

Data Structure In

Python

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Introduction

In the ever-evolving domain of computer science, data structures and algorithms form the bedrock upon which software applications are built. A profound understanding of these concepts is indispensable for any aspiring software engineer or computer scientist. This book, *Data Structure in Python: From Basics to Expert Proficiency*, is meticulously crafted to impart a comprehensive understanding of data structures and algorithms using the Python programming language.

Data structures are integral components that facilitate the organization, management, and storage of data for efficient access and modification. From the rudimentary arrays and linked lists to the more sophisticated trees and graphs, each data structure is designed to address specific computational problems. An adept knowledge of these structures not only aids in problem-solving but also enhances the performance and scalability of software solutions.

Algorithms, on the other hand, are systematic procedures that provide step-by-step instructions to accomplish a particular task or solve a specific problem. The symbiotic relationship between data structures and algorithms provides a powerful toolkit for tackling complex programming challenges. Understanding the intricacies of algorithmic design and analysis is pivotal in selecting the most appropriate data structure for a given problem, thereby optimizing the computational efficiency.

Python, known for its readability and simplicity, serves as an ideal language for learning and implementing data structures and algorithms. Its extensive standard library and dynamic typing capability further make it a versatile tool for both educational purposes and real-world applications. As such, this book leverages Python to elucidate the fundamental concepts of data structures and algorithms, making it accessible to learners with varying degrees of prior programming experience.



The structure of this book is meticulously designed to introduce concepts in a logical progression. It begins with an introductory overview that lays the foundation, followed by details on Python programming basics. As we delve deeper into the chapters, we explore specific data structures, starting from basic arrays to complex trees and graphs. Each chapter encompasses both theoretical explanations and practical implementations, ensuring a well-rounded understanding.

Moreover, the book emphasizes the importance of algorithm analysis and the Big O notation—a framework for evaluating the efficiency of algorithms. As we navigate through the various sorting and searching algorithms, readers will gain insight into how different approaches affect performance and resource usage. The advanced data structures chapter encapsulates cutting-edge structures that are pivotal in solving modern computational problems.

This book aspires to equip readers with a robust understanding of data structures and algorithms, empowering them to conceive and implement efficient solutions. Whether you are a novice programmer seeking to build a foundational understanding or an experienced developer aiming to refine your skills, this book serves as a comprehensive guide in your pursuit of excellence in the field of data structures and algorithms.

Welcome to the journey of mastering data structures and algorithms with Python. Let us embark on this intellectual endeavor with rigor, precision, and a commitment to excellenc



Chapter 1 Introduction to Data Structures and Algorithms

Data structures and algorithms are fundamental components of computer science, essential for organizing, managing, and manipulating data efficiently. This chapter introduces key concepts and classifications of data structures, defines what an algorithm is, and explains the importance of algorithms in solving computational problems. Additionally, it covers basic terminology, algorithm analysis, Big O notation, and time and space complexity, providing a comprehensive foundation for selecting the appropriate data structure for specific tasks.

1.1 What are Data Structures?

Data structures are a systematic way of organizing and managing data to enable efficient access and modification. They are the foundational constructs upon which software systems are built, facilitating the storage, retrieval, and processing of data. In computer science, data structures provide the means to solve complex computational problems by laying the groundwork for efficient algorithm design and implementation.

At the core, data structures represent a collection of data values, the relationships among them, and the functions or operations that can be applied to the data. These structures dictate the organization, manipulation, and storage of data in a computer's memory or any other storage device, improving both the efficiency and quality of software applications.

There are two primary classifications of data structures: primitive and non-primitive. Primitive data structures are the most basic types of data, inherent to the language being used, such as integers, floats, characters, and booleans. Non-primitive data structures, on the other hand, build upon these basic types to construct more sophisticated forms, which can be further divided into linear and non-linear structures. Understanding these categories is crucial for selecting the appropriate data structure based on the requirements and constraints of a given problem.

Linear data structures include arrays, linked lists, stacks, and queues. These structures arrange data in a sequential manner, meaning each element has a unique predecessor and successor. Key characteristics of linear data structures include:

•Arrays: A collection of elements identified by index or key, stored in contiguous memory locations. Arrays allow for constant-time access to elements but may require shifting during insertion or deletion, leading to inefficient operations.



```
# Example of an array in Python
array = [1, 2, 3, 4, 5]
print(array[2]) # Outputs: 3

Output:
3
```

•Linked Lists: Consists of nodes where each node contains a data element and a reference (or link) to the next node in the sequence. Linked lists support efficient insertion and deletion operations but require sequential access to retrieve an element by index.

```
# Example of a simple linked list in Python
class Node:
   def___init_(self, data):
      self.data = data
      self.next = None
class LinkedList:
   def___init_(self):
      self.head =
      None
   def append(self, data):
      new node = Node(data)
      if self.head is None:
         self.head =
      new node else:
         current =
         self.head while
         current.next:
            current = current.next
         current.next = new node
linked_list = LinkedList()
linked list.append(1)
linked list.append(2)
linked list.append(3)
```

•Stacks: A linear data structure that follows the Last-In-First-Out (LIFO) principle, wherein the last element inserted is the first one to be removed. Operations include push (insertion), pop (removal), and peek (accessing the top element without removal).

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```
# Example of a stack in Python using a list
stack = []
stack.append(1) #
Push stack.append(2)
# Push
stack.append(3) #
Push
print(stack.pop()) # Pop, Outputs: 3
print(stack) # [1, 2]
Output:
3
[1, 2]
```

•Queues: A linear data structure adhering to the First-In-First-Out (FIFO) protocol, where the first element added is the first one to be removed. Common operations include enqueue (insertion) and dequeue (removal).

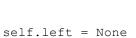
```
# Example of a queue in Python using a list
from collections import
deque queue = deque()
queue.append(1) # Enqueue
queue.append(2) # Enqueue
queue.append(3) # Enqueue
print(queue.popleft()) # Dequeue, Outputs: 1
print(queue) # deque([2, 3])
Output:
1
deque([2, 3])
```

Non-linear data structures include trees and graphs. These structures represent data elements that are hierarchically or inter-connected, allowing for more complex relationships between data elements:

•Trees: A hierarchical data structure with a root element and sub-elements or children, forming an acyclic graph. Trees are utilized in scenarios such as expression parsing, hierarchical data representation, and in binary search trees for efficient searching and sorting.

```
# Example of a simple binary tree in Python
class TreeNode:
    def___init_(self, key):
```

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```
self.right = None
self.val = key

root = TreeNode(1)
root.left = TreeNode(2)
root.right = TreeNode(3)
root.left.left =
TreeNode(4)
root.left.right = TreeNode(5)
```

Graphs: A generalization of trees where nodes can be interconnected with no constraints on connections, allowing cycles. Graphs are pivotal in network analysis, finding shortest paths, and solving problems such as the traveling salesman problem.

```
# Example of a graph using an adjacency list in Python
   def___init_(self):
      self.graph = defaultdict(list)
   def add edge(self, u, v):
      self.graph[u].append(v)
graph = Graph()
graph.add edge(0, 1)
graph.add edge(0, 2)
graph.add edge(1, 2)
graph.add edge(2, 0)
graph.add edge(2, 3)
graph.add edge(3, 3)
print(graph.graph)
           Output:
           defaultdict(<class 'list'>, {0: [1, 2], 1:
[2], 2: [0, 3], 3: [3]})
```

Understanding the characteristics of each data structure and their respective advantages and limitations is essential for designing efficient algorithms. Properly chosen data structures can significantly improve the performance and scalability of software applications, making data management more effective.

1.2 Why Study Data Structures?

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Data structures are an indispensable aspect of computer science that facilitate efficient data management and manipulation. A deep understanding of data structures enables computer scientists and software engineers to develop programs that can process data swiftly, conserve memory, and improve overall performance. This section explores the critical reasons for studying data structures in detail.

Conceptually, data structures provide the means to organize data in ways that enable efficient operations. For example, consider the task of searching for a particular element. Depending on the organization of the data, the search operation may take varying amounts of time. A linear search through an unsorted list has a time complexity of O(n), while a binary search on a sorted array is more efficient with $O(\log n)$. The choice of data structure thus directly impacts the performance of such operations.

One primary reason for studying data structures is to optimize algorithm efficiency. The choice of data structure can significantly affect the efficiency of an algorithm. For instance, when dealing with a dynamic set of elements that require frequent insertions and deletions, a linked list may be more suitable than an array. Arrays require shifting elements when an insertion or deletion takes place, resulting in a time complexity of O(n). In contrast, linked lists enable these operations in O(1) time, assuming that the position of insertion or deletion is known.

```
class ListNode:
    def___init_(self, value=0, next=None):
        self.value = value
        self.next = next
```

In addition to optimizing algorithms, data structures play a crucial role in memory utilization. Different data structures have diverse memory requirements. For example, while arrays require contiguous memory allocation, linked lists can be spread across different memory locations. This characteristic allows better memory utilization, especially in systems with limited dynamic memory.

Understanding the importance of choosing the right data structure is also crucial for handling large datasets. As data grows, the efficiency and scalability of the chosen data structure become paramount. For instance, tree structures such as B-trees and AVL trees facilitate efficient search, insertion, and deletion operations, making them suitable for databases and file systems.

```
class TreeNode:
    def___init__(self, key):
        self.left = None
        self.right = None
        self.val = key
```



Real-world applications are another compelling reason to study data structures. For instance, social networks like Facebook and LinkedIn leverage graph data structures to model connections between users. Each user is represented as a node, and connections between users are represented as edges. This allows efficient traversal and querying of user networks, enabling real-time recommendations and search functionalities.

```
class Graph:
   def___init_(self):
      self.graph = defaultdict(list)
   def add_edge(self, u, v):
      self.graph[u].append(v)
   def bfs(self,
      start): visited =
      set()
      queue = deque([start])
      while queue:
         vertex = queue.popleft()
         if vertex not in
         visited:
            visited.add(vertex)
            queue.extend(x for x in self.graph[vertex] if x not in
      visited) return visited
```

Data structures also underpin the development of modern computing frameworks. Many advanced algorithms rely on efficient data structures for their implementation. Sorting algorithms like quicksort and mergesort, dynamic programming solutions, and even machine learning models make extensive use of well-chosen data structures. For example, hash tables provide average-case constant-time complexity for search, insert, and delete operations, making them ideal for caching and fast retrieval systems.

```
class HashTable:
    def ___init__(self):
        self.table = [[] for _ in range(10)]

    def _hash_function(self, key):
        return hash(key) %
        len(self.table)

    def insert(self, key, value):
        hash_key = self._hash_function(key)
        key_exists = False
        for i, kv in
```

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```
enumerate(self.table[hash_key]): k, v =
kv
if key == k:
```



A comprehensive understanding of data structures is essential for mastering advanced topics in computer science, such as algorithm design, database management, and network protocols. Enabling the efficient organization and manipulation of data, data structures help achieve optimum performance and resource utilization.

Realizing the significance of data structures equips programmers with the skills to analyze and choose the most suitable data structure for a given problem, leading to robust and efficient software solutions.

1.3 Types of Data Structures

Data structures can be broadly categorized into two primary types: primitive data structures and non-primitive data structures. Understanding these types is fundamental as each serves distinct purposes and provides specific functionalities that are essential for effective data manipulation.

Primitive data structures are the simplest forms of data structures and are directly operated upon by machine-level instructions. They include the basic types such as integers, floats, characters, and pointers. These data structures are inherently built into programming languages and are used to construct more complex data structures.

Non-primitive data structures, on the other hand, are more complex and can be divided into two main classes: linear data structures and nonlinear data structures.

Linear Data Structures: Linear data structures arrange data in a linear sequence, where each element is connected to its previous and next element in a sequential manner. This category includes arrays, linked lists, stacks, and queues.

•Arrays: Arrays are a collection of elements, identified by index or key, where each element is of the same data type. Arrays are static in size, meaning their size is

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fixed upon creation. They offer the advantage of O(1) access time for indexed elements, but they require contiguous memory allocation.

```
# Example of an array in Python
arr = [1, 2, 3, 4, 5]
print(arr[2]) # Output: 3
```

•Linked Lists: Linked lists are collections of nodes where each node contains data and a reference (or link) to the next node in the sequence. Linked lists are dynamic in size and can efficiently support operations such as insertions and deletions. However, they do not support constant-time access to elements.

```
# Example of a simple linked list in Python
class Node:
  def___init_(self, data):
      self.data = data
      self.next = None
class LinkedList:
  def___init_(self):
      self.head =
     None
  def append(self, data):
      new node = Node (data)
      if not self.head:
         self.head =
         new node return
      last =
      self.head while
      last.next:
         last = last.next
      last.next = new node
# Create a linked list and append elements
ll = LinkedList()
ll.append(1)
11.append(2)
11.append(3)
```

•Stacks: Stacks are collections of elements that follow the Last In First Out (LIFO) principle. The basic operations for a stack are push (to add an element) and pop (to remove the most recently added element).



```
# Example of a stack in Python
stack = []

# Push elements to the stack
stack.append(1)
stack.append(2)
stack.append(3)

# Pop and display elements from the stack
print(stack.pop()) # Output: 3
print(stack.pop()) # Output: 2
3
2.
```

•Queues: Queues are collections of elements that follow the First In First Out (FIFO) principle. Key operations for queues are enqueue (to add an element to the end) and dequeue (to remove the first element).

```
# Example of a queue in Python
from collections import

deque queue = deque()

# Enqueue elements to the queue
queue.append(1)
queue.append(2)
queue.append(3)

# Dequeue and display elements from the queue
print(queue.popleft()) # Output: 1
print(queue.popleft()) # Output: 2

1
2
```

Nonlinear Data Structures: Nonlinear data structures store data in a hierarchical manner and are used to represent complex relationships and structures. This category includes trees and graphs.

•Trees: Trees are hierarchical structures with a root node, where every node has zero or more child nodes and a single parent (except for the root node, which has no parent). Trees are utilized in scenarios like file system organization, parsing expressions, and hierarchical data representation. A special kind of tree is the binary tree, where each node has at most two children.



```
# Example of a simple binary tree in Python
class TreeNode:
    def___init_(self, key):
        self.left = None
        self.right = None
        self.val = key

# Creating a tree
root = TreeNode(1)
root.left = TreeNode(2)
root.right = TreeNode(3)
root.left.left =
TreeNode(4)
root.left.right = TreeNode(5)
```

•Graphs: Graphs are collections of nodes (vertices) connected by edges. Graphs can represent various real-world entities like social networks, city maps, and network topologies. Graphs can be either directed (with directional edges) or undirected (edges with no direction), and they can be dense (many edges) or sparse (few edges).

```
# Example of a simple graph using adjacency list in Python
class Graph:
  def___init_(self):
      self.graph = {}
  def add edge(self, u, v):
      if u not in
      self.graph:
         self.graph[u] = []
      self.graph[u].append(v
      )
# Creating a graph
g = Graph()
g.add edge(0 1)
g.add_edge(0 2)
g.add_edge(1 2)
g.add_edge(2 0)
g.add_edge(2 3)
g.add_edge(3 3)
,
```

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Understanding these primary categories and their inherent characteristics enables the selection of appropriate data structures depending on the specific computational problem and constraints faced. This foundational knowledge establishes the base for more advanced topics in data structures and algorithm optimization.



1.4 Basic Terminology

In data structures and algorithms, a firm understanding of the fundamental terminology is indispensable for comprehending more advanced concepts. This section elucidates a collection of critical terms and their definitions, each of which plays a pivotal role in the study and application of data structures and algorithms.

A **data element** is the smallest unit of data that can represent a value. Data elements are often used to construct more complex data structures. For example, an integer or character can be regarded as a data element.

A data item refers to a single unit of meaningful information. It can be formed by one or more data elements. For instance, a person's name, which comprises multiple characters, is a data item.

A **data structure** is a systematic way of organizing and storing data to enable efficient access and modification. Examples include arrays, linked lists, stacks, queues, trees, and graphs.

A **record** is a collection of related data items, often organized as a structure. Each field in a record contains one data item that is a type of data element. Consider a record for an employee that may include fields such as name, employee ID, department, and salary.

An **array** is a collection of data elements identified by index or key. Elements are stored such that they can be accessed using indices, which are typically integer values. For instance, in a Python list, elements can be accessed with their positional index:

```
numbers = [10, 20, 30, 40]
print(numbers[2]) # Outputs 30
```

A **linked list** is a linear data structure where each element is a separate object, typically called a node. Each node comprises data and a reference (or link) to the next node in the sequence. This structure allows for efficient insertions and deletions as shown below:

```
class Node:
    def___init__(self, data):
        self.data = data
        self.next = None

class LinkedList:
    def___init__(self):
        self.head =
        None

    def append(self, data):
```

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```
new_node = Node(data)
if not self.head:
    self.head = new_node
    return
    last = self.head
    while last.next:
        last = last.next
    last.next = new_node

# Usage
linked_list = LinkedList()
linked_list.append(1)
linked_list.append(2)
linked_list.append(3)
```

A **stack** is a collection of elements that supports two main operations: push, which adds an element to the collection, and pop, which removes the most recently added element. This follows the Last In, First Out (LIFO) principle:

```
stack = []
stack.append(10) # Push
stack.append(20) # Push
print(stack.pop()) # Pop, Outputs 20
```

A queue is a collection of elements that supports two primary operations: enqueue, which adds an element to the end of the collection, and dequeue, which removes the element from the front. This follows the First In, First Out (FIFO) principle:

```
from collections import
deque queue = deque()
queue.append(1) # Enqueue
queue.append(2) # Enqueue
print(queue.popleft()) # Dequeue, Outputs 1
```

A **tree** is a hierarchical data structure consisting of nodes, with a single node designated as the **root**. Each node can have zero or more **child** nodes. Trees are used in various domains, such as representing hierarchical data, searching algorithms, and more. A **binary tree** is a common type of tree where each node has at most two children, often referred to as the left and right child.

A **graph** is a set of nodes (or vertices) connected by edges. Graphs can be directed or undirected and are used to represent pairwise relationships between objects. They play a crucial role in network analysis, shortest path problems, and many other applications.

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The concepts of **pointers** and **references** are essential in the context of dynamic data structures like linked lists and trees. A pointer is a variable that holds the address of another variable, allowing for the efficient manipulation of complex data structures.

The term **algorithm** refers to a well-defined set of instructions or rules designed to perform a specific task or solve a particular problem. Algorithms are fundamental to computer science and are pivotal in transforming data into meaningful results. They are evaluated based on their correctness and efficiency.

Understanding these basic terminologies will facilitate the comprehension of more intricate data structures and algorithms, forming a solid foundation for further exploration within computer science.

1.5 What is an Algorithm?

An algorithm is a finite sequence of well-defined instructions for solving a problem or performing a task. In computer science, algorithms are the cornerstone for constructing robust and efficient software systems. Each algorithm operates on data, which may be in various structures, such as arrays, linked lists, trees, and graphs, to produce a desired output. The clear structure and logical sequence make algorithms reproducible and reliable.

To delve into the technicalities, let us understand that an algorithm encompasses several intrinsic properties:

- •Finiteness: An algorithm must always terminate after a finite number of steps. Infinite loops or procedures that do not reach a conclusion are not considered algorithms.
- •Definiteness: Each step of an algorithm must be precisely defined. Ambiguities, which might invite different interpretations, are to be rigorously avoided.
- •Input: An algorithm must accept zero or more inputs. Input constitutes the data needed for processing.
- •Output: An algorithm must produce one or more outputs that have a clear relationship to the inputs.
- •Effectiveness: Each operation within the algorithm must be elementary enough to be feasibly performed with basic computational resources.

To illustrate these principles through a concrete example, consider the classic problem of determining the maximum value within a given list of integers. Below is a simple algorithm to accomplish this task, articulated in Python:

```
def find_maximum(lst):
    # Check if the list is empty
```

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```
if not lst:
    return None

# Initialize the maximum value to the first element in the list
max_value = lst[0]

# Iterate through the list
for num in lst:
    if num > max_value:
        max_value = num

return max value
```

Here, the algorithm find_maximum encapsulates all essential properties of an algorithm:

- •Finiteness: The loop will terminate after examining each element of the list, ensuring finiteness.
- •Definiteness: Each step, from the initialization of max_value to the comparison within the loop, is explicitly and unambiguously defined.
- •Input: The function accepts a list of integers.
- Output: The function returns the maximum integer in the list or None if the list is empty.
- •Effectiveness: The operations involve simple comparisons and assignments, making them computationally feasible and effective.

To further examine the concept of algorithms, consider their classification based on various factors:

- •By Implementation: This category includes recursive algorithms and iterative algorithms. Recursive algorithms solve problems by reducing them to smaller instances of the same problem, whereas iterative algorithms solve problems using a loop construct.
- •By Complexity: Algorithms are classified based on their time and space complexity. This includes categories like logarithmic, linear, quadratic, and polynomial time complexity.
- •By Paradigm: Algorithms can also be categorized by their design paradigms, such as divide and conquer, dynamic programming, greedy algorithms, and backtracking.

The effectiveness of an algorithm is evaluated in terms of its performance, predominantly measured by its time complexity and space complexity, as discussed in



later sections. The complexity analysis aids in understanding the scalability and efficiency of the algorithm relative to problem size.

Consider the example of sorting algorithms, such as Quick Sort, Merge Sort, and Bubble Sort. Each algorithm offers different time complexities and efficiencies based on the input data's structure and size. Thus, recognizing the appropriate algorithm for a specific task is crucial for optimal performance.

In essence, algorithms are the building blocks for problem-solving in computer science. They provide structured solutions to computational problems, ensuring that tasks are performed efficiently and correctly. The upcoming sections will further explore various types of data structures and their interaction with algorithms to enhance the efficacy of problem-solving techniques in computer science.

1.6 Importance of Algorithms in Computer Science

Algorithms are the core of computer science, serving as the blueprint for the systematic execution of tasks and problem-solving in computational contexts. Their importance spans multiple dimensions, influencing performance, efficiency, and scalability of systems and applications. Understanding their significance enhances a computer scientist's ability to design optimized and effective solutions.

Efficient algorithms are essential for various reasons:

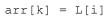
- •**Performance:** The efficiency of an algorithm directly affects the performance of software. For instance, given two algorithms solving the same problem, the one with lower time complexity will execute faster. This is particularly critical for applications requiring real-time processing, such as video streaming, gaming, and high-frequency trading.
- •Resource Optimization: Algorithms that use resources efficiently (e.g., memory, CPU cycles) can run on devices with limited computational power like smartphones and embedded systems. By optimizing resource usage, algorithms help in extending battery life and reducing operation costs.
- •Scalability: Algorithms that scale well can handle increasing amounts of data or more complex operations without a significant drop in performance. This scalability is crucial for applications in big data, where the volume of data can expand exponentially.
- •Solution to Complex Problems: Many computational problems are complex, and some cannot be solved efficiently without advanced algorithms. For example, algorithms in cryptography ensure secure data transmission, while algorithms in machine learning enable pattern recognition and predictive modeling.



•Foundation for Advanced Study: Mastering algorithms is foundational for studying more advanced topics in computer science, including artificial intelligence, data mining, and computational biology. A deep understanding of algorithms allows for the development of more sophisticated methods and techniques in these areas.

To illustrate the importance of algorithms, consider the problem of sorting a list of integers. While a simple sorting algorithm like Bubble Sort can perform the task, its time complexity is $O(n^2)$. In contrast, more advanced algorithms like Merge Sort have a time complexity of $O(n\log n)$. To illustrate this difference through Python code:

```
# Bubble Sort Implementation
def bubble sort(arr):
   n = len(arr)
   for i in range (n-1):
      for j in range(0,
        n-i-1): if arr[j] >
         arr[j+1]:
            arr[j], arr[j+1] = arr[j+1],
   arr[j] return arr
# Merge Sort Implementation
def merge_sort(arr):
   if len(arr) > 1:
      mid =
      len(arr)//2 L =
      arr[:mid]
      R = arr[mid:]
      merge sort(L)
      merge sort(R)
      i = j = k = 0
      while i < len(L) and j <
         len(R): if L[i] < R[j]:
            arr[k] =
            L[i] i += 1
         else:
            arr[k] =
           R[j] j += 1
         k += 1
      while i < len(L):
```







```
i += 1
k += 1

while j <
  len(R):
  arr[k] = R[j]
  j += 1
  k += 1

return arr</pre>
```

Here is an example of sorting a list of integers using both algorithms:

```
# Test list
arr = [64, 34, 25, 12, 22, 11, 90]

# Bubble Sort
print("Bubble Sort Result:", bubble_sort(arr.copy()))

# Merge Sort
print("Merge Sort Result:", merge_sort(arr.copy()))

The output of the above code:
Bubble Sort Result: [11, 12, 22, 25, 34, 64, 90]
Merge Sort Result: [11, 12, 22, 25, 34, 64, 90]
```

The Bubble Sort algorithm, though simpler to understand and implement, is inefficient for larger datasets due to its $O(n^2)$ time complexity. Merge Sort, while more complex, is significantly faster with its $O(n\log n)$ time complexity.

Analyzing algorithm efficiency through Big O notation and other performance metrics allows computer scientists to make informed decisions about which algorithms are best suited for specific tasks. Efficient algorithms can dramatically reduce execution time and resources required, which is especially important in sophisticated and large-scale systems.

In sum, the study of algorithms forms a crucial part of computer science education and practice. Algorithms enable the structured and efficient solution of problems, underpin critical applications, and improve the overall performance of computational systems. A thorough understanding and ability to implement various algorithms is a fundamental skill for any computer scientist.

1.7 Analysis of Algorithms



Algorithm analysis is a critical aspect of computer science, allowing us to evaluate the efficiency of algorithms in terms of running time and space requirements. This rigorous evaluation guides us in selecting algorithms that are not only correct but also efficient, ensuring optimal performance for various computational tasks.

Evaluating an algorithm involves both theoretical analysis and empirical (or experimental) analysis.

Theoretical analysis is conducted by estimating the time and space complexity of an algorithm without exact measurements. This is typically achieved by using Big O notation, which provides an upper bound on the growth rate of an algorithm's resource usage. Empirical analysis, on the other hand, involves implementing the algorithm and running it with various inputs to observe its actual performance in practice.

Time Complexity refers to the amount of time an algorithm takes to complete as a function of the length of the input. It is typically measured in terms of the number of basic operations or computational steps that the algorithm performs. This measure is crucial since a more time-efficient algorithm can handle larger inputs in less time, which is especially important given the growing sizes of modern datasets.

Space Complexity refers to the amount of memory an algorithm uses in terms of the length of the input. This includes all the variables, data structures, and auxiliary space required during the execution of the algorithm. Efficient space utilization is vital in scenarios where memory resources are limited.

To illustrate, consider the following Python function that computes the factorial of a number *n*:

```
def factorial(n):
    if n == 0:
        return
    1 else:
        return n * factorial(n-1)
```

The time complexity of this recursive function can be analyzed as follows: each function call involves a constant number of operations (a comparison and a multiplication) and results in a new function call with n-1, until n reaches 0. This leads to a recursion depth of n, so the time complexity T(n) can be represented as O(n).

Space complexity includes the space taken by function call stacks. The maximum depth of recursive calls here is n, resulting in O(n) space complexity due to the space required for the call stack during execution.

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In contrast to this recursive approach, consider an iterative version of the factorial function:

```
def factorial_iterative(n):
    result = 1
    for i in range(1, n + 1):
        result *= i
    return result
```

The time complexity remains O(n) because the loop executes n times. However, the space complexity is reduced to O(1) since only a constant amount of additional space is required regardless of the size of n.

When comparing algorithms, it's crucial to analyze both their time and space complexities to determine their suitability for specific applications. For instance, while an algorithm might have a modest $O(n^2)$ time complexity for small input sizes, a more efficient $O(n \log n)$ algorithm might be necessary for larger inputs.

Another key aspect of algorithm analysis is identifying the *best-case*, *average-case*, and *worst-case* scenarios for an algorithm's performance:

- **Best-case complexity** describes the minimum time or space that an algorithm requires for some input of size n. - **Average-case complexity** provides an expected time or space usage assuming a random distribution of inputs. - **Worst-case complexity** gives the maximum time or space that an algorithm will require for any input of size n.

Understanding these scenarios is essential for anticipating performance in different operational contexts. For example, consider the popular sorting algorithm Quicksort, which has an average-case time complexity of $O(n \log n)$ but a worst-case time complexity of $O(n^2)$. Knowing both complexities helps developers mitigate the risk of poor performance in adverse conditions by implementing strategic optimizations like randomized pivots or switching to different algorithms for particular data distributions.

Empirical analysis augments theoretical insights by executing the algorithm under realistic conditions, thus capturing the impact of factors like hardware peculiarities, system load, and compiler optimizations. Benchmarking and profiling tools can measure the actual run-time and memory usage, revealing practical performance characteristics.

In practical terms, consider benchmarking our factorial functions with Python's time module:

```
import time
```



```
# Runner for factorial functions
def time_execution(func, args):
    start_time = time.perf_counter()
    result = func(*args)
    end_time = time.perf_counter()
    return end_time - start_time,
    result

