8 13867957
                                                     852.
   9 Afghanistan Asia
                           1992
                                   41.7 16317921
                                                     649.
##
  10 Afghanistan Asia
                           1997
                                   41.8 22227415
                                                     635.
  # ... with 1,694 more rows
```

## **Lots and lots of data**

head(gapminder\$gdpPercap, n = 200)

```
##
     [1]
            779
                   821
                          853
                                 836
                                        740
                                               786
                                                      978
                                                            852
                                                                   649
    [10]
                   727
                          975
                                1601
                                       1942
                                              2313
##
            635
                                                    2760
                                                           3313
                                                                  3533
##
    [19]
           3631
                         2497
                                3193
                                       4604
                                              5937
                                                           3014
                                                                  2551
                  3739
                                                    2449
##
    [28]
           3247
                  4183
                         4910
                                5745
                                       5681
                                              5023
                                                    4797
                                                           5288
                                                                  6223
    [37]
                         4269
                                5523
                                             3009
                                                                  2628
##
           3521
                  3828
                                      5473
                                                    2757
                                                           2430
##
    [46]
           2277
                  2773
                         4797
                                5911
                                      6857
                                              7133
                                                    8053
                                                           9443
                                                                 10079
##
    [55]
           8998
                  9140
                         9308 10967
                                      8798
                                            12779
                                                   10040 10950
##
    [64]
          14526
                 16789
                       18334 19477 21889
                                            23425
                                                   26998 30688
##
    [73]
           6137
                  8843
                       10751 12835 16662
                                            19749
                                                   21597
                                                          23688 27042
          29096
                32418 36126
                                9867 11636
                                            12753 14805 18269 19340
##
          19211
                18524
                       19036
                              20292 23404
                                            29796
                                                      684
                                                            662
                                                                   686
##
##
   [100]
            721
                   630
                          660
                                 677
                                        752
                                              838
                                                      973
                                                           1136
                                                                  1391
   [109]
           8343
                  9715
                       10991
                              13149 16672
                                            19118
                                                   20980
                                                          22526
##
                                                                 25576
##
   [118]
          27561 30486
                       33693
                                1063
                                        960
                                              949
                                                    1036
                                                           1086
                                                                  1029
   [127]
           1278
                         1191
                                1233
                                      1373
                                                    2677
                                                           2128
                                                                  2181
##
                  1226
                                              1441
   [136]
                         3548
                                                                  3822
##
           2587
                  2980
                                3157
                                      2754
                                             2962
                                                    3326
                                                           3413
   [145]
            974
                  1354
                         1710
                                2172
                                      2860
                                             3528
                                                    4127
                                                           4314
                                                                  2547
   [154]
                                              984
                                                           2264
##
           4766
                  6019
                         7446
                                 851
                                        918
                                                    1215
                                                                  3215
   [163]
           4551
                  6206
                         7954
                                8647
                                     11004
                                            12570
                                                    2109
                                                           2487
                                                                  3337
   [172]
           3430
                  4986
                         6660
                                7031
                                       7807
                                             6950
                                                    7958
                                                           8131
                                                                  9066
```

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  - **Central tendency**: where is the middle/typical/average value.

- How should we summarize the wages data? Many possibilities!
  - Up to now: focus on averages or means of variables.
- Two salient features of a variable that we want to know:
  - **Central tendency**: where is the middle/typical/average value.
  - Spread around the center: are all values to the center or spread out?

• "Center" of the data: typical/average value.

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- Mean: sum of the values divided by the number of observations

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$$median = \begin{cases} middle \ value & \text{if number of entries is odd} \\ \frac{\text{sum of two middle values}}{2} & \text{if number of entries is even} \end{cases}$$

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In R: mean() and median().

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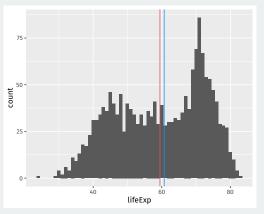
• Example 2: data = {0,1,2,3,100}. Mean? Median?

- · Median more robust to outliers:
  - Example 1: data =  $\{0, 1, 2, 3, 5\}$ . Mean? Median?

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• What does Mark Zuckerberg do to the mean vs median income?

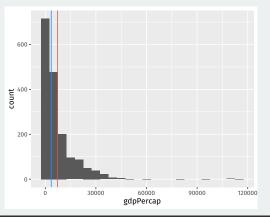
```
ggplot(gapminder, aes(x = lifeExp)) +
  geom_histogram(binwidth = 1) +
  geom_vline(aes(xintercept = mean(lifeExp)), color = "indianred") +
  geom_vline(aes(xintercept = median(lifeExp)), color = "dodgerblue")
```



#### summary(gapminder\$lifeExp)

## Min. 1st Qu. Median Mean 3rd Qu. Max. ## 23.6 48.2 60.7 59.5 70.8 82.6