# Example usage
time_recursive, result_recursive = time_execution(factorial, (100,))
time_iterative, result_iterative = time_execution(factorial_iterative, (100,))

print(f"Recursive time: {time_recursive}, result: {result_recursive}")
print(f"Iterative time: {time_iterative}, result: {result_iterative}")

Recursive time: 0.000013, result: 9.33262154439441e+157

Iterative time: 0.000005, result: 9.33262154439441e+157
```

These empirical results provide real-world data on the performance differences between recursive and iterative implementations, complementing the theoretical analysis.

Algorithm analysis forms the backbone of efficient algorithm design, equipping computer scientists and developers with the tools to evaluate and select the optimal solutions for their computational problems.

1.8 Big O Notation

When analyzing algorithms, it is crucial to understand their efficiency and scalability. Big O notation provides a mathematical framework to describe the upper bound of an algorithm's running time or space requirements in terms of the input size. This notation helps computer scientists and developers compare the performance of different algorithms, particularly as the input size grows.

Big O notation expresses the worst-case scenario, capturing the maximum amount of time or memory an algorithm could potentially require. This upper bound is critical for understanding how an algorithm performs under the most demanding conditions.

To define Big O notation rigorously, consider a function T(n) that represents the running time of an algorithm for an input of size n. Big O notation characterizes T(n) by describing its growth rate, excluding lower-order terms and constant factors. We say that T(n) is O(f(n)) if there exists a positive constant c and a value n_0 such that for all $n \ge n_0$, f(n)

$$T(n) \leq c$$



In other words, beyond a certain threshold n_0 , the function T(n) is bounded above by $c \cdot f(n)$.

To illustrate, consider some common classes of functions used in Big O notation:

- •Constant Time O(1): The algorithm's running time does not depend on the input size. An example is accessing an element in an array by index.
- •Logarithmic Time O(log n): The running time grows logarithmically as the input size increases. Binary search is a typical example.
- •Linear Time O(n): The running time grows linearly with the input size. A simple iteration over an array demonstrates linear time complexity.
- •Linearithmic Time O(nlog n): The running time grows as the product of *n* and log *n*. Many efficient sorting algorithms, such as Merge Sort and Quick Sort, exhibit this complexity.
- •Quadratic Time O(n²): The running time grows proportionally to the square of the input size. Algorithms with nested loops, such as Bubble Sort and Insertion Sort, often have quadratic complexity.
- •Cubic Time $O(n^3)$: The running time grows as the cube of the input size, typical in algorithms with three nested loops.
- **Exponential Time O(2ⁿ)**: The running time grows exponentially with the input size. Algorithms solving the Traveling Salesman Problem using brute force exhibit exponential complexity.
- •Factorial Time O(n!): The running time grows as the factorial of the input size, characteristic of certain combinatorial algorithms.

To further clarify, consider practical examples. Suppose we have the following Python functions:

```
def constant_time_function(arr):
    return arr[0]

def linear_time_function(arr):
    result = 0
    for value in arr:
        result += value
    return result

def quadratic_time_function(arr):
    result = 0
    n = len(arr)
    for i in range(n):
        for j in
        range(n):
```

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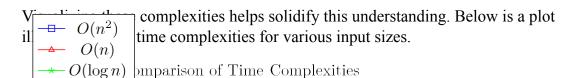
```
result += arr[i] *
arr[j] return result
```

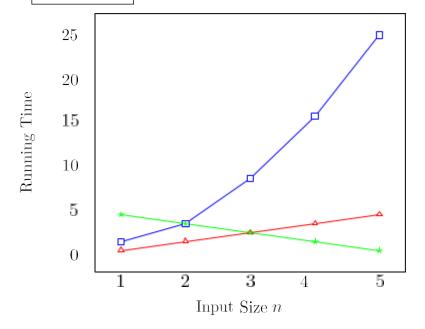
Explanation:

- •constant_time_function has a time complexity of O(1) because accessing an element by index in an array is done in constant time regardless of the array size.
- •linear_time_function has a time complexity of O(n) because it iterates through the entire array once.
- •quadratic_time_function has a time complexity of $O(n^2)$ due to the nested loops each iterating n times.

Understanding Big O notation is essential for algorithm optimization. The notation abstracts away constants and lower-order terms, allowing for a focus on the dominant factor that influences growth rates. This abstraction is particularly useful when dealing with large datasets where these dominant factors become more significant.

Consider sorting an array of size n using different algorithms. Insertion Sort has a time complexity of $O(n^2)$, while Merge Sort and Quick Sort operate in $O(n\log n)$. Though both are efficient for small input sizes, quickly growing data sets show a stark difference in performance.







The graph illustrates the divergent growth rates of quadratic, linear, and logarithmic time complexities. As the input size increases, algorithms with higher complexity exhibit significantly greater demands in terms of time or space, highlighting the importance of choosing the appropriate algorithm based on the problem's context and constraints.

Understanding and applying Big O notation is fundamental to the analysis and design of algorithms, enabling informed decisions to achieve optimal performance and efficiency.

1.9 Time and Space Complexity

When evaluating the efficiency of an algorithm, two primary metrics are often considered: time complexity and space complexity. These metrics help in understanding how resources, such as time and memory, are utilized as the input size grows. This section delves into the definitions, implications, and methods for analyzing both time and space complexity.

Time complexity refers to the computational time required by an algorithm to complete its execution as a function of the size of the input data, denoted by n. It provides an upper bound on the time required, ensuring that the algorithm performs optimally even in the worst-case scenario. Time complexity is commonly expressed using Big O notation, which abstracts away constant factors and lower-order terms to focus on the growth rate of the function. For example, an algorithm with time complexity $O(n^2)$ indicates that the execution time grows quadratically with the input size.

Analyzing time complexity typically involves the following steps:

- •Identify the basic operations: Determine the fundamental operations that significantly contribute to the total running time.
- •Calculate the frequency: Compute the number of times each basic operation is executed as a function of the input size.
- •Establish the growth rate: Translate the frequency count into Big O notation to express the leading term that dominates the growth rate as *n* increases.

Consider the following example of a Python algorithm to compute the sum of elements in an array:

```
def compute_sum(arr):
   total_sum = 0
   for num in arr:
      total_sum += num
   return total sum
```

To analyze the time complexity:



- •Basic operation: The addition operation total sum += num within the loop.
- •Frequency: The loop iterates over each element exactly once, so the operation is performed n times, where n is the number of elements in the array.
- •Growth rate: The frequency is n, hence the time complexity is O(n).

Space complexity, on the other hand, refers to the amount of memory required by an algorithm to process the input data. Similar to time complexity, it is also expressed in Big O notation and accounts for both the auxiliary space (extra space or temporary space used by the algorithm) and the input space (space taken by the inputs).

Considerations for space complexity include:

- •Input size: The memory required for the input data itself.
- •Auxiliary space: Additional memory utilized by variables, data structures, and function call stacks during the execution.

Revisiting the same example, the space complexity can be analyzed as follows:

- Input size: The array arr requires O(n) space.
- •Auxiliary space: The variable total_sum uses O(1) space as it only stores a single value.
- •Total space complexity: The dominant term is O(n), accounting for the input array, leading to a space complexity of O(n).

Example 2: Analyzing a Recursive Algorithm

Consider a recursive Python function to compute the factorial of a number:

```
def factorial(n):
    if n == 0:
        return
    1 else:
        return n * factorial(n - 1)
```

To analyze the time and space complexity:

•Time Complexity:

```
^{\circ}Basic operation: The multiplication n * factorial(n - 1) and the function call factorial (n - 1).
```

 \circ Frequency: The function factorial is called recursively n times before reaching the base case. Each call involves a multiplication operation.

 \circ Growth rate: The time complexity is O(n) due to n recursive calls.

•Space Complexity:



Input size: n is local to each function call and takes O(1) space.

•Auxiliary space: Each function call adds a frame to the call stack. Since there are *n* calls before reaching the base case, *n* frames are maintained on the call stack.

 \circ Total space complexity: The space complexity, primarily due to the recursive call stack, is O(n).

Example 3: Complex Example with Nested Loops

Consider the following Python code to sort an array using the bubble sort algorithm:

Analyzing this example:

•Time Complexity:

```
•Basic operation: The comparison arr[j] > arr[j+1] and the swap
arr[j], arr[j+1] = arr[j+1], arr[j].

•Frequency:
```

Outer loop runs n times.

Inner loop runs n-i-1 times, resulting in approximately comparisons/swaps in the worst case.

•Growth rate: The time complexity is $O(n^2)$.

•Space Complexity:

Input size: The array arr requires O(n) space.

•Auxiliary space: Bubble sort uses a constant amount of extra space (only a few variables).

 \circ Total space complexity: The space complexity is O(n).

This systematic approach to analyzing both time and space complexities is crucial for understanding the limitations and performance of algorithms in varying scenarios. It aids in making informed decisions when choosing the most efficient algorithm and data structure for particular tasks, ensuring optimal performance and resource utilization.

1.10 Choosing the Right Data Structure



Selecting an appropriate data structure is a critical aspect of software development and is key to optimizing performance and ensuring the efficiency of an algorithm. The choice of data structure can significantly impact both the time complexity and space complexity of an application, making it essential to consider various factors when making this decision.

To systematically approach the selection process, consider the following criteria:

- •Nature of the Data: Analyze the type and structure of the data. For instance, if data needs to be stored sequentially, arrays or linked lists may be suitable. If relationships between data elements are hierarchical, trees might be a more appropriate structure.
- •Operations Required: Identify the operations that will be performed most frequently. Data structures vary in operational efficiency. For example, if fast retrieval is crucial, hash tables offer average-case constant time complexity, O(1). Conversely, if data needs frequent sorting, balanced trees like AVL or Red-Black Trees might be preferable due to their logarithmic time complexity, $O(\log n)$.

```
# Python example to demonstrate different data structures
# Array for sequential data access.
arr = [1, 2, 3, 4, 5]
# Dictionary for key-value pair operations with average O(1) access time.
hash_map = {'a': 1, 'b': 2, 'c': 3}
# Using a custom class for tree structures.
class TreeNode:
    def___init_(self, key):
        self.left = None
        self.right = None
        self.val = key
# Basic operations can be defined to utilize these structures effectively.
```

- •Memory Constraints: Consider the memory overhead associated with a data structure. For instance, linked lists use more memory than arrays due to storage of additional pointers. Thus, in memory-constrained environments, the use of more space-efficient data structures, such as arrays, may be justified.
- •Algorithmic Complexity: Evaluate the time complexity for the operations your application will perform. Analyze best, average, and worst-case scenarios. Balanced trees maintain $O(\log n)$ for insertion, deletion, and search operations, making them efficient for diverse operation requirements.



•Ease of Implementation and Maintenance: - Consider how easy it is to implement and maintain the data structure. Simpler structures like arrays or stacks might be easier to implement, debug, and maintain compared to more complex structures like Graphs, Tries, or self-balancing Binary Search Trees.

Let's consider practical scenarios and analyze the best data structure choices based on the defined criteria:

•Real-time Search and Retrieval: - If the primary requirement is real-time retrieval of data elements, hash tables are highly efficient due to their average O(1) lookup time. However, they must be implemented with appropriate collision resolution strategies (like chaining or open addressing) to manage the worst-case O(n) time complexity when collisions occur.

```
# Python code for a simple hash table with separate chaining.
 class HashTable:
    def___init_(self):
      self.table = [[] for in range(10)]
   def hash function(self, key):
      return hash(key) %
      len(self.table)
   def insert(self, key, value):
      index
      self. hash function(key) for
      pair in self.table[index]:
         if pair[0] ==
            key: pair[1] =
            value return
      self.table[index].append([key, value])
   def search(self, key):
      index = self. hash function(key)
      for pair in self.table[index]:
         if pair[0] == key:
            return pair[1]
      return None
# Output of hash table insertion and retrieval
>>> ht = HashTable()
>>> ht.insert('a', 1)
```

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>>> ht.search('a')



```
1
>>> ht.insert('b', 2)
>>> ht.search('b')
2
```

•Hierarchical Data Representation: - Trees are suitable when the data is hierarchical. Binary Search Trees (BSTs) allow ordered data representation with logarithmic time complexity for insertion, deletion, and lookup operations. For balanced operations, self-balancing trees like AVL or Red-Black Trees are recommended.

```
# Python code for a basic binary search tree.
class BSTNode:
  def___init_(self, key):
      self.left = None
      self.right = None
      self.val = key
  def insert(self,
      key): if self.val:
         if key < self.val:
            if self.left is None:
               self.left = BSTNode(key)
            else:
               self.left.insert(key)
         elif key > self.val:
            if self.right is None:
               self.right = BSTNode(key)
            else:
               self.right.insert(key)
      else:
         self.val = key
   def search(self,
      key): if key <
      self.val:
         if self.left is None:
            return None
         return
      self.left.search(key) elif key
      > self.val:
         if self.right is None:
            return None
```

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return self.right.search(key)



```
# Usage of the BST implementation
>>> root = BSTNode(10)
>>> root.insert(5)
>>> root.insert(15)
>>> root.search(15)
<__main__.BSTNode object at 0x...>
>>> root.search(7)
```

else:

•Sequential Data Processing: - For operations requiring first-in-first-out (FIFO) order, queues are optimal. Queues can be efficiently implemented using arrays or linked lists, with each offering different trade-offs in terms of complexity and memory usage.

```
# Python code for a simple queue.
 class Queue:
    def___init_(self):
       self.queue = []
    def enqueue(self, item):
       self.queue.append(item)
    def dequeue(self):
      if len(self.queue) <</pre>
         1: return None
      return self.queue.pop(0)
    def size(self):
      return len(self.queue)
# Output for queue operations
>>> q = Queue()
>>> q.enqueue(1)
>>> q.enqueue(2)
>>> q.dequeue()
```



By carefully evaluating the nature of data, required operations, memory constraints, algorithmic complexity, and implementation & maintenance constraints, a well-considered choice of data structure can significantly optimize the overall performance of an application.



Chapter 2 Python Programming Basics

This chapter provides an overview of essential Python programming concepts, starting with basic syntax and variable declarations. It covers fundamental data types and structures, control flow statements, and the creation and use of functions and modules. Additionally, it introduces file handling, exception handling, and the utilization of libraries. The chapter concludes with an introduction to object-oriented programming, laying the groundwork for further exploration of data structures and algorithms in Python.

2.1 Introduction to Python

Python is a high-level, interpreted programming language known for its ease of learning, readability, and versatility. Guido van Rossum created Python in the late 1980s, and it has since evolved into one of the most widely used programming languages globally, particularly in data analysis, web development, artificial intelligence, and scientific computing.

Python supports multiple programming paradigms, including procedural, object-oriented, and functional programming. This flexibility allows developers to select the most appropriate paradigm for a given problem, making it a powerful tool for a wide range of applications.

Python's design philosophy emphasizes code readability, simplicity, and explicitness. The language features a clean and straightforward syntax that makes it accessible to beginners while powerful enough for experienced developers to build large-scale applications. The following code snippet illustrates a simple Python program that prints "Hello, World!":

```
print("Hello, World!")
```

When executed, the output will be:

Hello, World!

Python's interactive interpreter allows for immediate feedback, further enhancing its ease of use as a learning tool. Users can execute Python code snippets directly in the interpreter, allowing for rapid experimentation and debugging. To start the interpreter, simply type 'python' in the command line if Python is installed correctly.

One of Python's significant strengths is its extensive standard library, which provides modules and functions for various tasks, such as file I/O, system interaction, and data manipulation. This comprehensive library means that common programming needs are often met with built-in solutions, reducing the need for external dependencies.

Additionally, Python has a vast ecosystem of third-party libraries and frameworks, extending its capabilities significantly. Popular libraries such as NumPy, pandas, and Matplotlib are invaluable for scientific and numerical computing. At the same time, frameworks like Django and Flask are widely used in web development. Through the package management system 'pip', users can easily install and manage these external libraries.

Python's development environment is also highly flexible. It is available on multiple operating systems, including Windows, macOS, and various distributions of Linux, ensuring a consistent experience across different platforms. The language is open-source, with a vibrant community contributing to its continuous improvement and the development of new tools and libraries.

Python's popularity can be attributed to several factors:

Ease of Learning and Use: Python's syntax is intuitive and permits shorter development times compared to other languages.

Versatility: It supports various programming paradigms and can be used for scripting, automation, web development, data analysis, and more.

Extensive Libraries: Both the standard library and third-party modules cater to a wide array of applications.

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Community and Support: A large, active community provides expansive documentation, abundant online resources, and a wealth of community-contributed code.

Interoperability: Python can interface with other languages and systems, making it ideal for integration purposes.

A fundamental component of Python is its dynamically typed nature, meaning that variable types are interpreted at runtime. This feature allows for greater flexibility, though it also necessitates careful handling of variables to prevent type-related errors during execution:

```
x = 10 # x is an integer
x = "text" # x is now a string
print(x)
```

The output will be:

text

Python's memory management is handled automatically by a built-in garbage collector, which reclaims memory for reallocation. This automatic management relieves developers from manually managing memory allocation and deallocation, which reduces the likelihood of memory leaks and other related bugs.

Python syntax and the indentation structure play a crucial role in defining the scope of loops, functions, and classes. Proper indentation is not just a stylistic choice but a requirement for the correct execution of Python programs. Indentation typically consists of four spaces per level:

```
def greet(name):
    if name:
        print(f"Hello, {name}!")
    else:
        print("Hello, World!")
```

Executing 'greet("Alice")' would produce:

Hello, Alice!

If no name is provided by calling 'greet("")', the function returns:

Hello, World!

Understanding how Python handles variables and memory, along with its robust standard library and third-party ecosystem, sets the foundation for effectively leveraging Python in various programming scenarios. The simplicity of Python's syntax, combined with its powerful features, makes it a language of choice for both novice and experienced programmers.

2.2 Setting Up Python Environment

To begin your journey into Python programming, initializing your development environment is critical. This section will guide you through the installation of Python, setting up a text editor or Integrated Development Environment (IDE), and verifying your setup. The instructions provided will be suitable for Windows, macOS, and Linux operating systems.

Installing Python

The Python language is maintained by the Python Software Foundation, and the latest versions can be downloaded from the official Python website (https://www.python.org/). As of the latest update, Python 3.10 or later is recommended.

Windows:

1. Navigate to the Python download page (https://www.python.org/downloads/).

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- 2. Download the executable installer for Windows.
- 3. Run the installer and ensure you check the box labeled Add Python to PATH.
- 4. Select *Install Now* and follow the prompts to complete the installation.

macOS:

- 1. Download the latest Python installer from the same Python download page.
- 2. Open the downloaded .pkg file and follow the prompts in the installation wizard.
- 3. Alternatively, you can install Python using Homebrew with the command:

```
brew install python
```

Linux:

1. Most Linux distributions come with Python pre-installed. You can check the installed version using:

```
python3 --version
```

2. If Python is not installed or you need to upgrade, use your package manager. For instance, on Debian-based systems:

```
sudo apt update
sudo apt install python3.10
```

3. For Red Hat-based systems, use:

```
sudo dnf install python3
```

Setting Up an Integrated Development Environment (IDE)

A robust IDE can simplify coding by providing features like syntax highlighting, code completion, and debugging tools. Several popular options are available:

▼S Code: VS Code, or Visual Studio Code, is a free IDE developed by Microsoft. It is lightweight yet powerful, supporting Python via extensions.

Download and install VS Code from https://code.visualstudio.com/.

Open VS Code and go to the Extensions view by clicking on the square icon in the sidebar or pressing Ctrl+Shift+X.

Search for the *Python Extension* provided by Microsoft and install it.

PyCharm: PyCharm, developed by JetBrains, is a popular choice among professional developers.

Download PyCharm from https://www.jetbrains.com/pycharm/download/.

Follow the installation instructions specific to your operating system.

Open PyCharm and configure the Python interpreter by navigating to *File > Settings > Project: roject name > Python Interpreter.</code>*

Jupyter Notebook: Jupyter is particularly useful for data science projects and educational purposes.

Install Jupyter using pip:

```
pip install notebook
```

Launch Jupyter Notebook by running:

```
jupyter notebook
```

Verifying Your Setup

Once installation and setup are complete, verify that Python and your preferred IDE are correctly configured.

Check Python Installation: Open a terminal (command prompt on Windows), and execute:

```
python --version
# or if installed as python3
python3 --version
```

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The output should display the installed Python version, confirming the installation.

Running Your First Python Script: Create a simple Python script to ensure everything is functioning correctly.

```
Open your chosen IDE or a text editor.
```

Write the following code and save it as *hello.py*:

```
print("Hello, World!")
```

Run the script from the terminal:

```
python hello.py
```

The output should be:

Hello, World!

This confirms that your Python environment is set up correctly and you are ready to proceed with further Python programming.

2.3 Basic Syntax and Variables

Python's simplicity and readability make it a popular programming language for beginners and experienced developers alike. Understanding the basic syntax is crucial for writing clean and efficient Python code. This section covers the foundational elements of Python syntax, including variable declarations, comments, and basic data types.

Basic Syntax

Python code is executed line by line, and the language emphasizes the use of indentation to define blocks of code. There are a few key syntax rules to be aware of:

Indentation: Python uses indentation to define the scope of loops, functions, and other constructs. The recommended indentation level is four spaces.

Case sensitivity: Python is case-sensitive, meaning that variable names are treated differently if their case differs.

Comments: Comments are important for documenting code. Single-line comments begin with the # symbol, while multi-line comments are enclosed within triple quotes (""" . . . """).

```
# This is a single-line comment
"""
This is a multi-line comment
It can span multiple lines
"""

if True:
    print("Hello, World!") # Indented line
```

The above example showcases a simple conditional statement, where the print statement is indented to signify that it belongs to the if block.

Variables

Variables are used to store data that can be referenced and manipulated within a program. Python is dynamically typed, meaning that variable types do not need to be declared explicitly. Instead, the type is inferred at runtime based on the value assigned.



```
# Declaring variables
x = 5
y = "Hello"
z = 3.14
# Printing variable values
print(x)
print(y)
print(z)
```

The variable x is assigned an integer value, y is assigned a string, and z is assigned a floating-point number. The print function is used to output the values of these variables.

Variable Naming Conventions

Certain best practices should be followed for naming variables to ensure readability and maintainability:

Variable names should start with a letter (a-z, A-Z) or an underscore ().

- Variable names can contain letters, digits (0-9), and underscores. ■
- Variable names should be descriptive and meaningful.
- Use snake_case (lowercase words separated by underscores) for variable names.

```
valid_variable_name = 42
_validVariableName = "Python"
another_valid_name123 = [1, 2, 3]

# Invalid names
linvalid = "wrong" # Starts with a digit
invalid-name = 10 # Contains a hyphen
```

Basic Data Types

Python supports several built-in data types. Here, we focus on four fundamental ones: integers, floats, strings, and booleans.

```
Integers: Whole numbers, such as 1, 2, 3, etc.
Floats: Decimal numbers, such as 3.14, 2.71, etc.
Strings: Sequences of characters, such as "hello", "world", etc.
Booleans: Logical values True and False.
```

```
# Integer
a = 10

# Float
b = 20.5

# String
c = "Python"

# Boolean
d = True

# Printing their types
print(type(a)) # <class 'int'>
print(type(b)) # <class 'float'>
```



```
print(type(c)) # <class 'str'>
print(type(d)) # <class 'bool'>
```

In this example, the type function is used to determine the type of each variable.

```
<class 'int'>
<class 'float'>
<class 'str'>
<class 'bool'>
```

The above output shows the respective data types of the variables a, b, c, and d.

Understanding basic syntax and variable handling forms the core of writing Python programs. Moving forward, this foundational knowledge will be instrumental in grasping more complex programming constructs and data structures.

2.4 Data Types and Structures

Python offers a diverse array of native data types and structures, allowing developers to handle data efficiently and effectively. Understanding these foundational elements is crucial for writing robust and readable code. In this section, we will explore primitive data types like integers and strings, as well as complex data structures such as lists, tuples, sets, and dictionaries.

Primitive Data Types

1. **Integers:** Integers are whole numbers, positive or negative, without decimals. In Python, an integer is defined simply by assigning a number to a variable.

```
x = 5

y = -3

z = 1234567890
```

2. **Floats:** Floats are numbers with decimals. They are used for more precise calculations.

```
a = 5.5
b = -2.3
c = 0.123456789
```

3. **Strings:** Strings are sequences of characters enclosed within single or double quotes.

```
str1 = 'Hello'
str2 = "World"
str3 = "123"
```

Strings can be concatenated, repeated, and sliced. They are immutable, meaning once created, they cannot be altered.

```
# Concatenation
full_str = str1 + " " + str2 # Output: 'Hello World'
# Repetition
repeat_str = str1 * 3 # Output: 'HelloHelloHello'
# Slicing
sub str = full str[0:5] # Output: 'Hello'
```



4. Booleans: Booleans represent one of two values: True or False.

```
is_true = True
is_false = False
```

Boolean values are often used in control flow statements to determine the execution path of the program.

Complex Data Structures

1. Lists: Lists are ordered, mutable collections of items, which can be of different types.

```
my_list = [1, 2, 3, 'a', 'b', 'c']
```

Lists can be indexed and sliced, similar to strings.

```
# Indexing
first_item = my_list[0] # Output: 1
# Slicing
sub_list = my_list[1:4] # Output: [2, 3, 'a']
```

Lists can be modified after creation.

```
# Appending an item
my_list.append(4) # Output: [1, 2, 3, 'a', 'b', 'c', 4]
# Removing an item
my list.remove('a') # Output: [1, 2, 3, 'b', 'c', 4]
```

2. **Tuples:** Tuples are similar to lists, but they are immutable.

```
my tuple = (1, 2, 3, 'a', 'b', 'c')
```

Tuples also support indexing and slicing.

```
# Indexing
first_item_tup = my_tuple[0] # Output: 1
# Slicing
sub tuple = my tuple[1:4] # Output: (2, 3, 'a')
```

3. **Sets:** Sets are unordered collections of unique items.

```
my_set = {1, 2, 3, 'a', 'b', 'c'}
```

Operations on sets include union, intersection, and difference.

```
set1 = {1, 2, 3}
set2 = {3, 4, 5}

# Union
union_set = set1 | set2 # Output: {1, 2, 3, 4, 5}

# Intersection
intersection_set = set1 & set2 # Output: {3}

# Difference
difference set = set1 - set2 # Output: {1, 2}
```

4. **Dictionaries:** Dictionaries are unordered collections of key-value pairs.



```
my_dict = {'name': 'Alice', 'age': 25, 'city': 'New York'}
```

Values in a dictionary can be accessed using keys.

```
# Accessing value
name = my_dict['name'] # Output: 'Alice'

# Adding a new key-value pair
my_dict['email'] = 'alice@example.com' # Output: {'name': 'Alice', 'age': 25, 'city': 'New York', 'email'
# Removing a key-value pair
del my_dict['age'] # Output: {'name': 'Alice', 'city': 'New York', 'email': 'alice@example.com'}
```

Python's data types and structures are versatile and powerful, enabling efficient data manipulation and retrieval. Mastery of these foundational elements will facilitate more advanced programming tasks, ensuring both efficiency and clarity in your code.

2.5 Control Flow Statements

Control flow statements are essential in any programming language as they determine the flow of program execution. In Python, control flow is facilitated by a variety of statements including conditionals, loops, and other constructs that manage execution paths. We will delve into these control flow mechanisms to understand how to direct the execution of code segments efficiently.

Python's control flow statements include:

- **¶**f, elif, and else for conditional execution.
- **€**or loops for iterating over sequences.
- while loops for repeated execution as long as a condition holds true.
- Control flow modifying statements such as break, continue, and pass.

Conditional Statements

Python uses the if statement to execute a block of code based on a condition. The syntax is straightforward:

```
if condition:
    # Block of code to execute if condition is true
```

The condition is evaluated, and if it returns True, the indented block of code below the if statement is executed. You can also use elif and else to handle multiple branches:

```
if condition1:
    # Block of code to execute if condition1 is true
elif condition2:
    # Block of code to execute if condition2 is true
else:
    # Block of code to execute if none of the above conditions are true
```

Example:

```
x = 10
if x < 10:
    print("x is less than 10")
elif x == 10:
    print("x is equal to 10")
else:
    print("x is greater than 10")</pre>
```

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```
Output: x is equal to 10
```

The for Loop

A for loop in Python is used for iterating over a sequence (such as a list, tuple, string, or range). The syntax for a for loop is as follows:

```
for item in sequence:
    # Block of code to execute for each item in sequence
Example:
```

```
fruits = ['apple', 'banana', 'cherry']
for fruit in fruits:
    print(fruit)

Output:
apple
banana
cherry
```

To loop a certain number of times, the range () function is often used:

```
for i in range(5):
    print(i)
Output:
0
1
2
3
4
```

The while Loop

The while loop allows repeated execution as long as a condition remains true:

```
while condition:
    # Block of code to execute as long as condition is true
```

Example:

```
count = 0
while count < 5:
    print(count)
    count += 1

Output:
0
1
2
3</pre>
```

Control Flow Modifying Statements

break, continue, and pass provide additional control over flow within loops.



break is used to exit a loop prematurely:

```
for i in range(10):
    if i == 5:
        break
    print(i)

Output:
0
1
2
3
4
```

continue skips the rest of the loop and proceeds to the next iteration:

```
for i in range(10):
    if i % 2 == 0:
        continue
    print(i)

Output:
1
3
5
7
9
```

pass is a null operation; it is a statement that does nothing and is useful as a placeholder:

```
for i in range(10):
    if i < 5:
        pass
    else:
        print(i)

Output:
5
6
7
8</pre>
```

Understanding these control flow statements and their appropriate usage is fundamental to writing effective and efficient Python code. The examples provided demonstrate the basic syntax and application, enabling you to build more complex logic and functionalities as required.

2.6 Functions and Modules

Python functions and modules are fundamental constructs that facilitate code organization, reuse, and readability. Functions enable the decomposition of complex problems into simpler, manageable units, while modules provide a way to structure Python programs by encapsulating related functionalities.

A function in Python is defined using the def keyword, followed by the function name, parentheses that can contain parameters, and a colon. Indented underneath the function definition line are the statements that make up the body of the function. Consider the following example, which defines a simple function to calculate the factorial of a number:



```
def factorial(n):
    '''This function returns the factorial of a given number n.'''
    if n == 0 or n == 1:
        return 1
    else:
        result = 1
        for i in range(2, n+1):
            result *= i
        return result
```

In this example, factorial is the function name, and n is the parameter. The function first checks if n is 0 or 1 (in which case the factorial is 1) and returns the appropriate value. Otherwise, it uses a for loop to compute the factorial for values greater than 1.

To call the factorial function, you simply use its name followed by the argument in parentheses. For instance, the expression factorial (5) will return 120, as shown below:

```
print(factorial(5))
120
```

Functions can return any type of value, including complex data structures such as lists and dictionaries. Additionally, Python functions can have default parameter values, which allow them to be called with fewer arguments than specified in the definition. An example of this is:

```
def greet(name, message="Hello"):
    '''This function greets a person with a message.'''
    return f"{message}, {name}!"
```

By providing a default value for the message parameter, the greet function can be called with either one or two arguments:

```
print(greet("Alice"))
print(greet("Bob", "Good morning"))
Hello, Alice!
Good morning, Bob!
```

Modules in Python are files containing Python definitions and statements. The file name is the module name with the suffix .py added. A module allows the logical organization of Python code, making it reusable across various programs.

To use a module, you need to import it. The import statement is used for this purpose. For example, the math module provides access to many useful mathematical functions. You can import the math module and use its functions as follows:

```
import math
print(math.sqrt(16)) # Outputs 4.0
print(math.pi) # Outputs 3.141592653589793
4.0
3.141592653589793
```

It's also possible to import specific functions from a module using the from keyword. This can make the code cleaner and avoid namespace conflicts:

```
from math import sqrt, pi
```



```
print(sqrt(25)) # Outputs 5.0
print(pi) # Outputs 3.141592653589793
5.0
3.141592653589793
```

Python's module system also supports custom modules. You can create your own module by writing Python code in a file with a .py extension and then importing it in your program. For instance, if you save the factorial function defined earlier in a file named mymath.py, you can import and use it as follows:

```
import mymath
print(mymath.factorial(6)) # Outputs 720
720
```

Alternatively, you can import specific functions from the custom module:

```
from mymath import factorial
print(factorial(7)) # Outputs 5040
5040
```

By organizing code into functions and modules, you can create more modular, readable, and maintainable programs. These principles will be especially beneficial when dealing with more complex software projects.

2.7 File Handling

File handling is a crucial aspect of any programming language, enabling a program to read from and write to files stored on a disk. In Python, file handling is achieved through built-in functions and methods that allow seamless interaction with files. Understanding these fundamental operations is vital for effectively managing data persistence in various applications.

To begin with, Python provides the open () function to open a file. This function returns a file object, which provides methods and attributes to interact with the file's contents. The basic syntax of the open () function is as follows:

```
file object = open(filename, mode)
```

The filename parameter is a string that specifies the name of the file to be opened. The mode parameter is also a string that specifies the mode in which the file should be opened. The most common modes include:

- r': Opens the file for reading (default mode). The file must already exist.
- w': Opens the file for writing. If the file exists, its content is truncated. If the file does not exist, a new file is created.
- a': Opens the file for appending. New data is written at the end of the file content. If the file does not exist, it creates a new file.
- **♥**b': Opens the file in binary mode.

Here is a practical example of opening a file for reading:

```
file_object = open('example.txt', 'r')
```

Once a file is opened, it is essential to close it to free up resources. The close () method is used for this purpose:

```
file object.close()
```



However, a more efficient approach is using a with statement, which ensures the file is properly closed after its suite finishes, even if an exception is raised. This is demonstrated below:

```
with open('example.txt', 'r') as file_object:
    content = file_object.read()
    print(content)
```

Reading from a file can be done using several methods:

- read (size): Reads the specified number of bytes from the file. If the size argument is omitted, it reads the entire file.
- *readline(): Reads a single line from the file.
- readlines (): Reads all lines in the file and returns them as a list of strings.

Writing to a file similarly employs several methods:

```
write(string): Writes the specified string to the file.
writelines(list of strings): Writes a list of strings to the file.
```

An example of writing to and reading from a file is shown below:

```
# Writing to a file
with open('example.txt', 'w') as file_object:
    file_object.write("This is an example text.\n")
    file_object.write("Writing to files in Python is easy.\n")

# Reading from a file
with open('example.txt', 'r') as file_object:
    content = file_object.read()
    print(content)

This is an example text.
Writing to files in Python is easy.
```

Python also provides functionality for handling binary files, which are typically used for non-text data such as images or executable files. To work with binary files, include a b character in the mode string:

```
# Writing binary data
with open('example.bin', 'wb') as file_object:
    file_object.write(b'\xDE\xAD\xBE\xEF')

# Reading binary data
with open('example.bin', 'rb') as file_object:
    content = file_object.read() print(content)
b'\xDE\xAD\xBE\xEF'
```

Lastly, Python supports random access to file contents through the <code>seek()</code> and <code>tell()</code> methods. The <code>seek(offset, whence)</code> method modifies the current file position, where <code>offset</code> is the byte position to move to, and whence defines the reference point. The <code>tell()</code> method returns the current file position:

```
with open('example.txt', 'rb+') as file_object:
    file_object.write(b'0123456789abcdef')
    file_object.seek(5) # Move to the 6th byte
    print(file object.read(1)) # Print next byte
```

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```
file_object.seek(-3, 2) # Move 3 bytes before the end
print(file_object.read(1)) # Print next byte
b'5'
b'd'
```

Collectively, these operations form the foundation for file handling in Python, enabling robust and efficient data processing workflows.

2.8 Exception Handling

Exception handling in Python is a crucial concept for creating robust and error-resilient programs. Errors and exceptions are inevitable during the execution of a program. They can occur due to various reasons such as invalid user input, device failure, or unforeseen bugs in the code. Python provides a systematic way to catch and handle these exceptions using the try-except block.

An exception is an event detected during runtime that interrupts the normal flow of the program's instructions. In Python, many built-in exceptions can be raised and caught. Some common built-in exceptions include: IndexError, KeyError, ValueError, and TypeError.

The basic syntax for exception handling in Python involves the try and except blocks. Here's a concise example that demonstrates how to handle exceptions in Python:

```
try:
    # Code that may raise an exception
    result = 10 / 0
except ZeroDivisionError:
    # Code to handle the exception
    print("Cannot divide by zero!")
```

In this example, the code inside the try block attempts to divide a number by zero, which raises a ZeroDivisionError. The except block catches this specific exception and prints an error message. If an exception other than ZeroDivisionError were to occur, it would not be caught by this except block.

If you want to handle multiple exceptions, you can specify multiple except blocks:

```
try:
    # Code that may raise multiple exceptions
number = int(input("Enter a number: "))
    result = 10 / number
except ValueError:
    # Handles invalid input (not an integer)
    print("Please enter a valid integer.")
except ZeroDivisionError:
    # Handles division by zero
    print("Cannot divide by zero!")
```

In this code snippet, the try block can raise either a ValueError if the input is not a valid integer or a ZeroDivisionError if the user inputs zero. Each exception is handled by its respective except

block. It is also possible to catch multiple exceptions in a single except block using a tuple of exceptions:

```
try:
   number = int(input("Enter a number: "))
   result = 10 / number
```

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```
except (ValueError, ZeroDivisionError):
    print("Invalid input: Please enter a non-zero integer.")
```

In some cases, you may want to execute some code regardless of whether an exception occurred or not. This is where the finally block comes into play. The finally block always executes after the try and except blocks:

```
try:
   number = int(input("Enter a number: "))
   result = 10 / number
except (ValueError, ZeroDivisionError) as e:
   print(f"An error occurred: {e}")
finally:
   print("Execution complete.")
```

In this example, the finally block will always execute, printing "Execution complete" regardless of whether an exception was raised and handled or not.

Moreover, Python allows the use of the else block in conjunction with try... except. The else block is executed if the code in the try block does not raise an exception:

```
try:
   number = int(input("Enter a number: "))
   result = 10 / number

except (ValueError, ZeroDivisionError) as e:
   print(f"An error occurred: {e}")

else:
   print(f"Result is: {result}")

finally:
   print("Execution complete.")
```

In this scenario, the else block executes only if no exceptions were raised in the try block. The finally block executes in all cases.

Custom exceptions can also be defined to cater to specific needs within your application. A custom exception class can be created by inheriting from the built-in Exception class:

```
class CustomError(Exception):
    """Custom exception class for specific errors."""
    def __init_(self, message):
        self.message = message

try:
    raise CustomError("This is a custom error!")
except CustomError as e:
    print(f"Caught a custom exception: {e.message}")
```

In this code snippet, CustomError is a user-defined exception class. An instance of this class is raised within the try block and subsequently caught in the except block.

By leveraging exception handling effectively, programmers can ensure that their programs are more resilient to runtime errors, thus improving the robustness and reliability of the software.

2.9 Working with Libraries



Libraries in Python are collections of pre-written code that you can import into your programs to utilize existing functionalities. This saves significant time and effort as you don't need to write functions and classes from scratch. Python boasts a rich ecosystem of libraries, ranging from those handling basic tasks such as mathematical calculations, to more complex ones like data visualization and machine learning.

To begin working with libraries in Python, you must first understand how to import them. The import statement is used for this purpose. Let us explore some fundamental use-cases with standard libraries.

1. Using the math Library:

The math library in Python provides access to various mathematical functions like trigonometry, logarithms, and constants such as π . Here is an example of how to use it:

```
import math

# Compute the cosine of a number
cosine_value = math.cos(math.pi / 4)
print(f"The cosine of pi/4 is: {cosine_value}")

# Compute the factorial of a number
factorial_value = math.factorial(5)
print(f"The factorial of 5 is: {factorial_value}")

The output would be:
The cosine of pi/4 is: 0.7071067811865476
The factorial of 5 is: 120
```

2. Using the datetime Library:

The datetime library provides classes for manipulating dates and times. Here's an example:

```
import datetime
 # Get the current date and time
current_date_time = datetime.datetime.now()
print(f"Current date and time: {current date time}")
 # Create a specific date
specific_date = datetime.datetime(2021, 12, 31)
print(f"Specific date: {specific date}")
# Compute the difference between two dates
date1 = datetime.datetime(2021, 1, 1)
date2 = datetime.datetime(2022, 1, 1)
delta = date2 - date1
print(f"Difference between dates: {delta.days} days")
The output would be:
Current date and time: 2023-03-14 15:26:08.776000
Specific date: 2021-12-31 00:00:00
Difference between dates: 365 days
```

3. Using the random Library:

The random library provides functions to generate random numbers. Here is a basic usage:



```
# Generate a random number between 1 and 10
random_number = random.randint(1, 10)
print(f"Random number between 1 and 10: {random_number}")
# Generate a random float number between 0 and 1
random_float = random.random()
print(f"Random float between 0 and 1: {random float}")
```

The output would be a random number and a random float which changes every time the code is run.

```
Random number between 1 and 10: 7
Random float between 0 and 1: 0.567123456789
```

Moving beyond standard libraries, let's explore third-party libraries, which are not included in the standard Python distribution. They can be installed using the package manager pip.

4. Using the NumPy Library:

import random

NumPy is a popular library for numerical operations. To install it, use the following command in the terminal: pip install numpy

Here is an example of how to use NumPy:

```
import numpy as np
# Create a 1-D array
array 1d = np.array([1, 2, 3, 4, 5])
print(f"1-D array: {array_1d}")
# Create a 2-D array
array 2d = np.array([[1, 2, 3], [4, 5, 6]])
print(f"2-D array:\n{array_2d}")
# Perform element-wise addition
array_sum = array_1d + 10
print(f"Array after addition: {array_sum}")
 # Compute the dot product
dot_product = np.dot(array_1d, array_1d)
print(f"Dot product: {dot_product}")
The output would be:
1-D array: [1 2 3 4 5]
2-D array:
[[1 2 3]
 [4 5 6]]
Array after addition: [11 12 13 14 15]
Dot product: 55
```

5. Using the pandas Library:

pandas is a powerful library for data manipulation and analysis. It can be installed using: pip install pandas



Here is an example of using pandas:

```
import pandas as pd
 # Create a DataFrame
data = {'Name': ['Anna', 'Bob', 'Charlie'], 'Age': [24, 27, 22]}
df = pd.DataFrame(data)
print(f"DataFrame:\n{df}")
# Access a column
ages = df['Age']
print(f"Ages:\n{ages}")
 # Perform basic statistical operations
mean age = df['Age'].mean()
print(f"Mean age: {mean age}")
The output would be:
DataFrame:
      Name Age
0
       Anna 24
       Bob
                27
1
2
       Charlie 22
Ages:
0
      24
1
      27
      22
Name: Age, dtype: int64
```

Finally, when working with libraries, it is important to keep your environment organized. Virtual environments allow you to manage dependencies for different projects separately. To create and activate a virtual environment, use the following commands:

```
python -m venv myenv
source myenv/bin/activate # On Windows, use 'myenv\Scripts\activate'
```

Once activated, any packages you install using pip will be contained within this environment. This practice helps to avoid conflicts between dependencies of different projects.

2.10 Introduction to Object-Oriented Programming

Mean age: 24.333333333333333

Object-oriented programming (OOP) is a programming paradigm based on the concept of "objects", which can contain data and code: data in the form of fields (often known as attributes or properties), and code, in the form of procedures (often known as methods). The defining feature of objects is that an object's procedures can access and often modify the data fields of the object with which they are associated. In Python, OOP is a powerful instrument that allows for the creation of classes and objects, facilitating a more intuitive mapping between real-world entities and programming constructs.

A **class** in Python serves as a blueprint for creating objects. This blueprint encapsulates the data (also known as attributes) and functions (known as methods) that the objects created from the class will have. The class itself does not hold the data but defines what data objects instantiated from it can hold. An **object** is an instance of a class.

Consider the following example of defining a simple class in Python:



```
class Dog:
    species = "Canis familiaris"

def __init_(self, name, age):
    self.name = name
    self.age = age

def description(self):
    return f"{self.name} is {self.age} years old"

def speak(self, sound):
    return f"{self.name} says {sound}"
```

In this example, we define a class named <code>Dog</code>. This class has a class attribute <code>species</code> that is shared by all instances of the class. The <code>__init__</code> method is a special method that initializes the object's attributes. Each object created from the <code>Dog class</code> will have <code>name</code> and <code>age</code> attributes. The methods <code>description</code> and <code>speak</code> define behaviors that the <code>Dog objects</code> can perform.

To create an instance of the Dog class, we do the following:

```
my_dog = Dog("Buddy", 9)
print(my_dog.description())
print(my_dog.speak("Woof Woof"))
```

The output of the above code would be:

```
Buddy is 9 years old
Buddy says Woof Woof
```

The concept of **inheritance** in OOP allows for a class to inherit attributes and methods from another class. The class being inherited from is called the *parent* or *base class*, and the class inheriting is called the *child* or *derived class*. The derived class can override or extend the functionalities of the base class.

Consider an example where we have a base class Animal and a derived class Dog:

```
class Animal:
    def __init_(self, name):
        self.name = name

    def move(self):
        print(f'{self.name} is moving')

class Dog(Animal):
    def speak(self, sound):
        print(f'{self.name} says {sound}')
```

Here, the Dog class inherits from the Animal class. It can use the move method defined in Animal and has its own method speak.

Using these classes:

```
my_pet = Dog("Buddy")
my_pet.move()
my pet.speak("Woof Woof")
```

The output would be:



```
Buddy is moving
Buddy says Woof Woof
```

Encapsulation is another key principle of OOP, which means restricting direct access to some of an object's components and can prevent the accidental modification of data. This can be achieved using private attributes and methods by prefixing their names with an underscore:

```
class Car:
    def__init_(self, model, year):
        self._model = model
        self._year = year

    def get_model(self):
        return self._model

    def set_model(self, model):
        self. model = model
```

In this example, model is a private attribute and can be accessed and modified only through the methods get model and set model.

Finally, **polymorphism** allows for using a unified interface to operate on different types of objects. Polymorphism can be seen when a method in different classes implements behavior differently. For example:

```
class Bird:
    def sound(self):
        return "Chirp"

class Dog:
    def sound(self):
        return "Bark"

def make_sound(animal):
    print(animal.sound())

bird = Bird()
dog = Dog()
make_sound(bird)
make_sound(dog)
```

The output would be:

Chirp Bark

The function make sound can operate on any object that has a sound method, demonstrating polymorphism.

Understanding these core principles of OOP in Python—classes and objects, inheritance, encapsulation, and polymorphism—provides a solid foundation for developing more complex and reusable code.



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Chapter 3 Array Structures

This chapter delves into array structures, covering their definition, operations, and various types, including multidimensional arrays. It explores array slicing, sorting, and searching techniques, as well as the concept of dynamic arrays. Practical applications of arrays and considerations for performance optimization are also discussed, providing a comprehensive understanding of this fundamental data structure.

3.1 Introduction to Arrays

An array is a fundamental data structure in computer science, used to store a collection of elements, typically of the same type, in a contiguous block of memory. Each element in an array can be efficiently accessed using its index, which represents its position within the array. This direct access property makes arrays highly efficient for several operations, such as indexing, iterating, and modifying elements.

In Python, arrays can be implemented using built-in data structures such as lists and arrays from the array module. While Python lists are more flexible and can hold elements of any type, the array module provides a more efficient way to store homogeneous data.

```
# Creating a list in Python
list_example = [1, 2, 3, 4, 5]

# Creating an array in Python using the 'array' module
import array as arr

array_example = arr.array('i', [1, 2, 3, 4, 5])
```

In the above code snippet, 'i' denotes a signed integer type, ensuring all elements within array example are integers. The choice between using a



list and an array from the array module depends on the specific requirements of memory efficiency and type constraints.

Arrays are typically zero-indexed, meaning the first element of the array has an index of 0. This indexing mechanism is consistent across various programming languages, including Python. By utilizing indices, it is possible to access or modify specific elements directly.

```
# Accessing elements in a list
second_element = list_example[1]

# Modifying elements in a list
list_example[1] = 10

# Accessing elements in an array
second_element_array = array_example[1]

# Modifying elements in an array
array example[1] = 10
```

Arrays support numerous operations such as appending elements, extending the array with another array, and removing elements. However, it is essential to understand the time complexity of these operations to utilize arrays optimally. Accessing an element by index takes constant time, O(1), due to the direct access nature of arrays. Conversely, appending an element at the end of an array can be an O(1) operation if there is sufficient space, but can degrade to O(n) if the array needs to resize.

```
# Appending elements
list_example.append(6)
array_example.append(6
)

# Extending the array with another array
list_example.extend([7, 8])
array_example.extend(arr.array('i', [7, 8]))
# Removing elements
```

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```
list_example.remove(10)
array_example.remove(10)
```

When an array needs to resize, a new block of memory is allocated, and the existing elements are copied over. This operation is analogous in both lists and arrays. Consequently, frequent resizing can lead to inefficiencies, which is a crucial consideration in applications requiring high performance.

The concept of array slicing further enhances the flexibility of arrays. Slicing allows the creation of a subarray, or segment, from an existing array without copying the elements, thus providing a view into the array. Python supports slicing using a starting index, ending index, and a step value, which can be vital for various algorithms and data manipulation tasks.

```
# Slicing a list
sub_list = list_example[1:4] # elements from index 1 to 3
# Slicing an array
sub_array = array_example[1:4]
```

The utility of arrays is evident in their widespread application across different domains including scientific computing, real-time systems, and multimedia applications. The contiguous memory allocation of arrays ensures that they are cache-friendly, enabling fast access times and efficient memory usage.

Understanding the basic characteristics and operations of arrays lays a strong foundation for grasping more complex data structures and algorithms. Arrays not only serve as building blocks for other data structures such as lists, hash tables, and heaps but also play a critical role in optimizing performance in computational tasks. As we progress through this chapter, we will explore advanced topics such as dynamic arrays, array sorting, and searching, which further illustrate the versatility and efficiency of this fundamental data structure.

3.2 Array Operations

An array is a collection of elements identified by index or key. Array operations are fundamental to utilizing arrays effectively in Python and other www.gisurat.com 7777 95 68 77

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programming languages. This section will explore various array operations, including accessing elements, updating elements, inserting elements, deleting elements, traversing arrays, and understanding array length.

Accessing elements in an array is performed using indices, which start from zero in Python. For instance, if we have an array arr and need to access the first element, we use arr[0]. Access to any element is constant time, or O(1), due to direct indexing.

```
arr = [10, 20, 30, 40, 50]
print(arr[0]) # Output: 10
print(arr[3]) # Output: 40
10
40
```

Updating elements involves assigning a new value to a specific index in the array. The time complexity for updating an element is also O(1), indicating constant time operation.

```
arr[1] = 25
print(arr) # Output: [10, 25, 30, 40, 50]
[10, 25, 30, 40, 50]
```

Array insertion can be categorized into different types: inserting at the beginning, in the middle, or at the end. Inserting an element at the end, commonly known as appending, is a frequent operation and is O(1) on average in dynamic arrays since they automatically resize. However, inserting at other positions involves shifting subsequent elements, which has a time complexity of O(n).

```
arr.append(60)
print(arr) # Output: [10, 25, 30, 40, 50, 60]
arr.insert(2, 35)
print(arr) # Output: [10, 25, 35, 30, 40, 50, 60]
[10, 25, 30, 40, 50, 60]
[10, 25, 35, 30, 40, 50, 60]
```

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Deleting elements can be done at any specified position. Similar to insertion, deleting an element requires shifting subsequent elements if the deletion occurs in the middle or beginning, with a time complexity of O(n).

```
del arr[2]
print(arr) # Output: [10, 25, 30, 40, 50, 60]
arr.remove(50)
print(arr) # Output: [10, 25, 30, 40, 60]
[10, 25, 30, 40, 50, 60]
[10, 25, 30, 40, 60]
```

Traversing an array refers to accessing each element of the array for various operations such as printing or modifying elements. This operation typically has a time complexity of O(n). Traversal can be implemented in many ways, including using a for loop.

```
for element in
    arr:
    print(element)

10
25
30
40
60
```

Determining the length of an array is essential for various operations, such as bounds checking and iteration. The length of an array can be retrieved using the len() function in Python, which operates in O(1) time.

```
length = len(arr)
print(length) # Output:
5
```

The array operations discussed are intrinsically linked with many algorithms and data structures. For optimal performance, one must consider the underlying implementation and complexity of these operations.

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Understanding these operations paves the way for more advanced topics,



such as sorting and searching, which heavily rely on array manipulation. This knowledge base is crucial for further exploration into more complex data structural concepts and their applications in software development.

3.3 Types of Arrays

Arrays are a fundamental data structure in computer science and are utilized in numerous applications due to their simplicity and efficiency in both space and time complexity. Different types of arrays are leveraged depending on the requirements of an algorithm or application. Understanding these types is essential to effectively address varying computational problems.

1. One-Dimensional Arrays

A one-dimensional array is the simplest form of array and can be visualized as a list of elements, each identified by a unique index. This type of array is linear, and elements are accessed using a single index. If declared and initialized in Python, a one-dimensional array can be created using a list:

```
one d array = [1, 2, 3, 4, 5]
```

In the above array, the element at index 0 is 1, at index 1 is 2, and so on.

2. Multidimensional Arrays

Multidimensional arrays are arrays of arrays. They can be of two or more dimensions, offering higher levels of data organization and access.

2.1. Two-Dimensional Arrays

A two-dimensional array is essentially a list of lists and can be visualized as a table with rows and columns:

```
two_d_array = [
    [1, 2, 3],
    [4, 5, 6],
    [7, 8, 9]
]
```

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Here, the element at row 0, column 0 is 1, the element at row 1, column 2 is 6, and so forth.

2.2. Higher-Dimensional Arrays

Higher-dimensional arrays, such as three-dimensional arrays, extend this concept further. A three-dimensional array can be visualized as a cube of elements:

```
three_d_array =
   [ [
        [1, 2],
        [3, 4]
   ],
   [
        [5, 6],
        [7, 8]
   ]
]
```

The indexing for these arrays follows a hierarchical nesting, and the element at index [1][1][0] is 7.

3. Dynamic Arrays

Dynamic arrays differ from static arrays in their ability to resize dynamically when elements are added or removed. They provide greater flexibility in data handling compared to standard arrays.

In Python, a dynamic array can be implemented using the built-in list structure, which automatically resizes as elements are appended or deleted:

```
dynamic_array = []
dynamic_array.append(1
)
dynamic_array.append(2
)
```

Here, the list starts empty and expands as elements are appended. The underlying implementation uses capacity doubling to manage dynamic

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growth efficiently.



4. Associative Arrays (Dictionaries)

In contrast to traditional arrays that use integer indices, associative arrays, or dictionaries, use key-value pairs for indexing. This allows for more versatile data retrieval and storage:

```
associative_array =
    { "name":
    "Alice", "age":
    30,
    "city": "New York"
}
```

The above dictionary uses strings as keys. The value associated with the key "name" is "Alice", with the key "age" is 30, etc.

5. Sparse Arrays

Sparse arrays are specially designed to handle data that contains a majority of default values (typically zeroes). They store only non-default values along with their indices, optimizing the storage and management of large, sparse data sets. In Python, sparse arrays can be efficiently implemented using dictionaries:

```
sparse_array =
    { 0: 1,
    50: 13,
    123: 5
}
```

In this example, the dictionary keys represent indices, and the values represent the non-zero values at those indices.

6. Jagged Arrays

Jagged arrays are multidimensional arrays where rows have different lengths, unlike traditional rectangular arrays where all rows maintain a uniform length. In Python, jagged arrays can be represented using lists with lists of varying lengths:

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```
jagged_array =
   [ [1, 2, 3],
   [4, 5],
   [6, 7, 8, 9]
```

Each sub-list can have a different number of elements, making it flexible in scenarios where data entries vary in size.

Various additional types of arrays exist to fit specific needs and optimize performance under different constraints. Understanding these types extensively allows for efficient and effective use of arrays in computing tasks, ensuring that the appropriate data structure is chosen based on the specific requirements of the application.

3.4 Multidimensional Arrays

Multidimensional arrays extend the concept of single-dimensional arrays to arrays of arrays, allowing for more complex data representation and manipulation. These structures are particularly useful in scientific computing, image processing, and any domain where data is naturally represented in multiple dimensions.

A **two-dimensional array**, the simplest form of a multidimensional array, can be visualized as a grid or a table, where data elements are arranged in rows and columns. Higher-dimensional arrays generalize this idea, stacking two-dimensional arrays along additional dimensions.

Declaration and Initialization

To declare and initialize multidimensional arrays in Python, we use nested lists. For example, a two-dimensional array A with 3 rows and 4 columns can be initialized as follows:

```
A = [ [1, 2, 3, 4], [5, 6, 7, 8],
```



```
[9, 10, 11, 12]
```

For larger dimensions or more complex initializations, Python's numpy library provides a more efficient and convenient interface:

```
import numpy as np
A = np.array([
    [1, 2, 3, 4],
    [5, 6, 7, 8],
    [9, 10, 11, 12]
])
```

Accessing Elements

Accessing elements in a multidimensional array requires specifying the indices for all dimensions. For example, to access the element in the 2nd row and 3rd column of array A, one would use the following syntax in standard list and numpy notation:

```
element = A[1][2] # Standard list
element np = A[1, 2] # numpy array
```

This ability to precisely index each dimension is crucial for tasks such as matrix operations, applying transformations, or retrieving data subsets.