```
ggplot(gapminder, aes(x = gdpPercap)) +
  geom_histogram(binwidth = 5000) +
  geom_vline(aes(xintercept = mean(gdpPercap)), color = "indianred") +
  geom_vline(aes(xintercept = median(gdpPercap)), color = "dodgerblue")
```

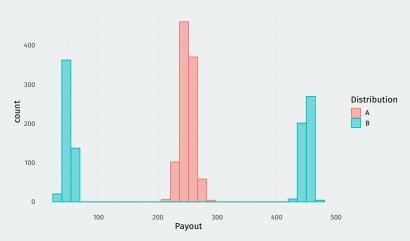


#### summary(gapminder\$gdpPercap)

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 241 1202 3532 7215 9325 113523
```

## Which distribution would you prefer?

Lottery where we randomly draw one value from A or B:



## Which distribution would you prefer?

Lottery where we randomly draw one value from A or B:



They have the same mean, so why do we care about the difference? **Spread!!** 

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- R function: range(), summary(), IQR()

## **Standard deviation**

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standard deviation = 
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$$\sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (x_i - \bar{x})^2}$$

- · Steps:
  - 1. Subtract each data point by the mean.

standard deviation 
$$=\sqrt{\frac{1}{n-1}\sum_{i=1}^{n}(x_i-\bar{x})^2}$$

- Steps:
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  - 4. Divide by n-1 (or n, doesn't matter much)
  - 5. Take the square root.
- Variance = standard deviation<sup>2</sup>
- Why not just take the average deviations from mean without squaring?

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  - Sensitive questions → social desirability bias
  - · Some countries lack official statistics like unemployment.
  - · Leads to missing data.
- · Missing data in R: a special value NA
- Have already seen how to use na.rm = TRUE

### **CCES** data

# library(gov50data) cces\_2020

```
## # A tibble: 51,551 x 6
     gender race educ
                                   pid3 turno~1 pres ~2
##
##
  <fct> <fct> <fct> <fct>
                                   <fct>
                                            <dhl> <fct>
##
   1 Male White 2-year
                                   Republ~ 1 Donald~
##
   2 Female White Post-grad
                                   Democr~
                                               NA <NA>
##
   3 Female White 4-year
                                   Indepe~ 1 Joe Bi~
   4 Female White 4-year
                                   Democr~ 1 Joe Bi~
##
   5 Male White 4-year
##
                                   Indepe~ 1 Other
   6 Male White Some college
                                   Republ~ 1 Donald~
##
   7 Male Black Some college
                                   Not su~
                                               NA <NA>
##
   8 Female White Some college
##
                                   Indepe~ 1 Donald~
   9 Female White High school graduate Republ~ 1 Donald~
##
## 10 Female White 4-year
                                   Democr~ 1 Joe Bi~
  # ... with 51,541 more rows, and abbreviated variable names
      1: turnout self, 2: pres vote
## #
```

## drop\_na() to remove rows with missing values

```
cces_2020 |>
drop_na()
```

```
## # A tibble: 45,651 x 6
##
     gender race educ
                                   pid3 turno~1 pres_~2
##
  <fct> <fct> <fct>
                                   <fct>
                                            <dhl> <fct>
##
   1 Male White 2-year
                                   Republ~
                                                1 Donald~
##
   2 Female White 4-year
                                   Indepe~ 1 Joe Bi~
                                   Democr~ 1 Joe Bi~
##
   3 Female White 4-year
##
   4 Male White 4-year
                                   Indepe~ 1 Other
##
   5 Male White Some college
                                   Republ~ 1 Donald~
##
   6 Female White Some college
                                   Indepe~ 1 Donald~
##
   7 Female White High school graduate Republ~ 1 Donald~
   8 Female White 4-vear
##
                                   Democr~ 1 Joe Bi~
   9 Female White 4-year
                                   Democr~ 1 Joe Bi~
##
  10 Female White 4-year
                                   Democr~ 1 Joe Bi~
  # ... with 45,641 more rows, and abbreviated variable names
     1: turnout self, 2: pres vote
```