Iterating Over Elements

Iterating through a multidimensional array can be achieved with nested loops. For instance, iterating over all the elements of a two-dimensional array involves:

```
for row in A:
   for element in
    row:
    print(element)
```

For numpy arrays, leveraging numpy's built-in functions can enhance performance and readability:

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```
np.apply_along_axis(print, 1, A)
```

Multidimensional Slicing

Multidimensional arrays support slicing operations to access subarrays. The syntax extends the one-dimensional slicing with comma-separated slices. For example, to obtain the first two rows and the last two columns of array A, one would use:

```
subarray = A[:2, -2:] # numpy array
```

Reshaping Arrays

The shape of a numpy array can be altered using the reshape method, which is particularly useful for data preparation and transformations.

Reshaping does not alter the original data but provides a different way to index it:

```
reshaped A = A.reshape((2, 6))
```

Here, the array A is reshaped from a 3x4 array to a 2x6 array. The total number of elements must remain constant.

Applications in Matrix Operations

Multidimensional arrays serve as the backbone for matrix operations in many scientific and engineering fields. Operations such as matrix addition, multiplication, and transposition are fundamental. numpy facilitates these operations efficiently:

```
import numpy as np

# Matrix addition

B = np.array([
    [13, 14, 15, 16],
    [17, 18, 19, 20],
    [21, 22, 23, 24]

])

result_add = np.add(A, B)
```

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```
# Matrix multiplication
result_mul = np.dot(A, B.T)
# Transposition
result transpose = A.T
```

These operations are optimized in numpy, ensuring high performance even for large datasets.

Higher-Dimensional Arrays

Building upon the concept of two-dimensional arrays, higher-dimensional arrays (3D, 4D, etc.) are often used in advanced applications such as volumetric data analysis and tensor operations. These arrays are naturally suited for complex data structures like RGB images (3D) or spatiotemporal data (4D).

For example, a three-dimensional array representing a bundle of 2D images (say, 5 images of 4x3 dimensions) can be initialized and manipulated as follows:

```
C = \text{np.random.randint}(0, 256, (5, 4, 3)) \# 5 \text{ images of } 4x3
resolution
```

Element access in such arrays still follows multidimensional indexing:

```
element 3d = C[2, 1, 0] # Element in 3rd image, 2nd row, 1st column
```

Practical Considerations

When working with multidimensional arrays, it is crucial to consider memory consumption and computational complexity. Multidimensional arrays, especially in higher dimensions, can quickly consume significant memory. Tools such as numpy provide efficient memory handling but understanding underlying data structures and efficient manipulation techniques remains essential for optimal performance.

3.5 Array Slicing



Array slicing is a powerful feature in Python that allows for extracting subsets of arrays. This operation involves specifying a range of indices to obtain a contiguous segment of the array. The practice of slicing arrays can be particularly useful for data manipulation, offering a flexible means to access and modify array elements.

In Python, array slicing is facilitated by the slicing operator, denoted by the colon (":"), and can be applied to one-dimensional and multidimensional arrays. The general syntax for slicing is:

```
array[start:stop:step]
```

Parameters:

- •start The index indicating where the slice starts. The element at this index is included in the slice.
- •stop The index indicating where the slice ends. The element at this index is not included in the slice.
- •step The interval between indices. By default, the step size is 1.

Examples of One-dimensional Array Slicing:

Consider a one-dimensional array of integers:

```
import numpy as np
arr = np.array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

1. Extracting elements from index 2 to 5:

```
slice1 =
arr[2:6]
print(slice1)
[2 3 4 5]
```

2. Extracting elements from the beginning to index 3:

```
slice2 =
arr[:4]
print(slice2)
[0 1 2 3]
```



3. Extracting elements from index 5 to the end:

```
slice3 =
arr[5:]
print(slice3)
[5 6 7 8 9]
```

4. Using a step size of 2:

```
slice4 =
arr[1:9:2]
print(slice4)
[1 3 5 7]
```

Examples of Multidimensional Array Slicing:

Consider a two-dimensional array:

1. Extracting a sub-array:

```
sub_arr1 = arr2d[1:3,
:2] print(sub_arr1)

[[4 5]
  [8 9]]
```

2. Extracting all rows of the first two columns:

```
sub_arr2 = arr2d[:,
:2] print(sub_arr2)
[[ 0     1]
     [ 4     5]
     [ 8     9]
     [12     13]]
```

3. Extracting the last two rows and the last two columns:



```
sub_arr3 = arr2d[2:,
2:] print(sub_arr3)
[[10 11]
  [14 15]]
```

4. Slicing with step size:

```
sub_arr4 = arr2d[::2,
::2] print(sub_arr4)

[[ 0 2]
  [ 8 10]]
```

Negative Indexing: Slices can also include negative indices, which count from the end of the array. Negative indexing provides a concise way to access elements from the end of the array.

1. Extracting the last three elements:

```
slice5 =
arr[-3:]
print(slice5)
[7 8 9]
```

2. Extracting elements except the last two:

```
slice6 =
arr[:-2]
print(slice6)

[0 1 2 3 4 5 6 7]
```

Advanced Slicing Techniques:

Slicing can be combined with array manipulation functions to achieve more complex operations. One common technique is boolean slicing, where slices are created based on specified conditions.

1. Boolean Slicing:

```
bool slice = arr[arr % 2 ==
```

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0] print(bool_slice)



[0 2 4 6 8]

2. Conditional Slicing:

```
cond_slice = arr[(arr > 3) & (arr <
8)] print(cond_slice)
[4 5 6 7]</pre>
```

Understanding how to effectively use array slicing is fundamental to working with arrays in Python. This deepens the capability to manage data efficiently, from simple sub-array extraction to advanced conditional data manipulations.

3.6 Array Sorting

Array sorting is a fundamental concept in computer science and is pivotal for organizing data efficiently. Sorting an array involves arranging its elements in a specific order, typically ascending or descending. Sorting algorithms vary in complexity and efficiency, and selecting the appropriate algorithm depends on factors such as the size of the array, the nature of the data, and the performance requirements.

Common Array Sorting Algorithms:

- •Bubble Sort: This simple algorithm repeatedly steps through the list, compares adjacent elements, and swaps them if they are in the wrong order. Its simplicity comes at the cost of efficiency, as it has an average and worst-case complexity of $O(n^2)$.
- •Selection Sort: This algorithm divides the array into a sorted and an unsorted part. It repeatedly selects the smallest (or largest, depending on the order) element from the unsorted part and moves it to the end of the sorted part. It also has a time complexity of $O(n^2)$.
- •Insertion Sort: This algorithm builds the sorted array one element at a time, placing each new element in its correct position. While its average and worst-case complexity is $O(n^2)$, it is more efficient than bubble sort and selection sort for small data sets or nearly sorted arrays.
- •Merge Sort: This divide-and-conquer algorithm splits the array into halves, recursively sorts each half, and then merges the sorted halves. It

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- offers a significant improvement in efficiency with a time complexity of $O(n \log n)$.
- •Quick Sort: Another divide-and-conquer algorithm, quick sort, selects a "pivot" element and partitions the array into sub-arrays, which are then sorted recursively. Its average-case complexity is $O(n \log n)$, but the worst case is $O(n^2)$ if the pivot selection is poor.
- •**Heap Sort:** This comparison-based algorithm uses a binary heap data structure to sort the array. It has a time complexity of $O(n \log n)$.

Example Implementations:

Bubble Sort:

```
def
  bubble_sort(arr):
  n = len(arr)
  for i in range(n):
    for j in range(0,
        n-i-1): if arr[j] >
        arr[j+1]:
        arr[j], arr[j+1] = arr[j+1],
    arr[j] return arr

# Example Usage
array = [64, 34, 25, 12, 22, 11, 90]
sorted_array = bubble_sort(array)
print("Sorted array:",
sorted_array)
```

Selection Sort:

```
def
    selection_sort(arr):
    n = len(arr)
    for i in
        range(n):
        min_idx = i
        for j in range(i+1, n):
        if arr[j]
```

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```
arr[min_idx]: min_idx
= j
arr[i], arr[min_idx] = arr[min_idx],
arr[i] return arr
```



```
# Example Usage
array = [64, 34, 25, 12, 22, 11, 90]
sorted_array =
selection_sort(array) print("Sorted
array:", sorted array)
```

Insertion Sort:

```
def
   insertion sort(arr):
   n = len(arr)
   for i in range(1,
     n): key = arr[i]
      j = i - 1
      while j >= 0 and key <
         arr[j]: arr[j + 1] =
         arr[j]
         j -= 1
      arr[j + 1] =
   key return arr
# Example Usage
array = [64, 34, 25, 12, 22, 11, 90]
sorted array =
insertion sort(array) print("Sorted
array:", sorted array)
```

Merge Sort:

```
def
  merge_sort(arr):
  if len(arr) > 1:
    mid =
    len(arr)//2 L =
    arr[:mid]
    R = arr[mid:]

    merge_sort(L
)
```

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```
merge_sort(R
)

i = j = k = 0

while i < len(L) and j <
   len(R): if L[i] < R[j]:</pre>
```



```
arr[k] =
            L[i] i += 1
         else:
            arr[k] =
            R[j] j += 1
         k += 1
      while i <
         len(L):
         arr[k] = L[i]
         i += 1
         k += 1
     while j <
         len(R):
         arr[k] = R[j]
         j += 1
         k += 1
   return arr
# Example Usage
array = [64, 34, 25, 12, 22, 11, 90]
sorted array = merge sort(array)
print("Sorted array:",
sorted array)
```

Quick Sort:

```
def partition(arr, low,
  high): i = (low-1)
  pivot = arr[high]

for j in range(low,
   high): if arr[j] <=
  pivot:
   i = i+1
   arr[i], arr[j] = arr[j], arr[i]</pre>
```

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arr[i+1], arr[high] = arr[high],
arr[i+1] return (i+1)



```
def quick_sort(arr, low,
   high): if low < high:
      pi = partition(arr, low,
      high) quick_sort(arr, low,
      pi-1) quick_sort(arr, pi+1,
      high)
   return arr

# Example Usage
array = [64, 34, 25, 12, 22, 11, 90]
sorted_array = quick_sort(array, 0,
len(array)-1) print("Sorted array:",
sorted array)</pre>
```

Heap Sort:

```
def heapify(arr, n,
   i): largest = i
   1 = 2 * i +
   1 r = 2 * i
   + 2
   if l < n and arr[i] <
      arr[l]: largest = 1
   if r < n and arr[largest] <</pre>
      arr[r]: largest = r
   if largest != i:
      arr[i], arr[largest] = arr[largest],
      arr[i] heapify(arr, n, largest)
def
  heap sort(arr):
   n = len(arr)
   for i in range (n//2 - 1, -1,
      -1): heapify(arr, n, i)
```

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```
for i in range(n-1, 0, -1):
    arr[i], arr[0] = arr[0],
    arr[i]
```



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```
heapify(arr, i,
0) return arr

# Example Usage
array = [64, 34, 25, 12, 22, 11, 90]
sorted_array = heap_sort(array)
print("Sorted array:",
sorted array)
```

The choice of sorting algorithm can significantly impact the performance of your programs, especially when working with large arrays or requiring high efficiency. The provided Python implementations exemplify the versatility and varied approach each algorithm offers. As a crucial concept in data structures and algorithms, mastering array sorting and understanding its nuances is essential for developing optimized and effective software solutions.

3.7 Array Searching

Array searching involves the process of finding the position of a specified element within an array. This is a fundamental operation in programming and is critical for tasks such as data retrieval, validation, and analysis. Two primary techniques for searching arrays are **linear search** and **binary search**, each with its unique characteristics and efficiency ratings.

Linear Search is the most basic form of searching. It works by iterating through each element of the array until the desired element is found or the end of the array is reached. While simple and straightforward, its time complexity is O(n) where n is the number of elements in the array. Here is a Python implementation of linear search:

```
def linear_search(arr, x):
    for i in
    range(len(arr)):
        if arr[i] ==
            x: return i
    return -1 # element not found
```



When executed, the function will return the index of the first occurrence of the element x in the array arr or -1 if the element is not present.

```
>>> linear_search([4, 2, 3, 1, 5], 3)
2
>>> linear_search([4, 2, 3, 1, 5], 6)
-1
```

Binary Search is a more efficient method for searching, but it requires the array to be sorted. The binary search algorithm divides the array into halves to reduce the search interval, making the time complexity $O(\log n)$. Below is a Python implementation of binary search:

```
def binary_search(arr,
    x): low = 0
    high = len(arr) - 1

while low <= high:
    mid = (low + high) //
    2 if arr[mid] == x:
        return mid
    elif arr[mid] <
    x:
        low = mid +
    1 else:
        high = mid - 1</pre>
```

When executed, the function returns the index of the element x in the sorted array arr or -1 if the element is not found.

```
>>> binary_search([1, 2, 3, 4, 5], 3)
2
>>> binary_search([1, 2, 3, 4, 5], 6)
-1
```

Binary searching can also be implemented using recursion. Here is an alternative recursive approach for binary search:



```
def binary_search_recursive(arr, x, low,
   high): if low > high:
      return -1 # element not found
   mid = (low + high) //
   2 if arr[mid] == x:
     return mid
   elif arr[mid] <</pre>
   х:
      return binary search recursive (arr, x, mid + 1,
   high) else:
      return binary_search_recursive(arr, x, low, mid - 1)
# Example usage
arr = [1, 2, 3, 4, 5]
x = 3
result = binary search recursive(arr, x, 0, len(arr) -
1) print(result)
```

The recursive version also efficiently narrows down the range by adjusting the low and high indices in each call.

Besides these traditional searching techniques, Python's built-in functions can be leveraged for array searches. The in keyword provides a simple and readable way to check for the presence of an element, and the index() method can retrieve the position of the first occurrence. However, these are typically implemented using linear search techniques.

```
arr = [4, 2, 3, 1, 5]

# Check existence
element_exists = 3 in arr

# Get index
index_of_element = arr.index(3) if element_exists else -1
print(element_exists) # Output: True
print(index_of_element) # Output: 2
```

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For large datasets and frequent searches, more sophisticated data structures such as hash tables, binary search trees, or advanced algorithm techniques may be employed to optimize search operations. Understanding and choosing the appropriate array searching technique is crucial for efficient data handling and can significantly influence performance in computational tasks.

3.8 Dynamic Arrays

Dynamic arrays are a versatile and fundamental data structure that extend the capabilities of static arrays by allowing resizing and efficient insertion and deletion of elements. In this section, we will explore the underlying mechanisms, implementation details, and performance characteristics of dynamic arrays. Additionally, we will consider the implications of using dynamic arrays in various computational contexts.

A dynamic array, also known as a resizable array, is an array that can automatically resize itself when elements are added or removed. Contrary to static arrays, which have a fixed size determined at the time of their creation, dynamic arrays can grow or shrink as needed. This flexibility makes dynamic arrays particularly useful for situations where the size of the dataset is not known beforehand.

The core operation that distinguishes dynamic arrays from static arrays is resizing. The dynamic array maintains a logical size—representing the number of elements it currently holds—and a capacity—representing the total number of elements it can accommodate without resizing. When the logical size exceeds the capacity, the array must be resized to accommodate new elements. Typically, this resizing involves allocating a new array with larger capacity and copying the existing elements to the new array.

To illustrate the concept of a dynamic array, we can implement a basic version in Python using a list. Here is a simple example demonstrating how to build a dynamic array class:

```
class DynamicArray:
    def___init__
    (self):
        self.capacity = 1
```

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```
self.size = 0
  self.array = self.make array(self.capacity)
def____len__
   (self): return
  self.size
def___getitem__(self, k):
  if not 0 <= k < self.size:
      raise IndexError('index out of
  bounds') return self.array[k]
def append(self, item):
  if self.size == self.capacity:
      self. resize(2 *
     self.capacity)
  self.array[self.size] =
  item self.size += 1
def resize(self, new capacity):
  new array =
  self.make array(new capacity) for k in
  range(self.size):
     new_array[k] =
  self.array[k] self.array =
  new array self.capacity =
  new capacity
@staticmethod
def make array(capacity):
  return (capacity * ctypes.py_object)()
```

The above example shows a simplified implementation of a dynamic array. The constructor initializes the capacity to 1 and the size to 0, creating an array with one element space. The append method adds a new item to the array, resizing it if necessary by doubling its capacity using the _resize method. The _resize method creates a new array with twice the capacity,

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copies all elements from the old array, and then replaces the old array with the new one.



The amortized time complexity for the append operation in a dynamic array is O(1). This means that while individual resizes may be expensive—taking O(n) time for n elements—the average cost per append operation remains constant over a sequence of operations because resizing happens logarithmically with respect to the number of append operations.

Dynamic arrays also support other operations such as insertion and deletion at arbitrary positions. The following code demonstrates how to implement these additional capabilities:

```
class
   DynamicArray(DynamicArray):
   def insert(self, k, item):
      if self.size == self.capacity:
         self. resize(2 *
         self.capacity)
      for i in range(self.size, k, -1):
         self.array[i] =
         self.array[i-1]
      self.array[k] =
      item self.size += 1
   def delete(self, k):
      if not 0 <= k < self.size:</pre>
         raise IndexError('index out of
     bounds') for i in range(k, self.size -
     1):
         self.array[i] = self.array[i +
      1] self.array[self.size - 1] = None
      self.size -= 1
      if self.size > 0 and self.size == self.capacity //
         4: self. resize(self.capacity // 2)
```

The insert method inserts an element at a specified index, shifting subsequent elements to the right to make room. The delete method removes an element at a specified index, shifting subsequent elements to the left to fill the gap. After deletion, if the size of the array drops to one-fourth of its capacity, the array is resized down to half its capacity to save space.

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Dynamic arrays provide a wide range of applications by allowing efficient random access and modification. Their ability to dynamically adjust capacity



while maintaining reasonable performance guarantees makes them suitable for many scenarios in coding and algorithm design. The refinement of implementing such structures correctly has profound implications for performance optimization in numerous practical applications.

3.9 Applications of Arrays

Arrays are among the most fundamental and ubiquitous data structures in computer science. They provide a mechanism to store and manipulate a collection of data elements, all of the same type, in a contiguous block of memory. Arrays find utility in numerous applications, extending from simple data storage tasks to complex algorithmic implementations in various domains. Understanding these applications allows for leveraging arrays effectively in problem-solving and software development.

Arrays are extensively used in implementing mathematical data structures such as matrices and tensors. These structures are pivotal in fields like linear algebra, numerical analysis, and machine learning. For instance, matrices, which are two-dimensional arrays, enable operations such as matrix multiplication, determinant calculation, and matrix inversion, fundamental in solving systems of linear equations and transformations in graphics.

In computer graphics, arrays are employed to represent images, where each element in the array corresponds to a pixel's color value. For example, a grayscale image can be stored in a two-dimensional array where each element holds an intensity value. For colored images, three-dimensional arrays are used to store the red, green, and blue (RGB) components of each pixel.

```
import numpy as np

# Assume grayscale image of size 256 x 256
image = np.zeros((256, 256))

# Example of setting a pixel value at position (10, 10)
image[10, 10] = 255
```



Text processing and manipulation are other areas where arrays play a critical role. Strings, which are essentially sequences of characters, can be viewed as arrays of characters. Various operations such as searching, sorting, and pattern matching (e.g., the Knuth-Morris-Pratt algorithm) utilize arrays for efficient implementation.

```
# Example of storing and manipulating a string in an array
text = "Hello, World!"
char_array =
list(text)

# Modify the first character
char_array[0] = 'h'

new_text = ''.join(char_array)
print(new_text) # Output: "hello,
World!"
```

Dynamic arrays, such as Python lists, are pivotal in the implementation of data structures like stacks and queues. They allow for flexible and efficient addition and removal of elements. Stacks, which follow Last-In-First-Out (LIFO) order, and queues, which follow First-In-First-Out (FIFO) order, are fundamental in algorithmic processes such as depth-first search (DFS) and breadth-first search (BFS) in graph theory.

Sorting algorithms, including quicksort and mergesort, utilize arrays as the underlying data structure for their operations. The efficiency of these algorithms, driven by the array's random access capability, highlights arrays' indispensable role in sorting large datasets.

```
def quicksort(arr):
    if len(arr) <=
    1:
        return arr
    pivot = arr[len(arr) // 2]
    left = [x for x in arr if x < pivot]
    middle = [x for x in arr if x ==
    pivot] right = [x for x in arr if x >
    pivot]
```

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return quicksort(left) + middle + quicksort(right)

Example usage



```
array = [3, 6, 8, 10, 1, 2, 1]
print(quicksort(array))
```

In the domain of databases, arrays can be used to efficiently store and access records. Relational databases often utilize arrays for indexing and query optimization, improving search and retrieval operations. Arrays also support multi-key indexing and composite keys of database systems, ensuring efficient data management.

Computational simulations and scientific computations frequently leverage arrays for tasks such as finite element analysis, particle simulations, and climate modeling. These simulations require handling large datasets and performing numerous operations on these datasets, for which arrays provide an efficient and straightforward approach.

Game development is another area where arrays are crucial. Arrays are often used to create and manage game states, including the representation of game boards, handling of sprites, and storage of game world data. For example, in grid-based games like chess or tic-tac-toe, a two-dimensional array can be used to store the game state, with each element representing a cell on the board.

```
# Initial empty chess board
chess_board = [[''] * 8 for _ in range(8)]

# Placing pieces on the board
chess_board[0][0] = 'R' # Rook
chess_board[0][1] = 'N' #
Knight chess_board[0][2] = 'B'
# Bishop
```

Arrays also facilitate the implementation of hash tables, where arrays are used to store the hash table entries. The simplicity of array indexing combined with hashing functions provides efficient solutions for managing associative data, widely utilized in applications requiring constant-time complexity for insertions, deletions, and lookups.

Arrays are foundational to many computational problems spanning various fields, including scientific computing, graphics, text processing, and

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algorithm implementation. Their ability to provide efficient storage, fast access times, and ease of implementation underscores their continued relevance and utility in both academic and industrial applications.

3.10 Performance Considerations

When working with array structures, performance is a crucial aspect that deserves thorough consideration. The efficiency of array operations, memory usage, and execution time are all vital factors that can significantly impact the overall performance of an application. This section will delve into the elements that influence the performance of arrays in Python and provide practices and principles to optimize their usage.

One of the primary factors affecting array performance is the **Time Complexity** of operations performed on arrays. Time complexity, denoted using Big O notation, provides an approximation of the number of operations an algorithm performs relative to the size of the input data. For arrays, common operations include accessing elements, inserting and deleting elements, and searching for values.

Accessing Elements: For a static array, accessing an element by its index is an O(1) operation. This constant time complexity is a significant advantage of arrays, as it allows for fast retrieval of values.

```
# Accessing an element in an array
arr = [1, 2, 3, 4, 5]
element = arr[2] # O(1) operation
```

Inserting Elements: Inserting an element at the beginning or middle of an array requires shifting subsequent elements to the right, resulting in an O(n) operation. Inserting an element at the end, however, is typically an O(1) operation, assuming the array has enough allocated space.

```
# Inserting an element to an array arr.insert(2, 10) # O(n) operation arr.append(6) # O(1) operation if space is available
```



Deleting Elements: Like insertion, deleting an element from the beginning or middle of an array requires shifting of elements to the left, leading to an O(n) time complexity. Deleting the last element is an O(1) operation.

```
# Deleting an element from an array
arr.pop(2) # O(n) operation
arr.pop() # O(1) operation
```

Searching for Elements: In the worst case, searching for an element in an unsorted array is an O(n) operation since it may require scanning the entire array.

```
# Searching for an element in an array
found = 4 in arr # O(n) operation
```

The **Space Complexity** is another critical factor, representing the amount of memory required by the array. Arrays generally have O(n) space complexity, meaning the memory usage grows linearly with the number of elements. Python's built-in lists, which are dynamic arrays, occasionally need to resize when appending new elements, potentially doubling their capacity to accommodate future growth.

Despite their straightforward nature, arrays can incur significant overhead if not managed correctly. Memory allocation for arrays can become a bottleneck, especially when dealing with large data volumes or frequent resizing operations. **Dynamic Arrays**, as implemented in Python lists, handle this by allocating extra space to minimize the number of resizes, balancing between time and space efficiencies.

```
# Dynamic array resizing in Python
arr = []
for i in range(1000):
    arr.append(i) # Underlying array may resize multiple times
```

Cache Locality plays a pivotal role in performance, particularly in modern computer architectures. Arrays benefit from excellent cache locality because their elements are stored contiguously in memory. This means that when accessing an element, nearby elements are also loaded into the cache,

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facilitating faster data access. Improving cache locality involves ensuring that the elements likely to be accessed together are physically close in memory.

Optimizing **Multidimensional Arrays** involves understanding memory layout patterns. For example, a common practice is to store a two-dimensional array in a row-major order or column-major order. An operation that repeatedly accesses consecutive memory locations (i.e., iterates over rows or columns) will benefit from better cache performance.

```
# Accessing elements to leverage cache locality
matrix = [[0] * 1000 for _ in
range(1000)] for row in matrix:
   for col in row:
     pass # More efficient row-wise access
```

In computational tasks, sometimes the choice between using a simple array and a more complex data structure depends on the specific operations and their expected frequency. For instance, if frequent insertions and deletions are necessary, linked lists or other data structures might be more performant despite higher space overheads.

Lastly, **Python's Global Interpreter Lock (GIL)** can affect the performance of array operations in multi-threaded environments. The GIL allows only one thread to execute in the Python interpreter at any given time, leading to potential performance bottlenecks in CPU-bound operations. Parallelizing array operations using libraries like NumPy can circumvent this limitation, as they utilize native C extensions that release the GIL.

Understanding these aspects and carefully selecting the appropriate approaches and algorithms can significantly impact the performance of array operations in Python applications.



Chapter 4 Linked Lists

This chapter explores linked lists, starting with their basic concepts and progressing through singly, doubly, and circular linked lists. It details fundamental operations such as insertion, deletion, traversal, and

searching. The chapter also examines practical applications, performance considerations, and comparisons with arrays, providing a thorough understanding of these versatile data structures.

4.1 Introduction to Linked Lists

Linked lists are a fundamental data structure in computer science, characterized by a collection of elements called nodes. Each node contains two fields: one to store data, and another to store a reference (or a pointer) to the next node in the sequence. Unlike arrays, which use contiguous memory allocation, linked lists use dynamic memory allocation and store elements non- contiguously. This flexibility allows for efficient insertions and deletions but can introduce complexity in memory management and traversal operations.

The primary advantage of linked lists over arrays is their ability to dynamically resize, which facilitates efficient memory utilization. While arrays have a fixed size, requiring the declaration of an array with a predefined capacity, linked lists can grow and shrink in size as elements are added or removed. This behavior is particularly useful in scenarios where the number of elements is unpredictable or varies significantly during runtime.

To begin understanding linked lists, consider a simple node structure in Python. This node forms the building block of a linked list.

```
class Node:
    def___init___(self, data=None):
        self.data = data
        self.next = None
```

In this implementation, the Node class contains a constructor that

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initializes the data $\,$ field to store the value of the node and the next $\,$ field to store the



reference to the next node in the list. As a result, each node in the linked list points to the subsequent node, creating a chain-like structure.

A linked list can be visualized as follows:

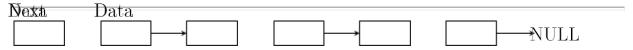


Figure 4.1: Simple visualization of a linked list with three nodes.

In the illustration above, each node consists of two parts: the **Data** part that stores the value and the **Next** part that stores the reference to the next node. The last node's **Next** reference points to NULL, signifying the end of the linked list.

The essential operations performed on linked lists include traversal, insertion, deletion, and searching. Traversal involves visiting each node in the list, starting from the head node and moving through subsequent nodes using the next references. Consider a basic traversal operation in Python:

```
class LinkedList:
    def ___init___(self):
        self.head = None

def traverse(self):
        current = self.head
    while current:
        print(current.data, end=" -> ")
        current = current.next
    print("NULL")
```

Here, the LinkedList class includes a traverse method that starts from the head node and iterates through each node using the next reference. This method prints the data stored in each node, depicting the structure of the linked list.

Insertion operations in linked lists depend on the position where the new node is to be inserted. The primary scenarios include insertion at the beginning, at

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the end, or at a specified position in the list. The following examples demonstrate these insertion operations:

```
class LinkedList:
   def____init___(self):
      self.head = None
   def insert at beginning(self, data):
      new_node = Node(data)
      new node.next = self.head
      self.head = new node
   def insert at end(self, data):
      new node = Node(data)
      if not self.head:
         self.head = new node
         return
      last = self.head
      while last.next:
         last = last.next
      last.next = new node
   def insert_at_position(self, data, position):
      new node = Node(data)
      if position == 0:
         new node.next = self.head
         self.head = new node
         return
      current = self.head
      for _ in range(position - 1):
         current = current.next
         if not current:
            raise IndexError("Position out of bounds")
      new_node.next = current.next
      current.next = new node
```



The insert_at_beginning method creates a new node and updates its next reference to point to the current head of the list. The head is then updated to the new node. The insert_at_end method traverses the list to find the last node and updates the next reference of the last node to point to the new node. The insert_at_position method inserts the new node at a specified position, adjusting the next references accordingly.

Deletion operations in linked lists can be similarly categorized based on the node's position: at the beginning, at the end, or at a specific position. The following examples illustrate these deletion methods:

```
class LinkedList:
   def____init___(self):
      self.head = None
   def delete at beginning(self):
      if not self.head:
         return
      self.head = self.head.next
   def delete at end(self):
      if not self.head:
         return
      if not self.head.next:
         self.head = None
         return
      second last = self.head while
      second last.next.next:
         second last = second last.next
      second last.next = None
   def delete at position(self, position):
      if not self.head:
         return
      if position == 0:
         self.head = self.head.next
         return
```



```
current = self.head
for _ in range(position - 1):
    current = current.next
    if not current.next:
        raise IndexError("Position out of bounds")
current.next = current.next.next
```

The delete_at_beginning method removes the head node by updating the head reference to point to the next node. The delete_at_end method traverses the list to find the second last node, then sets its next reference to NULL, thus removing the last node. The delete_at_position method removes the node at a specified position by adjusting the next references accordingly.

Searching for elements in a linked list involves traversing the list and examining each node's data to check for a match. If a match is found, the search operation returns the position of the node (or simply confirms the presence of the data), otherwise, it concludes that the element is not present. Consider the following example:

```
class LinkedList:
    def __init__(self):
        self.head = None

    def search(self, key):
        current = self.head
        position = 0
        while current:
        if current.data == key:
            return position
        current = current.next
        position += 1
        return -1 # Element not found
```

The search method iterates through the list, comparing each node's data with the search key. If a match is found, it returns the position of the node; otherwise, it returns -1 to indicate that the element is not found in the list.



The linked list data structure showcases its strengths in scenarios requiring dynamic memory management, frequent insertions and deletions, and non-contiguous storage of elements. Understanding the basic concepts and operations of linked lists forms the foundation for advanced topics like doubly and circular linked lists, as well as practical applications ranging from memory management to implementation of abstract data types like stacks, queues, and more.

4.2 Singly Linked Lists

A singly linked list is a fundamental data structure in computer science, consisting of a sequence of elements where each element points to the next element in the sequence. Each element in the list is called a node. A node comprises two parts: the data it holds and a reference (or pointer) to the next node in the sequence. The list terminates in a node that points to null, indicating the end of the list.

To implement a singly linked list in Python, we first define a class for the nodes. Each node contains the data and a pointer to the next node. Here is an example implementation:

```
class Node:
    def__init__(self, data=None):
        self.data = data
        self.next = None
```

In this Node class, the __init___method initializes the data to the provided value and the next pointer to None.

Next, we define the linked list class, which manages the nodes. The linked list class includes methods to insert, delete, and traverse the list:

```
class SinglyLinkedList:
    def___init___(self):
        self.head = None
```

In this SinglyLinkedList class, the __init__method initializes the head of the list to None, indicating that the list is initially empty.

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Inserting a new node at the beginning of the list is a common operation. Here is how you can implement it:

```
def insert_at_beginning(self, data):
    new_node = Node(data)
    new_node.next = self.head
    self.head = new node
```

In this method, a new node is created with the specified data. The new node's next pointer is set to the current head of the list, and then the head is updated to the new node.

To insert a new node at the end of the list, we need to traverse the list to find the last node and then append the new node:

```
def insert_at_end(self, data):
    new_node = Node(data)
    if not self.head:
        self.head = new_node
        return
    last = self.head
    while last.next:
        last = last.next
    last.next = new_node
```

In this method, if the list is empty (i.e., self.head is None), the new node becomes the head. Otherwise, the method traverses the list to find the last node and sets its next pointer to the new node.

Deleting a node from the list requires finding the node and adjusting the pointers appropriately. Here's how to delete a node by value:

```
def delete_node(self, key):
    temp = self.head

if temp is not None: if
    temp.data == key:
        self.head = temp.next
    temp = None
```

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while temp is not None:
 if temp.data == key:
 break
 prev = temp
 temp = temp.next

if temp == None:
 return

prev.next = temp.next

temp = None

return

In this deletion method, the list is traversed to find the node with the specified key. If the node is found, the previous node's next pointer is updated to skip the node being deleted.

Traversal of the list means visiting each node and performing an operation. For example, printing all the list elements can be done as follows:

```
def print_list(self):
    temp = self.head
    while temp:
        print(temp.data, end=' ')
        temp = temp.next
    print()
```

In this print_list method, the list is traversed from the head to the end, printing each node's data. The end=' ' parameter in the print function helps to print all node values in a single line separated by space.

Searching for an element in a singly linked list involves traversing the nodes and checking the data of each node against the target value:

```
def search(self, key):
    current = self.head
    while current:
```

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```
if current.data == key:
    return True
    current = current.next
return False
```

This search method checks each node's data to see if it matches the key. If it finds the key, it returns True; if it reaches the end of the list without finding the key, it returns False.

Hence, singly linked lists provide a flexible and dynamic way to manage collections of data, with efficient insertions and deletions. Understanding their structure and operations is critical for leveraging their advantages in varied computational problems.

4.3 Doubly Linked Lists

A doubly linked list is a type of linked list in which each node contains a reference to both the next node and the previous node. This bidirectional linkage allows for more flexible manipulation of the list, including traversal in both forward and backward directions. The structure of a node in a doubly linked list is typically defined with three components: the data, a reference to the next node, and a reference to the previous node.

Node Structure: In Python, a node for a doubly linked list can be represented using a class. Below is a simple implementation:

```
class Node:
    def__init__(self, data):
        self.data = data
        self.next = None
        self.prev = None
```

Doubly Linked List Structure: The doubly linked list itself can be managed using another class, which maintains references to the head and tail of the list. Here is an implementation of a basic doubly linked list:

```
class DoublyLinkedList:
    def___init___(self):
```

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```
self.head = None
self.tail = None

def append(self, data):
    new_node = Node(data)
    if self.head is None:
        self.head = new_node
        self.tail = new_node
    else:
        self.tail.next = new_node
    new_node.prev = self.tail
        self.tail = new_node
```

In the append method, we check if the list is empty. If it is, the new node becomes both the head and the tail of the list. If the list is not empty, the new node is added at the end, and the pointers are updated to maintain the doubly linked nature.

Traversal: Traversing a doubly linked list can be done in both forward and backward directions. Forward traversal starts from the head node and follows the next pointers, while backward traversal starts from the tail node and follows the prev pointers.

Forward Traversal:

```
def traverse_forward(self):
    current = self.head while
    current:
        print(current.data)
        current = current.next
```

Backward Traversal:

```
def traverse_backward(self):
    current = self.tail
    while current:
        print(current.data)
        current = current.prev
```

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Insertion: Insertion in a doubly linked list can occur at several positions, such as at the beginning, at the end, or at a specific position.

Insertion at the Beginning:

```
def insert_at_beginning(self, data):
    new_node = Node(data)
    if self.head is None:
        self.head = new_node
        self.tail = new_node
    else:
        new_node.next = self.head
        self.head.prev = new_node
        self.head = new_node
```

Insertion at a Specific Position:

```
def insert_at_position(self, data, position):
   if position <= 0:
      return
   new node = Node(data)
   current = self.head
   for in range (position - 1):
      if current is None:
         return
      current = current.next
   if current is None:
      return
   new node.next = current.next
   new node.prev = current
   if current.next:
      current.next.prev = new node
   current.next = new node
```

Deletion: Deletion operations in a doubly linked list can also be performed at the beginning, at the end, or at a specific position.

Deletion at the Beginning:



```
def delete_from_beginning(self):
    if self.head is None:
        return
    if self.head == self.tail:
        self.head = None
        self.tail = None
    else:
        self.head = self.head.next
        self.head.prev = None
```

Deletion at a Specific Position:

```
def delete at position(self, position): if
   position <= 0 or self.head is None:</pre>
      return
   current = self.head
   for in range (position - 1):
      if current is None:
         return
      current = current.next
   if current is None or current.next is None:
      return
   if current.next == self.tail:
      self.tail = current
      self.tail.next = None
   else:
      current.next = current.next.next
      if current.next:
         current.next.prev = current
```

Practical Considerations: Doubly linked lists provide greater flexibility in terms of traversal and can be more efficient for certain types of operations, such as bidirectional iteration. However, this flexibility comes at the cost of increased memory usage due to the additional pointers maintained in each node.

Understanding the trade-offs between different types of linked lists, including singly and doubly linked lists, is crucial for choosing the appropriate data

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structure for your specific application requirements.

4.4 Circular Linked Lists

A circular linked list is a subtype of linked list where all the nodes are connected to form a circle. Unlike a singly or doubly linked list, where the last node points to NULL, in a circular linked list, the last node contains a link to the first node. This creates a circular structure, ideal for scenarios where the data must be processed in a cyclic manner.

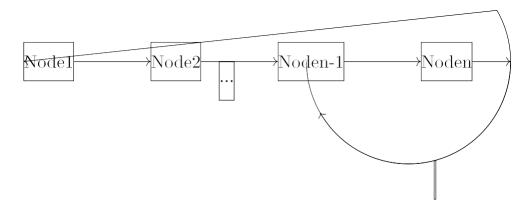
Definition: A circular linked list is a variation of the linear linked list where the last element points to the first element, thus forming a loop.

Node Structure: Each node in a circular linked list contains two fields:

•data: Holds the value or information of the node.

•next: Holds the reference to the next node in the list.

A diagrammatic representation of a circular linked list is as follows:



Advantages:

- •Efficient memory use by avoiding end markers.
- •Useful for implementing queues or buffers where circular processing is necessary.
- Facilitates the traversal from any node through every other node.

Disadvantages:



- •Complexity in implementation due to the circular nature.
- •Potential risk of infinite loops if the list is unsafely traversed.

Basic Operations:

•Insertion: Add a new node either at the start, in the middle, or at the end of the list.

•Deletion: Remove a specified node from the list.

•Traversal: Navigate through all nodes starting from any node.

•Searching: Locate a specific element within the list.

Implementation:

Insertion at the Beginning

To insert a new node at the start of a circular linked list, follow these steps:

- 1. Allocate memory for the new node.
- 2. Set the new node's next to point to the current head node.
- 3. Traverse to the last node and set its next to the new node.
- 4. Update the head to the new node.

```
class Node:
    def___init__(self, data):
        self.data = data
        self.next = None

class CircularLinkedList:
    def___init__(self):
        self.head = None

def insert_at_beginning(self, data):
        new_node = Node(data)
        temp = self.head

    new_node.next = self.head

if self.head is not None:
```



```
while temp.next != self.head:
    temp = temp.next
temp.next = new_node
else:
    new_node.next = new_node # For the first node
self.head = new_node
```

Insertion at the End

To insert a new node at the end of a circular linked list:

- 1. Allocate memory for the new node and set the new node's next to the head node.
- 2. If the list is empty, set the head to reference the new node, and set the new node's next to itself.
- 3. Otherwise, traverse to the last node and set its next to reference the new node.

```
def insert_at_end(self, data):
    new_node = Node(data)
    temp = self.head

new_node.next = self.head

if self.head is not None:
    while temp.next != self.head:
        temp = temp.next
        temp.next = new_node
else:
    self.head = new_node
    new_node.next = new_node # For the first node
```

Traversal

To traverse a circular linked list starting from the head:

1. Initialize a temporary pointer to reference the head.

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2. Loop through each node until the starting node is reached again.

```
def traverse(self):
   nodes = []
   temp = self.head
   if self.head is not None:
      while True:
        nodes.append(temp.data)
        temp = temp.next
        if temp == self.head:
            break
   return nodes
```

Deletion

To delete a node from a circular linked list:

- 1. Traverse to the node preceding the node to be deleted.
- 2. Update the next link of the preceding node to skip the node to be deleted.
- 3. If the node to be deleted is the head, update the head reference.
- 4. Free the memory occupied by the node to be deleted.

```
def delete_node(self, key):
    if self.head is None:
        return

temp = self.head
prev = None

while True:
    if temp.data == key: if
        prev is not None:
            prev.next = temp.next
        else:
        if temp.next == self.head:
            self.head = None
        else:
```

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```
prev = self.head
    while prev.next != temp:
        prev = prev.next
        prev.next = self.head = temp.next
    break
else:
    prev = temp
    temp = temp.next
    if temp == self.head:
        break
```

Use Cases: Circular linked lists are particularly useful in applications that require a cyclic process:

- •Implementing circular queues.
- •Managing the CPU scheduling in operating
- •systems. Buffer management in streaming applications.

A detailed understanding of these operations and their correct implementation is critical for leveraging the full potential of circular linked lists.

4.5 Basic Operations on Linked Lists

Linked lists are fundamental data structures that allow dynamic memory allocation and efficient insertions and deletions. Understanding and implementing the basic operations on linked lists is crucial for developing more complex data structures and algorithms. This section covers the core operations: insertion, deletion, traversal, and searching. Each operation will be discussed in the context of singly linked lists, with pertinent code examples in Python to illustrate their implementation.

Insertion: Insertion in a linked list can be performed in multiple ways: at the beginning, at the end, or at a specific position. Efficient handling of pointers is required to maintain the structure's integrity.

```
class Node:
   def___init___(self, data):
```

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```
self.data = data
    self.next = None
 class LinkedList:
    def___init__(self):
       self.head = None
    def insert at beginning(self, new data):
       new node = Node(new data)
       new node.next = self.head
       self.head = new node
    def print list(self):
       temp = self.head
       while(temp):
          print(temp.data, end=" -> ")
          temp = temp.next
       print("None")
 # Example usage:
 llist = LinkedList()
 llist.insert at beginning(10)
 llist.insert_at_beginning(20)
llist.print list()
Output:
20 -> 10 -> None
def insert_at_end(self, new_data):
    new_node = Node(new_data)
    if self.head is None:
       self.head = new_node
       return
    last = self.head
    while(last.next):
       last = last.next
    last.next = new node
 # Example usage:
```

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```
llist.insert_at_end(30)
 llist.print_list()
Output:
20 -> 10 -> 30 -> None
 def insert at position(self, position, new data):
    if position < 0:
       raise ValueError("Position cannot be negative")
    new_node = Node(new_data)
    if position == 0:
       new node.next = self.head
       self.head = new node
       return
    temp = self.head
    for _ in range(position - 1):
       if temp is None:
           raise IndexError("Position out of bounds")
       temp = temp.next
    new node.next = temp.next
    temp.next = new node
 # Example usage:
 llist.insert at position(1, 40)
 llist.print_list()
Output:
20 \rightarrow 40 \rightarrow 10 \rightarrow 30 \rightarrow None
```

Deletion: Deletion involves removing a node from the linked list and adjusting the pointers appropriately. Similar to insertion, deletion can occur at the beginning, at the end, or at a specific position.

```
def delete_at_beginning(self):
    if self.head is None:
        return
    self.head = self.head.next
# Example usage:
```

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```
llist.delete_at_beginning()
 llist.print_list()
Output:
40 -> 10 -> 30 -> None
 def delete at end(self):
    if self.head is None:
       return
    if self.head.next is None:
       self.head = None
       return
    temp = self.head
    while(temp.next.next):
       temp = temp.next
    temp.next = None
 # Example usage:
 llist.delete_at_end()
 llist.print list()
Output:
40 -> 10 -> None
 def delete at position(self, position):
    if self.head is None:
       raise IndexError("Position out of bounds")
    if position < 0:
       raise ValueError("Position cannot be negative")
    if position == 0:
       self.head = self.head.next
       return
    temp = self.head
    for _ in range(position - 1):
       if temp.next is None:
          raise IndexError("Position out of bounds")
       temp = temp.next
    temp.next = temp.next.next
```



```
# Example usage:
llist.delete_at_position(1)
llist.print_list()

Output:
40 -> None
```

Traversal: Traversal involves visiting each node in the linked list from the head to the last node, performing actions such as printing the node's data.

```
def traverse(self):
    temp = self.head
    while temp:
        print(temp.data, end=" -> ")
        temp = temp.next
    print("None")

# Example usage:
llist.traverse()

Output:
40 -> None
```

Searching: Searching for an element in the linked list involves traversing through the list and comparing each node's data with the target value.

```
def search(self, key):
    temp = self.head
    while temp:
        if temp.data == key:
            return True
        temp = temp.next
    return False

# Example usage:
found = llist.search(40)
print("Element found?" , found)

Output:
```

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Element found? True

Mastering the basic operations on linked lists is essential for constructing more advanced data structures. The ability to insert, delete, traverse, and search in a linked list provides a solid foundation for further exploration and efficient manipulation of data.

4.6 Insertion in Linked Lists

Insertion in linked lists is a fundamental operation that allows the addition of elements at any position within the list: beginning, end, or in-between two nodes. Understanding how to efficiently add elements to a linked list is crucial for utilizing the data structure effectively.

1. Inserting at the Beginning

Inserting a node at the beginning of a linked list is a straightforward process that involves updating the head pointer to point to the new node. The new node's next pointer should then point to the current head node. Here is a Python implementation for a singly linked list:

```
class Node:
    def___init___(self, data):
        self.data = data
        self.next = None

class LinkedList:
    def___init___(self):
        self.head = None

def insert_at_beginning(self, new_data):
        new_node = Node(new_data)
        new_node.next = self.head
        self.head = new_node
```

To insert a node at the beginning of a doubly linked list, update both the previous pointer of the current head and the next pointer of the new node:

class Node:

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```
def___init___(self, data):
    self.data = data self.next = None self.prev = None

class DoublyLinkedList:
    def___init___(self):
        self.head = None

def insert_at_beginning(self, new_data):
        new_node = Node(new_data)
        new_node.next = self.head
        if self.head is not None:
            self.head.prev = new_node
        self.head = new_node
```

2. Inserting at the End

Inserting a node at the end of a linked list requires traversal to the last node and updating its next pointer to the new node. Here is the implementation for a singly linked list:

```
class LinkedList:
    # Previous code omitted for brevity

def insert_at_end(self, new_data):
    new_node = Node(new_data)
    if self.head is None:
        self.head = new_node
        return
    last = self.head
    while last.next:
        last = last.next
    last.next = new_node
```

For a doubly linked list, update the previous pointer of the new node and the next pointer of the last node:



```
class DoublyLinkedList:
    # Previous code omitted for brevity

def insert_at_end(self, new_data):
    new_node = Node(new_data)
    if self.head is None:
        self.head = new_node
        return
    last = self.head
    while last.next:
        last = last.next
    last.next = new_node
    new node.prev = last
```

3. Inserting After a Given Node

Inserting a node after a specific node involves adjusting the next pointers so that the new node is linked into the list. Here is the code for a singly linked list:

```
class LinkedList:
    # Previous code omitted for brevity

def insert_after_node(self, prev_node, new_data):
    if not prev_node:
        print("The given previous node must be in the linked list.")
        return
    new_node = Node(new_data)
    new_node.next = prev_node.next
    prev_node.next = new_node
```

For a doubly linked list, both the next and previous pointers of adjacent nodes need adjustment:

```
class DoublyLinkedList:
    # Previous code omitted for brevity

def insert_after_node(self, prev_node, new_data):
```

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```
if not prev_node:
    print("The given previous node must be in the linked list.")
    return

new_node = Node(new_data)
new_node.next = prev_node.next
prev_node.next = new_node
new_node.prev = prev_node
if new_node.next:
    new node.next.prev = new node
```

4. Inserting Before a Given Node

In this case, the traversal is necessary to find the node preceding the given node, then adjusting the next pointers. The implementation for a singly linked list is as follows:

```
class LinkedList:
   # Previous code omitted for brevity
   def insert_before_node(self, next_node, new_data):
      if not self.head or not next_node:
         print("The given next node must be in the linked list.")
         return
      if self.head == next node:
         return self.insert at beginning(new data)
      new node = Node(new data)
      current = self.head
      while current.next and current.next != next node:
         current = current.next
      if not current.next:
         print("The given next node is not in the linked list.")
         return
      new node.next = current.next
      current.next = new node
```

Inserting before a node in a doubly linked list involves simpler logic as each node includes a reference to its predecessor:



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```
class DoublyLinkedList:
    # Previous code omitted for brevity

def insert_before_node(self, next_node, new_data):
    if not self.head or not next_node:
        print("The given next node must be in the linked list.")
        return

if self.head == next_node:
        return self.insert_at_beginning(new_data)

new_node = Node(new_data)

new_node.next = next_node

new_node.prev = next_node.prev

if next_node.prev:
    next_node.prev.next = new_node

next_node.prev = new_node
```

Insertion operations across singly and doubly linked lists require careful pointer management to maintain the integrity of the list. Accurate traversal and pointer adjustments are fundamental to accomplishing these tasks efficiently.

4.7 Deletion in Linked Lists

Deletion in linked lists involves removing a node from the data structure while ensuring the structural integrity and continuity of the list. This operation can be categorized into three main types: deleting from the beginning, deleting from the end, and deleting from a specific position. Each of these categories will be explained below with explicit handling of singly, doubly, and circular linked lists.

```
**Singly Linked Lists**
```

In a singly linked list, each node contains a data value and a reference to the next node in the sequence. When performing deletions, it is important to update these references appropriately to maintain the list's integrity.

* **Deleting from the Beginning:**



To delete the head node, the head reference needs to be updated to point to the next node.

```
class Node:
    def___init___(self, data):
        self.data = data
        self.next = None

class SinglyLinkedList:
    def___init___(self):
        self.head = None

def delete_from_beginning(self):
    if self.head is not None:
        self.head = self.head.next
```

* **Deleting from the End:**

When deleting the last node, it is necessary to traverse the list to find the second last node and set its next reference to 'None'.

```
def delete_from_end(self):
    if self.head is None:
        return None

if self.head.next is None:
        self.head = None
        return None

second_last = self.head
while(second_last.next.next):
        second_last = second_last.next
second_last.next = None
```

* **Deleting from a Specific Position:**

Deleting a node from a specific position involves traversing the list to the node just before the target and updating its next reference.

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```
def delete_at_position(self, position):
   if self.head is None:
      return None
   temp = self.head
   if position == 0:
      self.head = temp.next
      return None
   for i in range (position - 1):
      temp = temp.next
      if temp is None:
         break
   if temp is None or temp.next is None:
      return None
   next = temp.next.next
   temp.next = None
   temp.next = next
```

Doubly Linked Lists

In doubly linked lists, each node contains a reference to both the next and the previous node. This bidirectional reference requires additional steps when handling deletions.

* **Deleting from the Beginning:**

The head reference must be updated, and if the list is not empty after deletion, the new head's previous reference must be set to 'None'.

```
class DNode:
    def__init__(self, data):
        self.data = data
        self.next = None
        self.prev = None
```



```
class DoublyLinkedList:
    def __init__(self):
        self.head = None

def delete_from_beginning(self):
    if self.head is not None:
        self.head = self.head.next
    if self.head is not None:
        self.head.prev = None
```

* **Deleting from the End:**

For deletion at the end, traverse to the last node, update the second last node's next reference, and set the previous reference of the removed node to 'None'.

```
def delete_from_end(self):
    if self.head is None:
        return None

if self.head.next is None:
        self.head = None
        return None

last = self.head
while(last.next is not None):
        last = last.next

last.prev.next = None
last.prev = None
```

* **Deleting from a Specific Position:**

Identify the node at the specified position, adjust the previous and next references of neighboring nodes accordingly, and then remove the target node.

```
def delete_at_position(self, position): if
   self.head is None or position <= 0:</pre>
```

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```
current = self.head
for i in range(position - 1):
    if current is None:
        return None
    current = current.next

if current is None or current.next is None:
    return None

if current.next.next is not None:
    current.next.next.prev = current

current.next = current.next.next
```

Circular Linked Lists

return None

Circular linked lists differ as the last node points back to the head node, creating a circular structure. This characteristic alters how certain deletions are implemented.

* **Deleting from the Beginning:**

Adjust the head reference to the next node, ensure the last node points to the new head to maintain the circle.

```
class CNode:
    def___init___(self, data):
        self.data = data
        self.next = None

class CircularLinkedList:
    def___init___(self):
        self.head = None

    def delete_from_beginning(self):
        if self.head is None:
        return None
```

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```
if self.head.next == self.head:
    self.head = None
    return None

last = self.head
while(last.next != self.head):
    last = last.next

self.head = self.head.next
last.next = self.head
```

* **Deleting from the End:**

To remove the last node, traverse the list to find the second last node and set its next reference to the head node.

```
def delete_from_end(self):
    if self.head is None:
        return None

if self.head.next == self.head:
        self.head = None
        return None

last = self.head
while(last.next.next != self.head):
        last = last.next

last.next = self.head
```

* **Deleting from a Specific Position:**

Navigate to the node at the desired position, then re-link the neighboring nodes to exclude the target node.

```
def delete_at_position(self, position):
   if self.head is None or position < 0:
     return None</pre>
```

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```
if position == 0:
    self.delete_from_beginning()
    return None

current = self.head
for i in range(position - 1):
    current = current.next
    if current.next == self.head:
        return None

current.next = current.next.next
current.next.prev = current
```

Understanding deletion in linked lists is crucial for efficient manipulation and management of these data structures. The algorithms presented here ensure accurate and reliable deletions across various types of linked lists, preserving their respective properties and maintaining data integrity.

4.8 Traversal in Linked Lists

Traversal in linked lists is a fundamental operation that allows visiting each node in the list in a sequential manner. This operation is crucial for performing various tasks such as searching for an element, printing the list elements, or applying a given operation to each element in the list. In this section, we will examine the traversal process for singly linked lists, doubly linked lists, and circular linked lists, elucidating the traversal mechanism, algorithm, and implementation for each type.

For a singly linked list, traversal begins at the head of the list and proceeds to the end by following the links between nodes. Below is a Python implementation of the traversal algorithm for a singly linked list.

```
class Node:
    def__init__(self, data):
        self.data = data
        self.next = None
```



```
class SinglyLinkedList:
    def ___init___(self):
        self.head = None

    def traverse(self):
        current = self.head
        while current:
            print(current.data)
            current = current.next
```

The traversal method starts with the head node and iterates through the list using a loop. In each iteration, it prints the data of the current node and then moves to the next node by updating the current pointer. When the current pointer becomes None, the end of the list is reached, and the loop terminates.

Traversing a doubly linked list requires handling both forward and backward pointers. This traversal can be implemented to move in either direction. Below is an implementation for traversing a doubly linked list in both forward and backward directions.

```
class Node:
     def___init___(self, data):
         self.data = data
         self.next = None
        self.prev = None
  class DoublyLinkedList:
     def____init___(self):
        self.head = None
     def traverse forward(self):
         current = self.head
        while current:
           print(current.data)
            current = current.next
     def traverse backward(self):
        current = self.head
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```



```
if current is None:
    return
while current.next:
    current = current.next
while current:
    print(current.data)
    current = current.prev
```

Traversing in the forward direction is similar to the singly linked list, but each node also includes a prev pointer. The backward traversal starts by reaching the last node and then iterating backward using the prev pointers.

For circular linked lists, the traversal can continue indefinitely unless explicitly stopped. Therefore, care must be taken to avoid infinite loops. Here is an implementation for traversing a circular singly linked list.

```
class Node:
   def___init___(self, data):
      self.data = data
      self.next = None
class CircularLinkedList:
   def____init___(self):
      self.head = None
   def traverse(self):
      if not self.head:
         return
      current = self.head
      while True:
         print(current.data)
         current = current.next
         if current == self.head:
            break
```

In a circular linked list, the traverse method starts at the head node and continues to print each node's data. The loop condition checks whether the

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current node has cycled back to the head node to terminate the traversal, thus avoiding an infinite loop.

The concept of traversal is essential across these different types of linked lists whether the goal is to print node values, search for a specific value, or apply an operation on the node's data. The time complexity of the traversal operation in all types of linked lists is $\mathcal{O}(n)$, where n is the number of nodes in the list, since each node is visited exactly once.

Understanding linked list traversal prepares us for more complex operations like insertion, deletion, and searching, which often involve traversal as a preliminary step. It ensures that each node is visited methodically, facilitating accurate and efficient data manipulation.

4.9 Searching in Linked Lists

Searching in linked lists is a fundamental operation that enables retrieval of elements based on their values. This capability is crucial for many applications requiring data lookup and manipulation. In this section, we shall delve into the methodologies applied for searching within different types of linked lists: singly, doubly, and circular. We will illustrate each technique with corresponding Python code to elucidate the practical implementation.

To search for an element in a linked list, the algorithm typically traverses the list until it finds the target or reaches the end. This linear search method is common across all linked list types due to their sequential access nature.

Consider a singly linked list, wherein each node contains data and a reference to the next node.

The Python class structure for a singly linked list node might be defined as follows:

```
class Node:
    def___init__(self, data):
        self.data = data
        self.next = None
```

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Likewise, the linked list class initializes an empty list:

```
class SinglyLinkedList:
    def___init___(self):
        self.head = None
```

The linear search function in a singly linked list is implemented by iterating through each node and comparing the node's data with the search key. If a match is found, the position or node reference is returned; otherwise, the traversal continues until the end of the list is reached.

```
def search(self, key):
    current = self.head
    while current is not None:
        if current.data == key:
            return current
        current = current.next
    return None
```

For a doubly linked list, the concept remains the same, but each node contains references to both the next and previous nodes. The node structure for a doubly linked list extends the principle:

```
class Node:
    def___init___(self, data):
        self.data = data
        self.next = None
        self.prev = None
```

The doubly linked list class can be initialized similarly:

```
class DoublyLinkedList:
    def___init___(self):
        self.head = None
```

The search operation in a doubly linked list iterates through the nodes similarly to a singly linked list:

```
def search(self, key):
    current = self.head
```

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```
while current is not None:
   if current.data == key:
       return current
   current = current.next
return None
```

Next, examining the search method in a circular linked list, where the last node points back to the first node, creates a loop. This variant requires careful traversal to avoid infinite loops. The node structure and initial setup are consistent with singly linked lists, with an additional check in the search method to break the cycle.