### **Drop rows based on certain variables**

```
cces_2020 |>
  dim desc()
## [1] "[51,551 x 6]"
cces_2020 |>
  drop na() |>
  dim_desc()
## [1] "[45,651 x 6]"
cces 2020 |>
  drop_na(turnout_self) |>
  dim desc()
## [1] "[48,462 x 6]"
```

### Available-case vs complete-case analysis

**Available-case analysis**: use the data you have for that variable:

```
cces_2020 |>
  summarize(mean(turnout_self, na.rm = TRUE)) |>
  pull()
```

```
## [1] 0.942
```

### Available-case vs complete-case analysis

Available-case analysis: use the data you have for that variable:

```
cces_2020 |>
  summarize(mean(turnout_self, na.rm = TRUE)) |>
  pull()
```

## [1] 0.942

#### Complete-case analysis: only use units that have data on all variables

```
cces_2020 |>
  drop_na() |>
  summarize(mean(turnout_self)) |>
  pull()
```

## [1] 0.999

### Available-case vs complete-case analysis

Available-case analysis: use the data you have for that variable:

```
cces_2020 |>
  summarize(mean(turnout_self, na.rm = TRUE)) |>
  pull()
## [1] 0.942
```

Complete-case analysis: only use units that have data on all variables

```
cces_2020 |>
  drop_na() |>
  summarize(mean(turnout_self)) |>
  pull()
```

```
## [1] 0.999
(also called listwise deletion)
```

# is.na() to detect missingness

Trying to detect missingness with == doesn't work:

$$c(5, 6, NA, 0) == NA$$

## [1] NA NA NA NA

# is.na() to detect missingness

Trying to detect missingness with == doesn't work:

$$c(5, 6, NA, 0) == NA$$

## [1] NA NA NA NA

Use is.na() instead:

## [1] FALSE FALSE TRUE FALSE

## is.na() to detect missingness

Trying to detect missingness with == doesn't work:

```
c(5, 6, NA, 0) == NA
```

## [1] NA NA NA NA

Use is.na() instead:

## [1] FALSE FALSE TRUE FALSE

Can use sum() or mean() on this to get number/proportion missing:

## [1] 1

### **Nonresponse bias**

Nonresponse can create bias if lower turnout ⇒ more non-response:

```
cces_2020 |>
  group_by(pid3) |>
  summarize(
  mean_turnout = mean(turnout_self, na.rm = TRUE),
  missing_turnout = mean(is.na(turnout_self))
)
```

```
## # A tibble: 5 x 3
##
   pid3
              mean turnout missing turnout
##
  <fct>
                    <dbl>
                                <dbl>
## 1 Democrat
                    0.963
                                0.0280
  2 Republican
                0.953
                               0.0403
## 3 Independent
               0.924
                              0.0718
## 4 Other
                  0.957
                               0.0709
                   0.630
                                0.431
## 5 Not sure
```

# 3/ Proportion tables

### **Review of getting counts**

#### First, let's review how to get counts:

```
cces_2020 |>
  group_by(pres_vote) |>
  summarize(n = n())
```

```
## # A tibble: 7 x 2
##
  pres_vote
                                       n
    <fct>
##
                                   <int>
## 1 Joe Biden (Democrat)
                                   26188
  2 Donald J. Trump (Republican) 17702
## 3 Other
                                    1458
## 4 I did not vote in this race
                                    100
## 5 I did not vote
                                     13
## 6 Not sure
                                     190
## 7 <NA>
                                    5900
```

### First attempt to create proportions

```
cces_2020 |>
  group_by(pres_vote) |>
  summarize(prop = n() / sum(n()))
```

### First attempt to create proportions

```
cces_2020 |>
  group_by(pres_vote) |>
  summarize(prop = n() / sum(n()))
```

Inside summarize() all operations are done within groups!