```
class Node:
   def___init___(self, data):
      self.data = data
      self.next = None
class CircularLinkedList:
   def___init__(self):
      self.head = None
def search(self, key):
   if self.head is None:
      return None
   current = self.head
   while True:
      if current.data == key:
         return current
      current = current.next
      if current == self.head:
         break
   return None
```

The provided implementations are straightforward but important for handling these operations reliably. The runtime complexity of the search operation in all types of linked lists is O(n) because it potentially examines each node once.

This linear complexity is due to the sequential access nature of linked lists, which, unlike arrays, do not support direct access to elements.

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Given their structural differences, the process of searching in a doubly linked list doesn't decrease in complexity but may offer advantages in bidirectional traversal, especially in scenarios where searching backward might be required. Although circular linked lists introduce additional considerations, the fundamental linear search method applies, ensuring comprehensiveness across list variants.

These implementations provide a methodical approach to element search within linked lists, laying the groundwork for more complex operations and optimizations within this versatile data structure.

4.10 Applications of Linked Lists

Linked lists provide versatile and powerful structures adaptable to a myriad of applications. Beyond their standalone functionality, they serve as foundational constructs in more complex data structures and algorithms, facilitating efficient management and manipulation of data.

Dynamic Memory Allocation:

In dynamic memory allocation, linked lists are pivotal. Memory allocation in systems often requires efficient handling of free and used memory blocks. A free list, a type of singly linked list, keeps track of all the available memory blocks. When an allocation request is made, the allocator traverses this list to find a suitable block, splits it if necessary, and adjusts the list accordingly.

Upon deallocation, the memory block is reinserted into the free list. This technique minimizes fragmentation and optimizes memory usage without requiring contiguous memory blocks.

Implementing Stacks and Queues:

Stacks and queues can be implemented efficiently using linked lists.

Stacks: A stack can be implemented using a singly linked list where all insertions and deletions occur at the head of the list, ensuring efficient $\mathcal{O}(1)$ operations for both push and pop.



```
class Node:
   def___init___(self, data):
      self.data = data
      self.next = None
class Stack:
   def___init___(self):
      self.head = None
   def push(self, data):
      new node = Node(data)
      new node.next = self.head
      self.head = new node
   def pop(self):
      if self.head is None:
         return None
      data = self.head.data
      self.head = self.head.next
      return data
```

Queues: A queue, in contrast, operates through a singly linked list where insertions (enqueue) occur at the tail, and deletions (dequeue) occur at the head. This ensures $\mathcal{O}(1)$ operations for both enqueue and dequeue.

```
class Node:
    def___init___(self, data):
        self.data = data
        self.next = None

class Queue:
    def___init___(self):
        self.head = None
        self.tail = None

    def enqueue(self, data):
        new_node = Node(data)
        if self.tail:
```

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```
self.tail.next = new_node
self.tail = new_node
if self.head is None:
    self.head = self.tail

def dequeue(self):
    if self.head is None:
        return None
    data = self.head.data
    self.head = self.head.next
    if self.head is None:
        self.head is None:
        self.head is None:
        return data
```

Graph Representations:

Linked lists, specifically adjacency lists, are crucial for representing graphs. An adjacency list for each vertex is a linked list that stores all the vertices adjacent to the given vertex. This representation is memory efficient, particularly for sparse graphs, where edges are significantly fewer than the total possible edges.

```
class AdjNode:
    def ___init___(self, data):
        self.vertex = data
        self.next = None

class Graph:
    def ___init___(self, vertices):
        self.V = vertices self.graph
        = [None] * self.V

    def add_edge(self, src, dest):
        node = AdjNode(dest)
        node.next = self.graph[src]
        self.graph[src] = node

    node = AdjNode(src)
```



```
node.next = self.graph[dest]
self.graph[dest] = node
```

Polynomial Arithmetic:

In polynomial arithmetic, linked lists are used to store coefficients and exponents. Each node typically represents a term of the polynomial, where the coefficient and exponent are encapsulated in the node's structure. Operations like addition and multiplication of polynomials become straightforward by traversing and manipulating these lists.

```
class PolyNode:
   def___init__(self, coeff, exp):
      self.coeff = coeff
      self.exp = exp
      self.next = None
class Polynomial:
   def___init__(self):
      self.head = None
   def add term(self, coeff, exp):
      new node = PolyNode(coeff, exp)
      if self.head is None:
         self.head = new node
         return
      current = self.head
      while current.next:
         current = current.next
      current.next = new node
```

Undo Functionality in Applications:

Many applications, such as text editors, implement an undo feature using linked lists. Each change is stored in a node, forming a list that represents the sequence of actions. Reversing the change involves traversing this list and rolling back the actions.

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Hash Tables:

In hash tables, linked lists manage collisions through chaining. Each bucket of the hash table is a linked list storing all elements that hash to the same index. This method ensures that the hash table can dynamically handle numerous collisions efficiently.

```
class HashNode:
   def___init__(self, key, value):
      self.key = key
      self.value = value
      self.next = None
class HashTable:
   def____init___(self):
      self.size = 10
      self.table = [None] * self.size
   def hash function(self, key):
      return hash(key) % self.size
   def insert(self, key, value): hash index
      = self.hash function(key) new node =
      HashNode(key, value)
      if not self.table[hash index]:
         self.table[hash index] = new node
      else:
         current = self.table[hash index]
         while current.next and current.key != key:
            current = current.next
         if current.key == key:
            current.value = value
         else:
            current.next = new node
```

These examples delineate the essential roles linked lists play in various computational problems and system designs, demonstrating their adaptability and integral presence in advanced data structures and algorithms.

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4.11 Comparison of Linked Lists and Arrays

The comparison of linked lists and arrays is essential for understanding the appropriate contexts in which to employ each data structure. This section will delve into various aspects such as memory allocation, access time, insertion and deletion operations, and overall efficiency.

Memory Allocation: Arrays and linked lists utilize memory in fundamentally different ways. Arrays leverage contiguous memory blocks to store elements, which facilitates rapid access but can lead to problems such as memory fragmentation and inefficiency when dealing with dynamic datasets. When an array is defined, a single block of memory of a fixed size is allocated. If the size of the array is underestimated, there might be a need to resize, which generally involves creating a new array and copying the elements, a computationally expensive process.

Linked lists, on the other hand, utilize non-contiguous memory allocation. Each element, or node, in a linked list is dynamically allocated and points to the next element through a reference (or pointer). This allows for efficient use of memory when the number of elements changes dynamically. No resizing is necessary, and memory allocation is managed at the node level.

•Arrays: Contiguous memory allocation.

•Linked Lists: Non-contiguous memory allocation.

Access Time: The manner in which elements are accessed differs significantly between arrays and linked lists. Arrays offer constant time complexity, O(1), for accessing elements via their index. Due to the contiguous memory allocation, the location of any element can be directly computed knowing the starting address and the index.

Conversely, linked lists do not offer direct element access, leading to a linear time complexity, O(n), for accessing elements. Accessing an element in a linked list requires traversal from the head of the list to the desired node, which can be inefficient, especially in long lists.

•Arrays: O(1) access time.

•Linked Lists: O(n) access time.



Insertion and Deletion Operations: Operations for inserting and deleting elements vary markedly in arrays and linked lists.

In an array, insertion and deletion can involve shifting elements to maintain order, leading to O(n) time complexity. For instance, inserting an element at the beginning or removing an element from the middle necessitates shifting subsequent elements to manage the free space.

```
# Example of inserting an element in an array
def insert(arr, index, value):
   if index >= len(arr):
      return arr + [value]
   else:
      return arr[:index] + [value] + arr[index:]

arr = [1, 2, 3]
arr = insert(arr, 1, 4) # [1, 4, 2, 3]
```

Linked lists provide more efficient insertions and deletions, especially when positions are known. Both operations can be done in O(1) time if adjustments are made directly to the node references. This flexibility makes linked lists ideal for scenarios where the data structure undergoes frequent modifications.

```
class Node:
    def___init___(self, data):
        self.data = data
        self.next = None

# Function to insert a new node at the beginning
def insert(head, data):
    new_node = Node(data)
    new_node.next = head
    head = new_node
    return head

# Initial Linked List: 1 -> 2 -> 3
head = Node(1)
second = Node(2)
```

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```
third = Node(3)
head.next = second
second.next = third

# Inserting new element
head = insert(head, 4) # 4 -> 1 -> 2 -> 3
```

•Arrays: O(n) insertion/deletion due to shifting.

•Linked Lists: O(1) insertion/deletion with direct reference adjustments.

Dynamic Sizing: Arrays have a fixed size, necessitating manual resizing if the dataset exceeds predefined bounds. This can lead to performance overheads due to frequent allocations and data copying.

Linked lists natively support dynamic sizing, allocating nodes as needed without the need for predefined bounds. This feature makes linked lists suitable for applications with unpredictable or highly variable data sizes.

•Arrays: Fixed size, requiring resizing.

•Linked Lists: Dynamic size, no need for resizing.

Memory Overhead: Although linked lists excel in dynamic memory management, they incur additional memory overhead due to the storage of pointers/references in each node. This overhead can be significant, especially in memory-constrained environments or when the data size is small relative to the pointer size.

Arrays, with their contiguous memory structure, avoid such overhead, making them more memory-efficient for large datasets needing random access.

•Arrays: Lower memory overhead.

•Linked Lists: Higher memory overhead due to pointers/references.

Cache Friendliness: Arrays benefit from spatial locality, meaning consecutive elements are stored in proximity. This property enhances cache performance, leading to faster data retrieval and operations.



Linked lists, by contrast, lack spatial locality due to non-contiguous allocation, potentially leading to poorer cache performance and increased access times.

This difference is crucial in high-performance applications where cache efficiency is paramount.

•Arrays: Better cache performance.

•Linked Lists: Poorer cache performance.

Understanding these distinctions is pivotal for making informed decisions on data structure selection, ensuring optimal performance and resource utilization in varying computational scenarios.



Chapter 5 Stacks and Queues

This chapter provides an in-depth examination of stacks and queues, beginning with their definitions and operations. It includes implementations in Python and explores various types of queues. The chapter highlights practical applications of both data structures and compares their performance and use cases, offering a comprehensive overview of these fundamental concepts.

5.1 Introduction to Stacks

A **stack** is a linear data structure that adheres to the Last In, First Out (LIFO) principle. In a stack, the element added last is the one to be removed first. This characteristic makes stacks particularly useful in scenarios where data needs to be stored and retrieved in reverse order from which it was added.

The fundamental operations associated with a stack are:

Push: Adds an element to the top of the stack.

Pop: Removes the element from the top of the stack.

Peek (or **Top**): Returns the top element of the stack without removing it.

isEmpty: Checks whether the stack is empty.

Size: Returns the number of elements in the stack.

These operations allow for efficient management of data with constant time complexity, O(1), making stacks optimal for applications requiring such access patterns.

To illustrate the behavior of stack operations, consider the following abstract representation:

```
Initial Stack (Empty): []
Push(1): [1]
Push(2): [1, 2]
Push(3): [1, 2, 3]
Peek(): 3
Pop(): 3 => [1, 2]
Pop(): 2 => [1]
```

Push adds 1, then 2, and then 3 to the stack. The **Peek** operation then retrieves the top element (3), and subsequent **Pop** operations remove the elements from the top one by one.

Python, like other high-level programming languages, provides a simple way to implement a stack using its built-in list type. Lists in Python come with method implementations that directly support stack operations: append() for push, pop() for pop, and indexing for peek.

Here is a basic example of a stack implementation in Python:

```
class Stack:
    def_init_(self):
        self.items = []

    def is_empty(self):
        return len(self.items) == 0

    def push(self, item):
        self.items.append(item
    )
```

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```
def pop(self):
    if self.is_empty():
        raise IndexError("pop from empty
    stack") return self.items.pop()

def peek(self):
    if self.is_empty():
        raise IndexError("peek from empty
    stack") return self.items[-1]

def size(self):
    return len(self.items)
```

In this implementation, we define a class Stack with the necessary methods to perform stack operations. The is_empty method checks if the stack is empty, push adds an item to the stack, pop removes the top item, peek retrieves the top item without removing it, and size returns the number of items in the stack.

This stack class can be instantiated and utilized as follows:

```
stack =
Stack()
stack.push(1)
stack.push(2)
stack.push(3)
print(stack.peek()) # Output:
3 print(stack.pop()) # Output:
3 print(stack.size()) #
Output: 2
```

The output would be:

3

2

The LIFO principle that stacks adhere to is particularly useful in various computer science applications. For instance:

- **Function Call Management**: In most programming languages, function calls are managed using a call stack to keep track of active subroutines. When a function is called, its execution context is pushed onto the stack. When the function completes, the context is popped from the stack.
- **Expression Evaluation**: Stacks are used in the evaluation and parsing of expressions, particularly in the conversion of infix expressions to postfix expressions and their subsequent evaluation.
- **Backtracking Algorithms**: Stacks facilitate algorithms that involve exploring possible solutions and backtracking upon hitting a dead end, such as depth-first search (DFS) in graph traversal.
- **Undo Mechanism**: Many software applications use stacks to implement undo functionality, where the most recent action can be undone by popping from the stack of actions.

In addition to these, stacks are a fundamental part of many other data structures and algorithms, contributing to optimal and efficient solutions to complex problems. Their simplicity and efficiency make them indispensable in both theoretical and practical aspects of computing.



5.2 Stack Operations



Stacks are abstract data types that follow the Last In, First Out (LIFO) principle. Several fundamental operations can be performed on stacks, each essential for effective manipulation of stack data. The primary stack operations to be discussed include push, pop, peek (or top), isEmpty, and size.

Push Operation

The push operation adds an element to the top of the stack. Since stacks are LIFO, the element added is always appended at the highest available position in the stack. The time complexity of a push operation is O(1), as it involves inserting the element at a fixed position. Below is a Python implementation of the push operation:

```
class Stack:
   def_init_(self):
        self.items = []

   def push(self, item):
        self.items.append(item
   )
```

When using the push method, it appends the specified item to the end of the items list representing the stack.

Pop Operation

The pop operation removes and returns the top element from the stack. This operation also has a time complexity of O(1), as it involves accessing and removing the element from the list's end. The following Python code illustrates the pop operation:

```
class Stack:
    def_init_(self):
        self.items = []

    def push(self, item):
        self.items.append(item
      )

    def pop(self):
        if not self.is_empty():
            return
            self.items.pop()
        raise IndexError("pop from empty stack")
```

The pop method first checks if the stack is empty to avoid an IndexError, then uses the list's pop function to remove and return the last item.

Peek (Top) Operation

The peek operation returns the top element of the stack without removing it, providing insight into the stack's current state. The time complexity of peek is O(1), as it involves a single element access. Here is an implementation of the peek operation:

```
class Stack:
    def_init_(self):
        self.items = []

    def push(self, item):
        self.items.append(item)
```

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```
def pop(self):
    if not self.is_empty():
        return
        self.items.pop()
    raise IndexError("pop from empty stack")

def peek(self):
    if not self.is_empty():
        return
        self.items[-1]
    raise IndexError("peek from empty stack")
```

The peek method checks if the stack is empty and returns the last item using index -1 to access the top element.

is Empty Operation

The is_empty operation checks whether the stack contains any elements, returning True if the stack is empty and False otherwise. The time complexity is O(1). Below is the corresponding implementation:

```
class Stack:
    def_init_(self):
        self.items = []

    def is_empty(self):
        return len(self.items) == 0
```

The is_empty method evaluates whether the number of elements in the items list is zero.

Size Operation

The size operation returns the number of elements currently stored in the stack. It also operates in constant time, O(1). Example implementation:

```
class Stack:
   def_init_(self):
      self.items = []

def size(self):
    return len(self.items)
```

By leveraging the len function on the items list, the size method efficiently computes the current stack size.

To clarify the execution of these operations, consider the following code demonstrating a series of stack manipulations:

```
s = Stack()
s.push(1) # Stack: [1]
s.push(2) # Stack: [1, 2]
s.push(3) # Stack: [1, 2, 3]
print(s.pop()) # Output: 3, Stack: [1, 2]
print(s.peek()) # Output: 2, Stack: [1,
2] print(s.is_empty()) # Output: False
print(s.size()) # Output: 2
```

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```
3
2
False
2
```

This example stack creation and manipulation illustrate the push, pop, peek, is_empty, and size operations comprehensively. The stack's state evolves with each operation, reflecting the characteristic LIFO behavior and providing practical experience with stack operations in Python.

5.3 Stack Implementation in Python

A stack is a linear data structure that follows the Last In, First Out (LIFO) principle. In Python, a stack can be implemented using various methods, including lists and the deque module from the collections library. We will explore these implementations using Python code and detailed explanations.

```
class Stack:
  def_init_(self):
     self.stack = []
  def is empty(self):
     return len(self.stack) == 0
  def push(self, item):
      self.stack.append(item
  def pop(self):
     if self.is empty():
        raise IndexError("Pop from empty
      stack") return self.stack.pop()
   def peek(self):
     if self.is empty():
        raise IndexError("Peek from empty
      stack") return self.stack[-1]
   def size(self):
     return len(self.stack)
```

In the above implementation, the Stack class encapsulates stack behaviors using a list as the underlying storage. The methods provided are as follows:

- •__init___: Initializes an empty stack.
- is empty: Returns True if the stack is empty, False otherwise.
- push: Appends an item to the top of the stack.
- pop: Removes and returns the top item of the stack. Raises an IndexError if the stack is empty.
- peek: Returns the top item of the stack without removing it. Raises an IndexError if the stack is empty.
- size: Returns the number of items in the stack.

Next, we consider an implementation using the deque module from the collections library. The deque (double-ended queue) provides an efficient stack implementation.



```
from collections import deque
class StackDeque:
  def_init_(self):
     self.stack =
     deque()
  def is empty(self):
     return len(self.stack) == 0
  def push(self, item):
     self.stack.append(item
  def pop(self):
      if self.is empty():
        raise IndexError("Pop from empty
     stack") return self.stack.pop()
  def peek(self):
      if self.is empty():
        raise IndexError("Peek from empty
     stack") return self.stack[-1]
   def size(self):
      return len(self.stack)
```

In this implementation, the StackDeque class utilizes the deque collection. The methods align with those from the previous list-based implementation:

```
•__init___: Initializes an empty deque.
```

is empty: Checks if the deque is empty and returns a boolean.

push: Adds an item to the end of the deque.

pop: Removes and returns the last item of the deque. Errors if the deque is empty.

peek: Provides a view of the last item in the deque without removal.

*size: Returns the length of the deque.

```
Example Usage of Stack (List-Based):
>>> stack = Stack()
>>> stack.push(1)
>>> stack.push(2)
>>> stack.peek()
2
>>> stack.pop()
2
>>> stack.is_empty()
False
>>> stack.size()
1

Example Usage of StackDeque (deque-Based):
>>> stack_deque = StackDeque()
```

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```
>>> stack_deque.push(1)
>>> stack_deque.push(2)
>>> stack_deque.peek()
2
>>> stack_deque.pop()
2
>>> stack_deque.is_empty()
False
>>> stack_deque.size()
1
```

While both implementations are effective, the deque offers more efficient append and pop operations from both ends, making it a generally preferable choice for stack operations. The choice between a list-based and deque-based implementation can depend on specific application requirements and performance considerations.

5.4 Applications of Stacks

Stacks are utilized in a variety of computational contexts owing to their Last-In-First-Out (LIFO) property. This behavior is particularly advantageous in scenarios where the most recent item needs to be accessed first. Below are some key applications of stacks, described in detail.

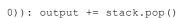
Function Call Management: Stacks play a crucial role in managing function calls in programming languages. When a function is invoked, its execution context (such as local variables, return address, etc.) is pushed onto a call stack. Upon completion of the function, the context is popped from the stack, ensuring that the control returns to the proper location in the program. This mechanism is vital in supporting recursive function calls, where each call must maintain its execution context independently from others.

```
def
  factorial(n):
  if n == 0:
    return
1 else:
    return n * factorial(n-1)
```

In the above code, each call to factorial results in a new stack frame being pushed onto the call stack, preserving the state of the computation until the base case is reached.

Expression Evaluation: Stacks are widely used in the evaluation of arithmetic expressions, particularly converting Infix expressions (human readable) to Postfix expressions (which machines can evaluate more easily). The Shunting Yard algorithm by Edsger Dijkstra is a classical method that uses a stack to achieve this conversion.

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```
stack.append(char
) while stack:
   output +=
stack.pop() return
output
```

This algorithm ensures that the operators are placed in the correct order using a stack.

Syntax Parsing: In the parsing phase of compilers, stacks are instrumental in checking balanced parentheses in expressions and code blocks. When encountering an opening parenthesis, it is pushed onto the stack. A closing parenthesis requires a matching opening parenthesis to be popped from the stack.

```
def
   is balanced(expression):
  stack = []
  for char in
     expression: if char
     in "([{":
        stack.append(char
     ) elif char in
      ")]}":
        if not stack:
           return
           False
         top = stack.pop()
        if not matches (top,
           char): return False
   return not stack
def matches (opening,
  closing): openings = "([{"
  closings = ")]}"
   return openings.index(opening) == closings.index(closing)
```

This function ensures that every opening parenthesis corresponds to a closing one in the correct order, validating the syntax of the expression.

Undo Mechanisms: Many applications, such as text editors, implement undo mechanisms by maintaining actions in a stack. When an operation is performed, it is pushed onto the undo stack. To undo an operation, it is popped from the stack, and an opposite action is executed (which might be pushed onto a redo stack).

```
class TextEditor:
    def_init_(self):
        self.text = ""
        self.undo_stack =
        []

    def write(self, char):
        self.text += char
        self.undo_stack.append(char
    )

    def undo(self):
```

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```
if not
    self.undo_stack:
    return
self.text =
self.text[:-1]
self.undo_stack.pop()
```

This simplistic example demonstrates how each character typed can be undone by popping from the undo stack.

Depth-First Search (DFS): In graph traversal algorithms, such as Depth-First Search, stacks are utilized to explore nodes in a depthward motion. Each time a new node is visited, it is pushed onto the stack; backtracking occurs when a node has no unvisited adjacent nodes, achieved by popping the stack.

```
def depth_first_search(graph,
    start): stack, visited =
    [start], set() while stack:
    vertex = stack.pop()
    if vertex not in
       visited:
       visited.add(vertex)
       stack.extend(neighbour for neighbour in graph[vertex] if neighbour not in
    visited) return visited
```

This algorithm ensures an exhaustive search of the graph in a manner that leverages the LIFO property of stacks to facilitate backtracking.

Hanoi Towers Simulation: The simulation of the classic Tower of Hanoi puzzle can be implemented using stacks. Here, each rod is represented by a stack, and the movement of disks follows the game's rules by pushing and popping disks between stacks.

```
def move_tower(height, from_pole, to_pole, with_pole,
    stacks): if height >= 1:
        move_tower(height - 1, from_pole, with_pole, to_pole,
        stacks) move_disk(from_pole, to_pole, stacks)
        move_tower(height - 1, with_pole, to_pole, from_pole, stacks)

def move_disk(from_pole, to_pole,
    stacks): disk =
    stacks[from_pole].pop()
    stacks[to_pole].append(disk)
    print(f"Moving disk from {from pole} to {to pole}")
```

This simulation demonstrates how disks are transferred between poles (stacks).

These examples illustrate the versatility of stacks in handling a range of computational tasks, underlining their importance in the field of computer science.

5.5 Introduction to Queues

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A queue is a linear data structure that follows a specific order for element operations, known as First-In-First-Out (FIFO). In a queue, the first element added to the structure will be the first one to be removed. This property is analogous to a real-life queue, such as a line of customers waiting for service, where the first customer to arrive is the first to be served.

The primary operations associated with a queue include:

Enqueue: The process of adding an element to the end of the queue.

Dequeue: The process of removing an element from the front of the queue.

Front: Retrieves, but does not remove, the front element of the queue.

Rear: Retrieves, but does not remove, the last element of the queue.

IsEmpty: Checks if the queue is empty.

Size: Returns the number of elements in the queue.

Queues are essential in various computing scenarios, including scheduling algorithms, breadth-first search (BFS) in graph theory, and buffering in data streams. They provide a mechanism to manage tasks in a sequential processing order.

The following pseudocode illustrates the fundamental operations of a queue:

```
class Oueue:
  def_init_(self):
     self.items = []
  def is empty(self):
     return len(self.items) == 0
  def enqueue(self, item):
     self.items.append(item
  def dequeue(self):
     if not self.is empty():
        return
        self.items.pop(0)
     else:
        raise IndexError("dequeue from an empty queue")
  def front(self):
     if not
        self.is empty():
        return
        self.items[0]
        raise IndexError("front from an empty queue")
  def rear(self):
     if not self.is empty():
        return
        self.items[-1]
        raise IndexError("rear from an empty queue")
```

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```
def size(self):
    return len(self.items)
```

Upon initializing a queue, the items list will store the elements. The is_empty method checks if the queue has no elements. The enqueue method appends an element to the end of the list, effectively adding it to the rear of the queue. The dequeue method removes and returns the front element of the queue. If the queue is empty, it raises an IndexError. The front method returns the front element without removing it, while the rear method returns the last element. The size method returns the count of elements in the queue.

The behavior of the queue ensures that elements are processed in the exact order they were added, which makes queues particularly useful for resource management tasks and in contexts where order of operations is critical. For example, queues are utilized in operating systems for task scheduling, managing print jobs in printers, and in networking for packet-routing.

The efficiency of queue operations is critical, with enqueue and dequeue expected to operate in O(1) time complexity. However, this is only achievable when the queue is implemented using data structures optimized for these operations, such as linked lists. With the basic list implementation shown above, the dequeue operation is O(n) due to the need to shift all elements one position to the left.

Another important aspect is the variation of queue data structures that cater to specific requirements. Common variants include:

Circular Queue: Overcomes the limitation of fixed queue size by reusing empty space created by dequeued elements.

Priority Queue: Elements are dequeued in order of priority rather than FIFO order.

Double-ended Queue (Deque): Allows insertion and deletion of elements from both ends, providing additional flexibility.

Each variant maintains the fundamental principles of a queue but introduces additional characteristics to handle more complex scenarios and requirements in computing systems. Understanding these nuances and implementations allows for selecting the appropriate queue type based on specific task requirements, effectively using queues to optimize and structure operations in data processing and resource management applications.

5.6 Queue Operations

A queue is a linear data structure that follows the First-In-First-Out (FIFO) principle, where the first element inserted into the queue is the first one to be removed. This structure features two main operations: **enqueue** and **dequeue**, along with some auxiliary operations such as **isEmpty**, **isFull**, **front**, and **rear**. These operations are fundamental in understanding how queues function and are implemented.

The **enqueue** operation is responsible for adding an element to the rear of the queue. If the queue is not full, the element is inserted into the position pointed to by the rear pointer, and the rear pointer is then incremented to the next position.

```
def enqueue(queue, element, rear,
    size): if rear == size:
        print("Queue is
    full") else:
        queue[rear] =
        element rear += 1
```

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return rear

The **dequeue** operation removes an element from the front of the queue. This involves checking if the queue is empty and, if not, removing the element pointed to by the front pointer and then incrementing the front pointer.

```
def dequeue(queue, front,
    rear): if front == rear:
    print("Queue is
    empty") return front,
    None
    else:
        element =
        queue[front] front +=
        1
        return front, element
```

Checking if the queue is empty can be done using the **isEmpty** operation, which simply compares the front and rear pointers. If they're equal, the queue is empty.

```
def isEmpty(front,
    rear): return front
== rear
```

The **isFull** operation determines if the queue has reached its maximum capacity, which is when the rear pointer equals the size of the queue.

```
def isFull(rear,
    size): return rear
== size
```

The **front** operation retrieves the element at the front of the queue without removing it and is useful for inspecting the queue's state.

```
def front(queue, front,
  rear): if isEmpty(front,
  rear):
    print("Queue is
    empty") return None
  return queue[front]
```

Similarly, the rear operation retrieves the element at the rear of the queue without removing it.

```
def rear(queue, rear):
    return queue[rear-1] if rear != 0 else None
```

Each operation is crucial for the proper functioning of the queue data structure. Understanding these operations and their Python implementations is foundational for leveraging queues in various applications, such as task scheduling, buffering, and handling real-time system demands.

5.7 Queue Implementation in Python

Queues in Python can be efficiently implemented using lists or by utilizing the collections.deque class from the Python standard library, which provides an optimized double-ended queue. Here, we delve into both implementations, highlighting their syntax, operations, and efficiency.

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Using Lists

Python lists can be used to simulate a queue, but with some performance trade-offs. Lists are dynamic arrays that allow us to add or remove elements. The operations for a queue are *enqueue* (add elements to the back), and *dequeue* (remove elements from the front). Below is the implementation using lists:

```
class ListQueue:
    def_init_(self):
        self.queue = []

def is_empty(self):
        return len(self.queue) == 0

def enqueue(self, item):
        self.queue.append(item
    )

def dequeue(self):
    if not self.is_empty():
    return self.queue.pop(0) else:
        raise IndexError("dequeue from empty queue")

def size(self):
    return len(self.queue)
```

In this list-based implementation:

- The enqueue operation uses the append () method to add an item to the end of the list, with a time complexity of O(1).
- The dequeue operation uses the pop (0) method to remove the first item from the list. This operation has a time complexity of O(n), as it involves shifting all subsequent elements one position to the left.

Considering the O(n) time complexity for the dequeue operation, lists are not the most efficient way to implement a queue, especially for large datasets.

Using collections.deque

The deque (double-ended queue) from the collections module provides a much more efficient means to implement a queue. It allows appending and popping from both ends of the queue with a time complexity of O(1).

```
from collections import deque

class DequeQueue:
    def_init_(self):
        self.queue =
        deque()

    def is_empty(self):
        return len(self.queue) == 0

    def enqueue(self, item):
```

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```
self.queue.append(item
)

def dequeue(self):
    if not self.is_empty():
        return
        self.queue.popleft()
    else:
        raise IndexError("dequeue from empty queue")

def size(self):
    return len(self.queue)
```

In this deque-based implementation:

- The enqueue operation uses the append () method to add an item to the end, with a time complexity of O(1).
- The dequeue operation uses the popleft () method to remove the first item, also with a time complexity of O(1).

The deque provides an efficient and straightforward alternative for implementing a queue, with constant time complexity for both enqueue and dequeue operations, making it suitable for applications requiring frequent insertions and deletions.

Comparison

Both implementations achieve the primary goal of providing a queue with basic operations. However, they differ significantly in performance, particularly for the dequeue operation:

List-based Queue: While easy to implement, the list-based queue suffers from O(n) dequeue operation time complexity due to the need to shift elements after removing the front item.

tleque-based Queue: The deque-based queue is efficient with O(1) time complexity for both enqueue and dequeue operations, making it superior for practical applications, especially when handling large amounts of data.

Example Usage

Below is an illustrative example demonstrating the usage of the DequeQueue class:

```
if_name == "_main_":
    queue = DequeQueue()
    queue.enqueue(10)
    queue.enqueue(20)
    queue.enqueue(30)
    print("Current queue size:", queue.size()) # Output: 3

    print("Dequeued element:", queue.dequeue()) # Output: 10
    print("Dequeued element:", queue.dequeue()) # Output: 20

    print("Current queue size:", queue.size()) # Output: 1

    print("Is the queue empty?", queue.is empty()) # Output:
```

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```
queue.dequeue()
print("Is the queue empty?", queue.is_empty()) # Output: True

try:
    queue.dequeue() # This will raise an IndexError
except IndexError as
    e: print("Error:",
    e)

The output of this code will be:
Current queue size: 3
Dequeued element: 10
Dequeued element: 20
Current queue size: 1
Is the queue empty? False
Is the queue empty? True
Error: dequeue from empty queue
```

This example demonstrates the basic operations of enqueuing, dequeuing, checking the queue size, and handling the empty queue scenario with the DequeQueue class.

5.8 Types of Queues

False

In this section, we explore various types of queues beyond the basic First-In-First-Out (FIFO) model. Each queue type has unique characteristics and use cases, allowing more sophisticated data management schemes. We will discuss the following queue types: Simple Queue, Circular Queue, Priority Queue, Double-Ended Queue (Deque).

Simple Queue: A simple queue, or a linear queue, follows the FIFO principle. Elements are enqueued at the rear and dequeued from the front. Below is the implementation of a simple queue using Python:

```
class SimpleQueue:
  def_init_(self):
     self.queue = []
  def is empty(self):
     return len(self.queue) == 0
   def enqueue(self, item):
     self.queue.append(item
      )
  def dequeue(self):
     if not self.is empty():
        return
        self.queue.pop(0)
        raise IndexError("Dequeue from an empty queue")
   def peek(self):
     if not
        self.is empty():
```

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```
return
    self.queue[0]
else:
    raise IndexError("Peek from an empty queue")

def size(self):
    return len(self.queue)

# Example usage:
q =
SimpleQueue()
q.enqueue(1)
q.enqueue(2)
q.enqueue(3)
print(q.dequeue()) # Output:
1 print(q.peek()) # Output: 2
print(q.size()) # Output: 2
```

Circular Queue: A circular queue addresses the limitations of a simple queue by treating the queue as a circular buffer. When the end of the queue is reached, it wraps around to the beginning. Here is an implementation of a circular queue:

```
class CircularQueue:
   def_init_(self, size):
      self.size = size
      self.queue = [None] * size
      self.front = self.rear =
   def is full(self):
      return (self.rear + 1) % self.size == self.front
   def is empty(self):
      return self.front ==
   def enqueue(self,
      item): if
      self.is full():
         raise IndexError("Enqueue on a full
      queue") elif self.is empty():
         self.front = self.rear =
      0 else:
         self.rear = (self.rear + 1) %
      self.size self.queue[self.rear] = item
   def dequeue(self):
      if self.is empty():
         raise IndexError("Dequeue from an empty
      queue") elif self.front == self.rear:
         item =
         self.queue[self.front]
         self.front = self.rear = -1
```

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```
else:
        item = self.queue[self.front]
        self.front = (self.front + 1) %
      self.size return item
  def peek(self):
     if self.is empty():
        raise IndexError("Peek from an empty
     queue") return self.queue[self.front]
  def size(self):
        self.is empty()
         : return 0
     elif self.rear >= self.front:
        return self.rear - self.front +
        1
      else:
        return self.size - self.front + self.rear + 1
# Example usage:
cq =
CircularQueue(3)
cq.enqueue(1)
cq.enqueue(2)
cq.enqueue(3)
print(cq.dequeue()) # Output: 1
cq.enqueue(4) print(cq.peek()) # Output: 2
```

Priority Queue: A priority queue assigns a priority level to each element. Elements with higher priority are dequeued before those with lower priority. If two elements have the same priority, the FIFO order is maintained. Here's a Python implementation using the heapq module:

```
import heapq

class PriorityQueue:
    def_init_(self):
        self.queue = []

    def is_empty(self):
        return len(self.queue) == 0

    def enqueue(self, priority, item):
        heapq.heappush(self.queue, (priority, item))

    def dequeue(self):
        if self.is_empty():
            raise IndexError("Dequeue from an empty queue") return heapq.heappop(self.queue)[1]

    def peek(self):
        if self.is_empty():
```

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```
raise IndexError("Peek from an empty
    queue") return self.queue[0][1]

# Example usage:
pq = PriorityQueue()
pq.enqueue(3, 'low')
pq.enqueue(1, 'high')

pq.enqueue(2,
'medium')
print(pq.dequeue()) # Output: high
print(pq.peek()) # Output: medium
```

Double-Ended Queue (Deque): A deque allows insertion and deletion of elements from both ends, combining aspects of stacks and queues. Below is the implementation of a deque using Python's collections module:

```
from collections import deque
class Deque:
  def_init_(self):
     self.deque =
     deque()
  def is empty(self):
     return len(self.deque) == 0
  def add front(self, item):
      self.deque.appendleft(item
  def add rear(self, item):
     self.deque.append(item
  def
     remove_front(self):
     if self.is empty():
        raise IndexError("Remove from an empty
     deque") return self.deque.popleft()
  def
     remove_rear(self):
     self.is empty():
         raise IndexError("Remove from an empty
     deque") return self.deque.pop()
  def peek_front(self):
     if
      self.is empty():
        raise IndexError("Peek from an empty
```

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```
deque") return self.deque[0]

def peek_rear(self):
    if
    self.is_empty()):
       raise IndexError("Peek from an empty deque") return self.deque[-1]

# Example usage:
dq = Deque()
```



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dq.add_rear(1)
dq.add front(2



```
dq.add_rear(3)
print(dq.remove_front()) # Output: 2
print(dq.remove_rear()) # Output: 3
```

5.9 Applications of Queues

Queues are fundamental data structures widely employed in various computing and real-world scenarios due to their First-In-First-Out (FIFO) nature. This property ensures that the order of processing is preserved, which is critical in many applications. Herein, we delve into several practical applications of queues, demonstrating their versatility and efficacy.

1. Task Scheduling: Queues are extensively used in operating systems for task scheduling. In a multi- tasking environment, where numerous processes compete for CPU time, a queue can manage these processes efficiently. The operating system places all incoming processes in a queue and schedules them based on their arrival order.

```
from collections import deque

class TaskScheduler:
    def_init_(self):
        self.queue = deque()

    def add_task(self,

    task):
```



```
self.queue.append(task)
   def
      execute task(self):
      if self.queue:
         return
      self.queue.popleft() return
      None
 scheduler =
TaskScheduler()
 scheduler.add task("Task
scheduler.add task("Task 2")
print(scheduler.execute task()) # Output: Task
 1 print(scheduler.execute task()) # Output:
Task 2
Task 1
Task 2
```

2. Print Spooling: In a networked environment with multiple print requests, queues manage print job spooling. Each print job is placed in a queue and processed sequentially, ensuring that print commands are executed in the order they were received.

```
class PrintSpooler:
   def_init_(self):
      self.queue = deque()
   def add_print_job(self,
      job):
      self.queue.append(job)
   def
      process job(self):
      if self.queue:
         return
      self.queue.popleft() return
      None
 spooler = PrintSpooler()
 spooler.add_print_job("Job
 spooler.add print job("Job 2")
 print(spooler.process job()) # Output: Job
 1 print(spooler.process_job()) # Output:
 Job 2
Job 1
Job 2
```

3. Breadth-First Search (BFS) in Graphs: Queues facilitate the BFS algorithm in graph traversal, ensuring exploration starts from the given node and moves level by level. This method is instrumental in finding the shortest path in unweighted graphs.

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```
def bfs(graph,
   start node): visited =
   set()
   queue =
   deque([start_node])
   visited.add(start node)
   while queue:
      current node =
      queue.popleft()
      print(current node, end=" ")
      for neighbor in
         graph[current node]: if
         neighbor not in visited:
            queue.append(neighbor
            visited.add(neighbor)
graph = {
   'A': ['B', 'C'],
   'B': ['A', 'D', 'E'],
   'C': ['A', 'F'],
   'D': ['B'],
   'E': ['B'],
    'F': ['C']
bfs(graph, 'A')
ABCDEF
```

- **4. Handling of Interrupts in Real-time Systems:** Real-time systems often use queues to handle interrupts. An interrupt handler places each interrupt request into a queue, where they are processed in the order received, ensuring timely and predictable handling.
- 5. Customer Service Systems: Customer service departments utilize queues to manage incoming customer requests, be it in a call center or a service desk. Each customer is attended to in the order they arrived, which is crucial for fairness and efficiency.

```
class
   CustomerService:
   def_init_(self):
      self.queue = deque()

   def add_customer(self,
      customer):
      self.queue.append(customer)

   def
      serve_customer(self):
      if self.queue:
        return
```

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```
self.queue.popleft() return
    "No customers to serve"

service = CustomerService()
service.add_customer("Customer
1")
service.add_customer("Customer 2")
print(service.serve_customer()) # Output: Customer
1 print(service.serve_customer()) # Output:
Customer 2

Customer 1
Customer 2
```

- **6. Traffic Management:** Queues are utilized in traffic management systems, especially at traffic signals. Vehicles queue up at red lights and are allowed to pass sequentially when the light turns green, ensuring orderly traffic flow.
- 7. **Simulation of Real-life Scenarios:** In simulation models for various scenarios like customer checkout lines in supermarkets or network packet routing, queues help mimic real-life waiting lines, providing insights into system performance and behavior under different conditions.

These applications underscore queues' essential role in both computational tasks and real-world problem-solving, showcasing their utility and robustness in maintaining order and ensuring fair processing of tasks. The FIFO characteristic pivotal to queues is central to achieving efficiency and predictability across diverse applications.

5.10 Comparison of Stacks and Queues

Stacks and queues are fundamental data structures in computer science, each with distinctive characteristics and use cases. Both are abstract data types that allow for the collection and manipulation of homogeneous elements, but they differ significantly in terms of how these elements are inserted and removed. Understanding their differences helps to select the appropriate data structure based on specific problem requirements.

Order of Operations: Stacks follow a Last In, First Out (LIFO) principle, which means that the last element added to the stack is the first one to be removed. This behavior is likened to a stack of plates, where the plate on the top is the first to be taken off. In contrast, queues follow a First In, First Out (FIFO) principle, meaning that the first element added is the first one to be removed, similar to a line of people where the person at the front exits first.

Basic Operations: Both stacks and queues support three primary operations: insertion, deletion, and inspection of elements. However, the manner in which these operations are performed diverges.

Insertion (Push for Stacks, Enqueue for Queues): For stacks, the push operation adds an element to the top of the stack. For queues, the enqueue operation adds an element to the rear of the queue.

Deletion (Pop for Stacks, Dequeue for Queues): The pop operation in a stack removes the topmost element. Conversely, the dequeue operation in a queue removes the frontmost element.

Inspection (Peek for Stacks, Front for Queues): The peek operation in a stack returns the topmost element without removing it, while the front operation in a queue returns the element at the front without removing it.

Use Cases: Their differences in operational order endow stacks and queues with specific advantages for certain applications.

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Stacks: Ideal for scenarios where the most recently added element needs to be accessed first. For example:

Function Call Management: The call stack in programming languages where function calls and their local variables are managed is a classic example.

Undo Mechanism: Undo features in text editors or graphic applications, where the most recent action is reversed first.

Expression Evaluation: Parsing and evaluating expressions, such as converting infix to postfix notation.

Queues: Suitable for applications where the first element needs to be processed first. For example:
 Order Processing: Handling tasks or jobs in the order they arrive, as seen in print queues.
 Data Streaming: Managing data packets in network routers where packets are processed in the order they arrive.

Breadth-First Search (BFS): Implementing BFS in graph traversal, where nodes are explored in the order of their distance from the source node.

Python Implementation: Both stacks and queues can be implemented using Python lists, although their operations and performance characteristics can vary slightly due to the underlying list operations.

```
class Stack:
  def_init_(self):
     self.items = []
   def is empty(self):
      return self.items ==
  def push(self, item):
      self.items.append(item
  def pop(self):
     return self.items.pop()
  def peek(self):
      return self.items[-1]
  def size(self):
     return len(self.items)
stack =
Stack()
stack.push(1)
stack.push(2)
print(stack.pop()) # Output: 2
class Queue:
  def_init_(self):
     self.items = []
  def is empty(self):
      return self.items ==
```

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```
def enqueue(self, item):
    self.items.insert(0,
    item)

def dequeue(self):
    return self.items.pop()

def size(self):
    return len(self.items)

queue = Queue()
queue.enqueue(1
)
queue.enqueue(2
)
print(queue.dequeue()) # Output: 1
```

[]



While Python lists can be used for both implementations, the time complexity for queue operations using a list where insertion is performed at the front (O(n)) and deletion at the rear (O(1)) makes it inefficient for large data sets. This is due to the shifting of all other elements during insertion. Queue implementations can hence benefit from collections such as deque from Python's collections module, which provides average O(1) time complexity for both append and pop operations.

```
from collections import deque
class Queue:
  def_init_(self):
     self.items =
     deque()
  def is empty(self):
     return len(self.items) == 0
   def enqueue(self, item):
      self.items.append(item) #
      0(1)
   def dequeue(self):
     return self.items.popleft() # 0(1)
   def size(self):
     return len(self.items)
queue = Oueue()
queue.enqueue(1
queue.enqueue(2
print(queue.dequeue()) # Output: 1
```

Analyzing the differences between stacks and queues provides insights into their application in solving various computational problems. Their appropriate use can lead to efficient memory and time management, optimizing performance for specific tasks.

5.11 Performance Considerations in Stacks and Queues

Understanding the performance of stacks and queues is crucial for effective algorithm design and implementation. Both data structures offer distinct operational efficiencies and selecting the appropriate one can significantly influence the performance of an application. This section elucidates the critical performance aspects of stacks and queues, providing detailed analysis on time and space complexities associated with their operations.

Time Complexity Analysis:

Stacks and queues both support a well-defined set of operations (such as push, pop, enqueue, dequeue, etc.) which we will analyze here.

Stacks:

•push: Adding an element to the top of the stack.

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pop: Removing the topmost element from the stack.

peek/top: Accessing the topmost element without removing it.



These operations are typically implemented using arrays or linked lists.

Array-based implementation:

- push operation: This involves adding an element at the end of an array, which has constant time complexity, i.e., O(1). However, if the array is full and needs to be resized (usually doubled in size), the amortized time complexity remains O(1).
- \Rightarrow op operation: This removes the last element of the array, also constant time, O(1).
- ϕ eek/top operation: Accessing the top element without removal has a time complexity of O(1).

Linked list-based implementation:

- ϕ ush operation: Adding an element at the head of the list takes O(1) time.
- pop operation: Removing the head element also takes O(1) time.
- ϕ eek/top operation: Accessing the head element without removal takes O(1) time.

From this, it is evident that stack operations, regardless of the underlying implementation, provide constant time complexity, O(1), which guarantees high performance in scenarios requiring frequent push and pop operations.

Queues:

- enqueue: Adding an element to the end of the queue.
- dequeue: Removing an element from the front of the queue.
- peek/front: Accessing the front element without removing it.

Array-based implementation:

- enqueue operation: When implemented using circular arrays, adding an element at the rear, wrapping around as necessary, takes O(1) time.
- dequeue operation: Removing the front element, updating the front pointer, also takes O(1) time.
- $\phi = k/front$ operation: Accessing the front element without removal takes O(1) time.

Linked list-based implementation:

- enqueue operation: Adding an element at the tail of the list takes O(1) time.
- \bullet dequeue operation: Removing the head element takes O(1) time.
- ϕ eek/front operation: Accessing the head element without removal takes O(1) time.

Analyzing both array and linked list implementations shows that standard queue operations also adhere to constant time complexity, O(1).

Space Complexity Analysis:

The space complexity of both data structures depends on the underlying storage mechanism, i.e., arrays or linked lists.

Array-based implementation:

The array must be of a pre-defined size or dynamically resized. Space complexity is O(n), where n is the number of elements, disregarding any additional overhead for dynamically resizing arrays in amortized scenarios.

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Linked list-based implementation:

Each element requires additional space for pointers, but the space complexity remains O(n), where n is the number of elements stored.

Practical Performance Considerations:

Besides theoretical analysis, practical performance is influenced by factors such as memory locality, cache performance, and overhead of dynamic memory allocation.

Memory locality and cache performance:

- Array-based implementations benefit from better memory locality. Consecutive elements are stored in contiguous memory locations, enhancing cache performance.
- Linked list implementations suffer from poor locality, as nodes may be scattered across memory, leading to more cache misses.

Overhead of dynamic memory allocation:

- Linked lists involve overhead for dynamic allocation and deallocation, which can affect performance when operations are frequent.
- Arrays, particularly those with a fixed size or resized infrequently, have minimal allocation overhead.

Selecting between stacks and queues and their particular implementations depends on specific application requirements. Factors like the expected number of elements, frequency of operations, and memory constraints should be considered to optimize performance. For environments with predictable load and frequent access to elements, array-based structures are often preferred due to their superior cache performance. For applications requiring flexible and dynamic memory management, linked lists might be more suitable despite their relatively higher overhead.



Chapter 6 Trees

This chapter offers a thorough exploration of tree data structures, covering basic concepts and different types such as binary trees, binary search trees (BST), AVL trees, B-trees, heaps, and trie trees. It explains tree traversal methods, as well as insertion and deletion operations in BSTs. Additionally, the chapter discusses practical applications and performance considerations, providing a comprehensive understanding of trees.

6.1 Introduction to Trees

A tree is a hierarchical data structure that simulates a hierarchical tree structure with a root value and subtrees of children, represented as a set of linked nodes. Trees are widely used in computer science due to their efficiency in various operations and their ability to model relationships between data elements naturally. Each tree structure is composed of nodes, where each node holds a value or condition, and references to other nodes. The fundamental concepts essential to understanding trees include nodes, edges, root, leaves, and height.

Nodes: A node is an individual element of a tree holding data. Each node can have zero or more child nodes. The nodes that have the same parent are called siblings.

Edges: An edge is the connection between two nodes. It signifies the relationship between the parent and the child nodes.

Root: The node at the top of the tree is called the root. It is the only node with no parent. Every tree must have a root node.

Leaves: Nodes that do not have any children are called leaves or leaf nodes. They are also known as external nodes.

Height of a Tree: The height of a tree is the length of the longest path from the root to a leaf. It signifies the maximum number of edges from the root to the leaf.

Depth of a Node: The depth of a node is the number of edges from the root to the node.

Subtree: A subtree represents any node of the tree and all of its descendants.

The hierarchical nature of trees makes them suitable for representing hierarchical data structures such as organizational structures, file systems, and abstract syntax trees. Trees provide several beneficial properties:

- Efficient traversal and search operations.
- Hierarchical representation of data.
- Recursive nature enabling simpler implementation of algorithms.

Types of Trees:



- **Binary Trees**: Each node has at most two children, often termed the left and right child.
- **Binary Search Trees (BST)**: A binary tree with the property that the left child of a node contains a value less than the node's value, and the right child contains a value greater than the node's value.
- **AVL Trees**: A self-balancing binary search tree where the difference between the heights of the left and right subtrees of any node is no more than one.
- **B-Trees**: A generalization of binary search trees where nodes can have more than two children. They are optimized for systems that read and write large blocks of data.
- **Heaps**: A special tree-based data structure that satisfies the heap property. In a max-heap, each parent node is greater than or equal to its children; in a min-heap, each parent node is less than or equal to its children.
- •Trie Trees: A tree used to store a dynamic set or associative array where the keys are usually strings.

Tree Representation: There are multiple ways to represent trees in a program. The most common representations include:

1. Linked Representation: Each node is an object. Nodes have references to their children.

```
class TreeNode:
    def___init_(self, key):
        self.key = key
        self.left = None
        self.right = None
```

2. List Representation: Parent nodes and child nodes are indexed in a list.

```
tree = [
   [1, 2], # Node 0 has children 1 and 2
   [None, None], # Node 1 is a leaf node
   [None, None] # Node 2 is a leaf node
```

Traversal Methods: Trees can be traversed in multiple ways. The fundamental tree traversal methods include:

- **Pre-order traversal**: Process the root node first, then recursively process the left subtree, followed by the right subtree.
- **4n-order traversal**: Recursively process the left subtree first, then the root node, followed by the right subtree.
- **Post-order traversal**: Recursively process the left subtree, the right subtree, and finally the root node
- **Level-order traversal**: Traverse nodes level by level, starting from the root.

In many applications, trees help improve the efficiency and performance for operations such as search, insertion, and deletion, particularly when compared to linear data structures like arrays or linked lists.



Understanding the fundamental concepts of trees and their various types and representations is crucial for mastering more advanced topics in data structures and algorithms. Subsequent sections will delve into specific tree types and explore their properties, operations, and applications in greater depth.

6.2 Binary Trees

A binary tree is a hierarchical data structure in which each node has at most two children, referred to as the left child and the right child. A binary tree is defined recursively as either being empty or consisting of a root node with two subtrees, each of which is also a binary tree. This structure forms the basis of many algorithms and data structures, making it essential to understand its properties, implementation, and real-world applications.

Properties of Binary Trees:

- •Maximum Nodes: A binary tree of depth d (where the root node is at depth 0) can have at most 2^d nodes at depth d, and $2^{d+1}-1$ nodes in total.
- *Minimum Nodes:* The minimum number of nodes in a binary tree of depth d is d + 1 (a tree where each node has only one child).
- *Height of Binary Tree*: The height of a binary tree is defined as the length of the longest path from the root to a leaf. For a tree with a single node, the height is 0.
- *Balanced Binary Tree: A binary tree is balanced if, for every node in the tree, the height difference of the left and right subtrees is at most one.

Binary Tree Representation: Binary trees can be implemented using various representations, two of which are array representation and linked representation.

Array Representation: In an array representation of a binary tree, the nodes are stored in a sequential manner. The root is placed at the first position of the array (index 0 or 1 depending on 1-based or 0-based indexing). For a node at index *i*,

- •The left child is at index 2i + 1 (0-based indexing) or 2i (1-based indexing).
- •The right child is at index 2i + 2 (0-based indexing) or 2i + 1 (1-based indexing).

This method is efficient in terms of space but becomes inefficient when the tree is sparse because it leads to wasted space.

Linked Representation: In the linked representation, each node is an object containing three fields:

- •A data element
- •A reference to the left child.
- •A reference to the right child.

This approach is often used as it allows the tree to grow dynamically. Below is an example of a simple binary tree node class in Python using the linked representation.



```
class TreeNode:
    def___init_(self, key):
        self.left = None
        self.right = None
        self.val = key

# Example of creating a binary tree with this class
root = TreeNode(1) root.left
= TreeNode(2) root.right =
TreeNode(3) root.left.left =
TreeNode(4)
root.left.right = TreeNode(5)
```

Traversing a Binary Tree: Traversal of a binary tree refers to the process of visiting each node in the tree exactly once in a systematic way. There are several common methods of binary tree traversal, each serving different purposes.

```
Inorder Traversal (Left, Root, Right):
```

```
def inorder_traversal(root): if
  root:
    inorder_traversal(root.left)
    print(root.val, end=' ')
    inorder_traversal(root.right)
```

Preorder Traversal (Root, Left, Right):

```
def preorder_traversal(root):
    if root:
        print(root.val, end=' ')
        preorder_traversal(root.left)
        preorder traversal(root.right)
```

Postorder Traversal (Left, Right, Root):

```
def postorder_traversal(root): if
  root:
    postorder_traversal(root.left)
    postorder_traversal(root.right)
    print(root.val, end=' ')
```

Applications of Binary Trees: Binary trees are fundamental structures in computer science, often utilized in the following scenarios:

- *Expression Trees:* Used in compilers to represent expressions. Each leaf is an operand, and each internal node is an operator.
- Binary Search Trees (BSTs): Facilitates efficient searching, insertion, and deletion operations.
- *Heaps:* Implement priority queues.



- *Decision Trees: Used in machine learning for decision-making processes.
- •Syntax Trees: Used in natural language processing to parse sentences.

The straightforward nature of binary trees and their extensive applicability in various domains highlight their importance in both theoretical and practical aspects. Whether through array or linked representations, the ability to traverse and manipulate binary trees efficiently is a foundational skill for proficient programming and algorithm design. Detailed understanding of binary tree traversal methodologies lays the groundwork for mastering more complex tree structures and algorithms discussed in subsequent sections.

6.3 Tree Traversal Methods

In computer science, tree traversal refers to the process of visiting each node in a tree data structure exactly once in a systematic manner. Efficient traversal methods are critical for performing operations such as searching, inserting, and deleting nodes in trees. This section discusses commonly used tree traversal methods: Pre-order, In-order, Post-order, and Level-order traversal.

Pre-order Traversal: In a pre-order traversal, the nodes are recursively visited in this order: the root node, the left subtree, and then the right subtree. For a tree with root R, left child L, and right child R, the traversal follows $R \to L \to R$. The pseudo-code for pre-order traversal is:

```
def preOrderTraversal(node): if
  node is not None:
    print(node.data)
    preOrderTraversal(node.left)
    preOrderTraversal(node.right)
```

For example, given the following tree structure:



The pre-order traversal would visit the nodes in the following order: $\mathbb{A} \to \mathbb{B} \to \mathbb{D} \to \mathbb{E} \to \mathbb{C}$. The output is:

```
ABDEC
```

In-order Traversal: In-order traversal visits the nodes in the following order: the left subtree, the root node, and then the right subtree. This method is often utilized for binary search trees (BSTs) because it results in nodes being visited in non-decreasing order. The pseudo-code for in-order traversal is:

```
def inOrderTraversal(node):
   if node is not None:
      inOrderTraversal(node.left)
```

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```
print(node.data)
inOrderTraversal(node.right)
```

Using the same example tree, the in-order traversal would visit the nodes in the following order:

```
D \rightarrow B \rightarrow E \rightarrow A \rightarrow C. The output is:
 D B E A C
```

Post-order Traversal: Post-order traversal recursively visits nodes in the following order: the left subtree, the right subtree, and then the root node. It is often used for deleting or freeing nodes and various tree-related algorithms that require processing child nodes before their parent nodes. The pseudo-code for post-order traversal is:

```
def postOrderTraversal(node):
    if node is not None:
        postOrderTraversal(node.left)
        postOrderTraversal(node.right)
        print(node.data)
```

For the example tree, the post-order traversal would visit the nodes in the following order: $D \to E$ $\to B \to C \to A$. The output is:

Level-order Traversal: Level-order traversal, also known as breadth-first traversal, visits nodes level by level from top to bottom and left to right within each level. This is typically implemented using a queue data structure to keep track of the nodes. The pseudo-code for level-order traversal is:

```
from collections import deque

def levelOrderTraversal(root): if
  root is None:
     return
  queue = deque([root])
  while queue:
     node = queue.popleft()
     print(node.data)

  if node.left is not None:
        queue.append(node.left)
   if node.right is not None:
        queue.append(node.right)
```

In the example tree, the level-order traversal would visit the nodes in the following order: $A \to B$ $\to C \to D \to E$. The output is: $A \to C \to D \to E$



These traversal methods provide comprehensive ways to visit every node in a tree, each serving different practical scenarios depending on the requirements of the tree-based operation. The choice of traversal method is determined by the desired order in which the nodes should be processed.