### **Mutate after summarizing**

```
cces_2020 |>
  group_by(pres_vote) |>
  summarize(n = n()) |>
  mutate(prop = n / sum(n))
```

```
## # A tibble: 7 x 3
## pres vote
                                   n prop
                                <int> <dbl>
## <fct>
## 1 Joe Biden (Democrat)
                               26188 0.508
## 2 Donald J. Trump (Republican) 17702 0.343
## 3 Other
                               1458 0.0283
## 4 I did not vote in this race 100 0.00194
## 5 T did not vote
                                13 0.000252
                                 190 0.00369
## 6 Not sure
## 7 <NA>
                                 5900 0.114
```

### **Mutate after summarizing**

```
cces_2020 |>
  group_by(pres_vote) |>
  summarize(n = n()) |>
  mutate(prop = n / sum(n))
```

```
## # A tibble: 7 x 3
## pres vote
                                  n prop
## <fct>
                                <int> <dbl>
## 1 Joe Biden (Democrat)
                               26188 0.508
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                              1458 0.0283
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                                13 0.000252
## 6 Not sure
                                 190 0.00369
## 7 <NA>
                                5900 0.114
```

Grouping is silently dropped after summarize()

### **Multiple grouping variables**

#### What happens with multiple grouping variables

```
## # A tibble: 10 x 4
  # Groups: pid3 [5]
##
##
     pid3 pres_vote
                                             n
                                                prop
##
     <fct> <fct>
                                         <int> <dhl>
##
   1 Democrat Joe Biden (Democrat)
                                        17649 0.968
##
   2 Democrat Donald J. Trump (Republican) 581 0.0319
   3 Republican Joe Biden (Democrat) 856 0.0712
##
##
   4 Republican Donald J. Trump (Republican) 11164 0.929
##
   5 Independent Joe Biden (Democrat)
                                          6601 0.571
   6 Independent Donald J. Trump (Republican) 4951 0.429
##
##
   7 Other
               Joe Biden (Democrat) 735 0.487
##
   8 Other
             Donald J. Trump (Republican) 774 0.513
   9 Not sure Joe Biden (Democrat)
##
                                          347 0.599
  10 Not sure Donald J. Trump (Republican) 232 0.401
##
```

```
## # A tibble: 10 x 4
##
  # Groups: pid3 [5]
     pid3 pres_vote
##
                                                 prop
##
     <fct> <fct>
                                          <int> <dhl>
##
   1 Democrat Joe Biden (Democrat)
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##
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   3 Republican Joe Biden (Democrat)
##
                                    856 0.0712
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##
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                                          6601 0.571
##
   6 Independent Donald J. Trump (Republican) 4951 0.429
##
   7 Other
               Joe Biden (Democrat) 735 0.487
##
##
   8 Other Donald J. Trump (Republican) 774 0.513
   9 Not sure Joe Biden (Democrat)
##
                                           347 0.599
## 10 Not sure Donald J. Trump (Republican) 232 0.401
```

With multiple grouping variables, summarize() drops the last one.

### **Dropping all groups**

If we want the proportion of all rows, need to drop all groups.

```
## # A tibble: 10 x 4
##
    pid3 pres vote
                                           n prop
## <fct> <fct>
                                        <int> <dbl>
##
   1 Democrat Joe Biden (Democrat)
                                       17649 0.402
   2 Democrat Donald J. Trump (Republican) 581 0.0132
##
   3 Republican Joe Biden (Democrat) 856 0.0195
##
##
   4 Republican Donald J. Trump (Republican) 11164 0.254
   5 Independent Joe Biden (Democrat)
##
                                    6601 0.150
##
   6 Independent Donald J. Trump (Republican) 4951 0.113
##
   7 Other
              Joe Biden (Democrat)
                                 735 0.0167
##
   8 Other Donald J. Trump (Republican) 774 0.0176
                                 347 0.00791
##
   9 Not sure Joe Biden (Democrat)
  10 Not sure Donald J. Trump (Republican) 232 0.00529
```