6.4 Binary Search Trees (BST)

A Binary Search Tree (BST) is a particular type of binary tree that maintains a specific order among its elements, facilitating efficient search, insertion, and deletion operations. In a BST, each node contains a key, and possibly associated data, with the key values organized such that:

- •The key in the left child of a node is less than the key in the parent node.
- •The key in the right child of a node is greater than the key in the parent node.
- Both the left and right sub-trees of each node are also binary search trees.

This ordering allows for binary search properties to be applied, ensuring operations are logarithmic in complexity in the average case.

Definition and Properties

Formally, a BST is defined as a binary tree where for every node *n*:

where left(n) and right(n) denote the left and right children of n, respectively.

The primary properties of BSTs include:

- **Searching:** Given a key, the structure of the BST allows for efficient querying by recursively traversing left or right sub-trees, depending on whether the key is lesser or greater than the current node's key.
- **Insertion:** New keys are inserted by recursively finding the correct position that maintains the binary search property.
- **Deletion:** Removing a node from a BST is more complex and involves three primary cases: deleting a leaf node, deleting a node with one child, and deleting a node with two children.

Operations in BSTs

Search Operation

Given a BST, the search operation is performed by comparing the target key with the root node's key. Based on the comparison, the algorithm decides to proceed to either the left or the right subtree, continually narrowing down the search space.

```
class Node:
    def___init_(self, key):
        self.left = None
        self.right = None
```

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```
self.val = key

def search(root, key):
   if root is None or root.val == key:
       return root

if root.val < key:
       return search(root.right, key)

return search(root.left, key)</pre>
```

Insertion Operation

Insertions in a BST maintain its ordered structure. Starting from the root, we recursively find the position to insert the new key such that the binary search property is preserved.

```
def insert(root, key):
    if root is None:
        return Node(key)

if key < root.val:
        root.left = insert(root.left, key)
    else:
        root.right = insert(root.right, key)</pre>
```

Deletion Operation

Deletion in a BST handles three distinct cases:

1. **Node to be deleted is a leaf node: ** Simply remove the node. 2. **Node to be deleted has one child: ** Remove the node and replace it with its child. 3. **Node to be deleted has two children: ** - Find the in-order successor (the smallest key in the right sub-tree). - Replace the node's key with the in-order successor's key. - Delete the in-order successor.

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```
elif key > root.val:
    root.right = deleteNode(root.right, key)
else:
    if root.left is None:
        temp = root.right
        root = None return
        temp
    elif root.right is None:
        temp = root.left root
        = None
        return temp

temp = minValueNode(root.right)
    root.val = temp.val
    root.right = deleteNode(root.right, temp.val)
```

Traversal Methods

Traversal methods for BSTs include in-order, pre-order, and post-order traversals, which are defined the same way as for binary trees. In-order traversal is particularly useful for BSTs as it visits nodes in ascending order of their keys.

```
def inorderTraversal(root):
    if root:
        inorderTraversal(root.left)
        print(root.val, end=" ")
        inorderTraversal(root.right)
```

Performance Considerations

BSTs offer logarithmic time complexity operations for balanced trees, but the worst-case complexity can degrade to linear time when the tree becomes skewed (i.e., resembles a linked list). The shape of the tree depends on the order of insertions and deletions.

Balanced variants such as AVL trees or Red-Black trees are often employed to ensure logarithmic time complexities for all operations. These balanced trees automatically adjust to maintain their structure, generally ensuring O(log n) performance.

Understanding and implementing BSTs form a critical foundation for advanced data structures and algorithms. The operations and properties outlined serve as the cornerstone for understanding more complex balanced trees explored in subsequent sections.

6.5 Insertion in BST



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The insertion operation in a Binary Search Tree (BST) is a fundamental procedure that maintains the tree's distinctive property: for any given node, all elements in the left subtree are less than the node's key, and all elements in the right subtree are greater than the node's key. This section delves into the mechanisms of the insertion process, detailing the algorithm, its implementation in Python, and the implications on the BST's structure and balance.

To insert a new key into a BST, we initially start at the root and traverse the tree following the BST property until we find the correct location for the new node. The following steps outline this process:

- 1. **Start at the Root**: Begin the operation at the root node. 2. **Traverse the Tree**: Compare the key of the new node, *k*, with the key of the current node:
 - If k is less than the current node's key, move to the left child.
 - If *k* is greater than the current node's key, move to the right child.
- 3. **Find the Position**: Continue this procedure recursively until the appropriate NULL position is found (where either the left or right pointer of a node is NULL). 4. **Insert the Node**: Insert the new node at the identified position.

The time complexity of the insertion operation in a BST is O(h), where h is the height of the tree. In the worst-case scenario, for an unbalanced BST, h can be as large as n, the number of nodes, resulting in O(n) complexity. In a balanced tree, $h = \log n$, yielding $O(\log n)$ complexity.

Python Implementation

The following Python code demonstrates the insertion process in a BST.

```
class Node:
   def___init_(self, key):
      self.left = None
      self.right = None
      self.val = key
def insert (root, key):
   # If the tree is empty, return a new node
   if root is None:
      return Node (key)
   # Otherwise, recur down the tree
   if key < root.val:
      root.left = insert(root.left, key)
   else:
      root.right = insert(root.right, key)
   # return the (unchanged) node pointer
   return root.
```



```
# Function to do inorder tree traversal
def inorder(root):
    if root:
        inorder(root.left)
        print(root.val, end=' ')
        inorder(root.right)

# Driver program to test the above functions
root = None
keys = [20, 8, 22, 4, 12, 10, 14]

for key in keys:
    root = insert(root, key)

print("Inorder traversal of the BST:")
inorder(root)
```

In the provided implementation, the 'insert()' function initiates by checking if the current root is NULL. If so, it creates a new node with the specified key. Otherwise, it compares the key with the value of the root node and recursively calls itself to either the left or right subtree accordingly. The 'inorder()' function is used for verification of the insertion process by performing an inorder traversal of the tree, which should produce a sorted sequence of inserted keys.

Example Execution

```
Inorder traversal of the BST:
4 8 10 12 14 20 22
```

This output verifies that keys are correctly inserted and placed to conform to the BST properties.

Effect on Tree Structure

The insertion of nodes affects the overall structure and balance of the tree. Repeated insertions of sequential or random keys can result in highly unbalanced trees with unfavorable height. For example, inserting keys in ascending or descending order will yield a degenerate tree (similar to a linked list), where each node has only one child. This scenario is detrimental as it degrades the performance of search, insertion, and deletion operations to O(n).

Effective strategies to maintain tree balance, such as self-balancing mechanisms (e.g., AVL trees, Red-Black trees), will be discussed in subsequent sections. Ensuring balance is crucial for achieving the ideal performance of $O(\log n)$ for the aforementioned operations.

Understanding the insertion process in BSTs forms the bedrock for mastering tree data structures. The presented approach and implementation are fundamental, serving as a precursor to more sophisticated tree algorithms and structures.

6.6 Deletion in BST

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Deletion in a Binary Search Tree (BST) is a fundamental operation that ensures the integrity and utility of the data structure as elements are dynamically removed. When an element is deleted from a BST, three primary cases must be handled: deleting a leaf node, deleting a node with one child, and deleting a node with two children. Each case maintains the BST property, i.e., for any given node, all elements in the left subtree are less than the node, and all elements in the right subtree are greater.

Let's delve into each case with meticulous detail.

Case 1: Deleting a Leaf Node

A leaf node is a node that has no children. Deleting a leaf node is the simplest case. We only need to remove the node from the tree and update the parent node to adjust its reference accordingly.

For example, consider the following BST:

To delete the node 20: 1. Find the node to be deleted (20). 2. Since 20 is a leaf node, simply remove it.

The resulting BST is:

Case 2: Deleting a Node with One Child

This case involves a node that has exactly one child, either left or right. The process requires the child to take the place of the node to be deleted.

Consider the same BST example, and let's delete the node 30, which has one child (node 40):

1. Find the node to be deleted (30). 2. Since 30 has one child (40), remove 30 and replace it with 40.

The resulting BST is:



Case 3: Deleting a Node with Two Children

This is the most complex case. A node with two children requires finding the node's in-order predecessor or successor to maintain the BST properties.

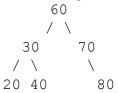
The process to delete a node with two children is as follows:

1. Find the node to be deleted. 2. Find its in-order successor (smallest node in the right subtree) or in-order predecessor (largest node in the left subtree). 3. Replace the node's value with the in-order successor's (or predecessor's) value. 4. Delete the in-order successor (or predecessor), which will now have at most one child.

Consider again the BST example. To delete the node 50, which has two children:

1. Find the node to be deleted (50). 2. Find the in-order successor of 50, which is 60 (smallest node in the right subtree of 50). 3. Replace the value of 50 with 60. 4. Delete the node 60, which has no children.

The resulting BST is:



Python Implementation

The following Python code demonstrates the deletion process in a BST:

```
class TreeNode:
   def___init_(self, key):
      self.left = None
      self.right = None
      self.val = key
def deleteNode (root, key):
   if root is None:
      return root
   if key < root.val:
      root.left = deleteNode(root.left, key)
   elif key > root.val:
      root.right = deleteNode(root.right, key)
   else:
      if root.left is None:
         return root.right
      elif root.right is None:
         return root.left
```



```
temp = minValueNode(root.right)
root.val = temp.val
root.right = deleteNode(root.right, temp.val)

return root

def minValueNode(node): current
= node
while current.left is not None:
    current = current.left
return current
```

The deleteNode function follows the aforementioned steps for deletion: 1. It searches for the node with the specified key. 2. Once found, if the node has no children or only one child, the node is simply replaced by its child. 3. If the node has two children, it replaces the node's value with its in-order successor's value and recursively deletes the successor node.

The helper function minValueNode finds the in-order successor, ensuring the proper maintenance of BST properties during deletion.

Ensuring correctness in these operations is critical for maintaining the efficiency and structural integrity of the BST, keeping operations like search, insertion, and deletion at optimal time complexities.

6.7 AVL Trees

AVL trees, named after their inventors Adelson-Velsky and Landis, are a type of self-balancing binary search tree (BST). In an AVL tree, the heights of the two child subtrees of any node differ by at most one, ensuring that the tree remains approximately balanced. This balancing is crucial as it guarantees $O(\log n)$ time complexity for insertion, deletion, and lookup operations, where n is the number of nodes in the tree.

An AVL tree maintains its balance through a series of rotations that adjust the structure after insertions or deletions. This section delves into the fundamental properties of AVL trees, their balancing mechanisms, and the operations for insertion and deletion with corresponding rotations.

Balance Factor:

The balance factor of a node in an AVL tree is the difference between the heights of the left and right subtrees. Formally, for a node N:

```
BalanceFactor(N) = Height(LeftSubtree) - Height(RightSubtree)
```

A node is considered balanced if its balance factor is -1, 0, or 1. If the balance factor of any node becomes less than -1 or greater than 1, the tree requires rebalancing.

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Rotations:

Rotations are operations that change the structure of the tree without altering the in-order sequence of elements, thereby preserving the BST property. There are four types of rotations used to restore balance in an AVL tree:

1. **Left Rotation (LL Rotation)**: A left rotation is performed when a right-heavy subtree becomes unbalanced.



Transforms to:



2. **Right Rotation (RR Rotation)**: A right rotation is performed when a left-heavy subtree becomes unbalanced.



Transforms to:



- 3. **Left-Right Rotation (LR Rotation)**: When a left subtree is right-heavy, a double rotation (left-right) is needed. This involves a left rotation on the left child followed by a right rotation on the unbalanced node.
- 4. **Right-Left Rotation (RL Rotation)**: When a right subtree is left-heavy, a double rotation (right-left) is needed. This involves a right rotation on the right child followed by a left rotation on the unbalanced node.

Insertion in AVL Tree:



The insertion process in an AVL tree involves performing a standard BST insertion followed by verifying and restoring balance through rotations if necessary.

Consider the following function for inserting a node in an AVL tree:

```
class TreeNode:
   def___init_(self, key):
      self.key = key
      self.left = None
      self.right = None
      self.height = 1
def insert (node, key):
   # Step 1: Perform the normal BST insertion
   if not node:
      return TreeNode(key)
   elif key < node.key:
      node.left = insert(node.left, key)
   else:
      node.right = insert(node.right, key)
   # Step 2: Update the height of the ancestor node
   node.height = 1 + max(get height(node.left), get height(node.right))
   # Step 3: Get the balance factor
   balance = get balance(node)
   # Step 4: If the node becomes unbalanced, then balance it
   # Case 1: Left Left
   if balance > 1 and key < node.left.key:
      return right rotate(node)
   # Case 2: Right Right
   if balance < -1 and key > node.right.key:
      return left_rotate(node)
   # Case 3: Left Right
   if balance > 1 and key > node.left.key:
      node.left = left rotate(node.left)
      return right rotate (node)
   # Case 4: Right Left
   if balance < -1 and key < node.right.key:
      node.right = right rotate(node.right)
      return left rotate(node)
```



```
def left rotate(z):
   y = z.right
   T2 = y.left
   y.left = z
   z.right = T2
   z.height = 1 + max(get_height(z.left), get_height(z.right))
   y.height = 1 + max(get_height(y.left), get_height(y.right))
   return y
def right rotate(z):
   v = z.left
   T3 = y.right
   y.right = z
   z.left = T3
   z.height = 1 + max(get_height(z.left), get_height(z.right))
   y.height = 1 + max(get_height(y.left), get_height(y.right))
   return y
def get height(node):
   if not node:
      return 0 return
   node.height
def get_balance(node):
   if not node:
      return 0
   return get height(node.left) - get height(node.right)
```

Executing the insertion and rotations ensures the AVL tree remains balanced after each insertion.

Deletion in AVL Tree:

return node

Deletion in an AVL tree involves similar steps: performing a standard BST deletion followed by verifying and restoring the balance through rotations.

Consider the deletion procedure outlined below:

```
def delete(node, key):
   if not node:
```

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```
# Step 1: Perform standard BST deletion
   if key < node.key:
      node.left = delete(node.left, key)
   elif key > node.key:
      node.right = delete(node.right, key)
   else:
      if node.left is None:
         return node.right
      elif node.right is None:
         return node.left
      temp = get_min_value_node(node.right)
      node.key = temp.key
      node.right = delete(node.right, temp.key)
   # Step 2: Update the height of the current node
   node.height = 1 + max(get_height(node.left), get_height(node.right))
   # Step 3: Get the balance factor
   balance = get balance(node)
   # Step 4: Restore balance if necessary
   # Case 1: Left Left
   if balance > 1 and get balance(node.left) >= 0:
      return right rotate(node)
   # Case 2: Left Right
   if balance > 1 and get balance(node.left) < 0:
      node.left = left rotate(node.left)
      return right_rotate(node)
   # Case 3: Right Right
   if balance < -1 and get balance(node.right) <= 0:
      return left_rotate(node)
   # Case 4: Right Left
   if balance < -1 and get balance(node.right) > 0:
      node.right = right rotate(node.right)
      return left rotate(node)
   return node
def get min value node (node):
```

if node is None or node.left is None:

return node



return node
return get_min_value_node(node.left)

This deletion operation ensures that the AVL tree remains balanced by performing necessary rotations after each deletion.

The balancing operations through rotations maintain the tree's height at $O(\log n)$, which is critical for ensuring efficient performance in dynamic set operations. These detailed procedures facilitate a deeper understanding of how AVL trees manage structural modifications to preserve their balanced nature

6.8 B-Trees

B-Trees are balanced tree data structures that maintain sorted data and allow searches, sequential access, insertions, and deletions in logarithmic time. The B-Tree, a generalization of the binary search tree (BST), is optimized for systems that read and write large blocks of data, such as databases and file systems.

Unlike a binary tree, where each node has at most two children, a B-Tree of order m (also denoted as a B-m Tree) allows a node to have up to m children and m-1 keys. This feature contributes to the B-Tree's high degree of balancement, ensuring that the tree remains shallow, facilitating efficient disk reads and writes.

Key properties of B-Trees are:

- €ach node has at most *m* children.
- Each internal node contains between $\lceil m/2 \rceil$ and m children (except for the root, which may have as few as two children).
- •All leaves appear on the same level.

Structure of B-Tree Node:

A B-Tree node comprises the following components:

- An array of k keys $(k \le m-1)$, each key separating the values in its subtrees.
- An array of child pointers, where each pointer references a subtree, thus maintaining the property of sorted order.

Thus, if x is a B-Tree node with n[x] keys, and k_i denoting the i-th key, then:

$$k_1 < k_2 < \quad \text{and} \quad k_{n[x]}$$

The pointers $c_1, c_2, ..., c_{n[x]+1}$ point to the subtrees where any key k in the subtree c_i satisfies: k_{i-1}

$$<$$
 k_i

for i = 1, 2, ..., n[x] + 1, assuming that $k_0 = -\infty$ and $k_{n[x]+1} = +\infty$.



Searching in B-Trees:

Searching in a B-Tree starts at the root and proceeds until a leaf node is reached. Consider a B-Tree where each node contains keys $k_1, k_2, ..., k_n$ and child pointers $c_1, c_2, ..., c_{n+1}$.

To search for a key *k*:

- 1. Start at the root node.
- 2. Check the current node for the key k.
- 3. If the key is found, return the node along with the position of *k* in that node.
- 4. If the key is not found, identify the interval $[k_{i-1}, k_i)$ where k should belong, and proceed to the child node at position c_i .
- 5. Repeat the process until reaching a leaf node.

Below is the code for searching in a B-Tree:

```
class BTreeNode:
    def___init_(self, t, leaf=False):
        self.t = t
        self.keys = []
        self.children = []
        self.leaf = leaf

def search(x, k):
    i = 0
    while i < len(x.keys) and k > x.keys[i]: i
        += 1

    if i < len(x.keys) and k == x.keys[i]:
        return (x, i)
    elif x.leaf:
        return None
    else:
        return search(x.children[i], k)</pre>
```

Insertion in B-Trees:

Insertion in a B-Tree requires maintaining the tree properties, particularly ensuring that nodes do not overflow. When a node exceeds the maximum permissible number of keys, it is split into two nodes, and the middle key is promoted to the parent node. This process may propagate up to the root, possibly increasing the height of the tree.

Steps for inserting a key k into a B-Tree of order t:

- 1. If the root node is full (contains 2t 1 keys), split the root and create a new root.
- 2. Traverse from the root to the appropriate leaf node as in a search operation.
- 3. Insert the key *k* into the leaf node in sorted order.



4. If the leaf node exceeds the permissible keys, split the node, and promote the median key to the parent node.

Below is the code for insertion in a B-Tree:

```
def split child(parent, i, child): t
   = child.t
   new child = BTreeNode(t, child.leaf)
   parent.keys.insert(i, child.keys[t-1])
   parent.children.insert(i+1, new_child)
   new child.keys = child.keys[t:]
   child.keys = child.keys[:t-1]
   if not child.leaf:
      new child.children = child.children[t:]
      child.children = child.children[:t]
def insert_non_full(x, k):
   i = len(x.keys) - 1
   if x.leaf:
      x.keys.append(0)
      while i \ge 0 and x.keys[i] > k:
         x.keys[i+1] = x.keys[i]
         i -= 1
      x.keys[i+1] = k
      while i \ge 0 and x.keys[i] > k: i
         -= 1
      i += 1
      if len(x.children[i].keys) == 2*x.t - 1:
         split_child(x, i, x.children[i])
         if k > x.keys[i]:
             i += 1
      insert non full(x.children[i], k)
def insert(tree, k):
   r = tree.root
   if len(r.keys) == 2 * tree.t - 1: s
      = BTreeNode(tree.t, False)
      tree.root = s
      s.children.insert(0, r)
      split child(s, 0, r)
      insert non full(s, k)
```



```
else:
   insert_non_full(r, k)
```

Deletion in B-Trees:

Deletion in B-Trees is more complex than insertion. The goal is to remove a key while maintaining B-Tree properties. Key scenarios include deleting from a leaf node, deleting from an internal node, and ensuring internal nodes retain the minimum number of keys.

Three major cases guide the deletion process:

- 1. If the key is in a leaf node, remove it directly.
- 2. If the key is in an internal node:
 - •If the predecessor or successor has at least *t* keys, replace the key with it and recursively delete the predecessor or successor.
 - •If both the preceding and subsequent children have the minimum number of keys, merge these children.
- 3. If the key is not present in the node, proceed to the appropriate child node:
 - •If the child has the minimum number of keys, ensure it has at least *t* keys by borrowing or merging nodes.

Below is the code for deletion in a B-Tree:

```
def merge(parent, i):
   child = parent.children[i]
   sibling = parent.children[i+1]
   child.keys.append(parent.keys[i])
   child.keys.extend(sibling.keys)
   if not child.leaf:
      child.children.extend(sibling.children)
   parent.keys.pop(i)
   parent.children.pop(i+1)
def borrow from next(parent, i):
   child = parent.children[i]
   sibling = parent.children[i+1]
   child.keys.append(parent.keys[i])
   parent.keys[i] = sibling.keys[0]
   sibling.keys.pop(0)
   if not sibling.leaf:
      child.children.append(sibling.children[0])
      sibling.children.pop(0)
```



```
def borrow_from_prev(parent, i):
   child = parent.children[i]
   sibling = parent.children[i-1]
   child.keys.insert(0, parent.keys[i-1])
   parent.keys[i-1] = sibling.keys.pop()
   if not child.leaf:
      child.children.insert(0, sibling.children.pop())
def fill(parent, i):
   if i != 0 and len(parent.children[i-1].keys) >= parent.t:
      borrow from prev(parent, i)
   elif i != len(parent.children) - 1 and len(parent.children[i+1].keys) >= parent.t:
      borrow from next(parent, i)
   else:
      if i != len(parent.children) - 1:
         merge(parent, i)
      else:
          merge(parent, i-1)
def delete_from_non_leaf(node, idx): k
   = node.keys[idx]
   if len(node.children[idx].keys) >= node.t:
      pred = get pred(node, idx) node.keys[idx]
      = pred delete(node.children[idx], pred)
   elif len(node.children[idx+1].keys) >= node.t:
      succ = get succ(node, idx)
      node.keys[idx] = succ
      delete(node.children[idx+1], succ)
   else:
      merge(node, idx)
      delete(node.children[idx], k)
def delete(node, k):
   idx = 0
   while idx < len(node.keys) and node.keys[idx] < k:</pre>
   if idx < len(node.keys) and node.keys[idx] == k: if</pre>
      node.leaf:
          node.keys.pop(idx)
      else:
         delete from non leaf(node, idx)
   else:
```



```
if node.leaf:
    return

flag = (idx == len(node.keys))

if len(node.children[idx].keys) < node.t:
    fill(node, idx)

if flag and idx > len(node.keys):
    delete(node.children[idx-1], k)

else:
    delete(node.children[idx], k)
```

B-Trees effectively balance nodes to maintain search, insertion, and deletion operations' efficiency, making them a suitable choice for filesystem and database management systems. Their structured nature ensures consistent performance even with substantial data growth, adhering to logarithmic time complexity guarantees.

6.9 Heaps

Heaps are a specialized tree-based data structure that satisfies the heap property. This property is what distinguishes heaps from other types of trees. A heap can be of two types: a **min-heap** or a **max-heap**. In a min-heap, for any given node i, the value of i is less than or equal to the values of its children. Conversely, in a max-heap, the value of i is greater than or equal to the values of its children. This characteristic makes heaps particularly useful for implementing priority queues.

Properties of Heaps:

- •A heap is a complete binary tree. This means all levels of the tree are fully filled except possibly for the last level, which must be filled from left to right.
- •The heap property must be maintained after any insertion or deletion operation, ensuring the min-heap or max-heap property is preserved.

Heap Representation:

Heaps are typically represented using arrays, which allows for efficient storage and manipulation. Given a node at index i in an array:

- The left child can be found at index 2i + 1
- •The right child can be found at index 2i + 2
- The parent can be found at index $\lfloor \frac{i-1}{2} \rfloor$

The array representation allows efficient access and manipulation of the heap's elements.

Basic Operations on Heaps:

1. **Insertion:** Inserting a new element into a heap involves adding the element at the end of the heap (maintaining the complete binary tree property) and then performing a **heapify-up** (also known as bubble-up, percolate-up, sift-up, or trickle-up) operation to restore the heap property.

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```
def heapify_up(heap, index):
    parent_index = (index - 1) // 2
    if parent_index >= 0 and heap[index] < heap[parent_index]: heap[index],
        heap[parent_index] = heap[parent_index], heap[index] heapify_up(heap,
        parent_index)

def insert(heap, element):
    heap.append(element)
heapify_up(heap, len(heap) - 1)</pre>
```

2. **Deletion:** The removal of the root element (the minimum in the case of a min-heap or the maximum in the case of a max-heap) requires replacing the root with the last element of the heap and then performing a **heapify-down** (also known as bubble-down, percolate-down, sift-down, or trickle-down) operation to restore the heap property.

```
def heapify down(heap, index):
   left child index = 2 * index + 1
   right child index = 2 * index + 2
   smallest = index
   if left child index < len(heap) and heap[left child index] < heap[smallest]:
      smallest = left_child_index
   if right child index < len(heap) and heap[right child index] < heap[smallest]:
      smallest = right child index
   if smallest != index:
      heap[index], heap[smallest] = heap[smallest], heap[index]
      heapify down(heap, smallest)
def delete min(heap):
   if len(heap) == 1:
      return heap.pop()
   root = heap[0] heap[0]
   = heap.pop()
   heapify down(heap, 0)
   return root
```

3. **Heap Construction:** Building a heap from an arbitrary list of elements can be done efficiently in O(n) time using the **heapify** process. Starting from the lowest non-leaf nodes and moving upwards, we perform heapify-down on each node.

```
def build_heap(elements):
   heap = elements.copy()
   start_index = len(heap) // 2 - 1
   for index in range(start_index, -1, -1):
      heapify_down(heap, index)
   return heap
```



Applications of Heaps:

Heaps have diverse applications in various domains:

- **Priority Queues:** Heaps are the ideal choice for priority queues where elements with higher (or lower) priority need to be served first.
- **Heap Sort:** An efficient comparison-based sorting algorithm that uses a heap data structure. The time complexity of heap sort is $O(n \log n)$.
- **Graph Algorithms:** Dijkstra's Shortest Path and Prim's Minimum Spanning Tree algorithms leverage heaps for efficient edge selection.

Through the formal definition, properties, and operations discussed, we gain comprehensive insight into heaps' functioning and implementation. The following is an example that demonstrates the insertion, deletion, and heap construction in a priority queue context implemented using a min-heap.

```
class MinHeap:
    def___init_(self):
       self.heap = []
    def insert(self, element):
       self.heap.append(element)
       heapify up(self.heap, len(self.heap) - 1)
    def extract min(self):
       if len(self.heap) == 0:
          return None
       if len(self.heap) == 1:
          return self.heap.pop()
       root = self.heap[0] self.heap[0]
       = self.heap.pop()
       heapify down(self.heap, 0)
       return root
    def build heap(self, elements):
       self.heap = build heap(elements)
 mh = MinHeap()
 mh.build heap([10, 20, 15, 30, 40])
 print(mh.extract min())
10
```

In this implementation, the class MinHeap encapsulates heap operations, providing an efficient and reusable data structure for managing priorities.

6.10 Trie Trees



Trie trees, commonly referred to simply as tries (pronounced "trees" or "try"), are specialized tree-based data structures that efficiently store a dynamic set of strings where the keys are usually strings. Tries are particularly useful for tasks involving collections of strings, such as autocomplete features, spell checkers, and IP routing.

A trie is defined by its nodes and edges. Each node represents a prefix of the strings inserted into the trie, and each edge represents a single character extending from one prefix to its next. The root node corresponds to the empty prefix, and each subsequent node corresponds to the prefixes formed by the characters traversed from the root to that node.

A fundamental characteristic of a trie is that all descendants of a node share a common prefix. The root is associated with the empty string, and each descending node adds one more character to the accumulated value of the parent node.

To construct a trie, we consider each character of a string as a step deeper into the tree. Here's how insertion of a string into a trie can be implemented in Python:

```
class TrieNode:
    def ___init__(self):
        self.children = {}
        self.is_end_of_word = False

class Trie:
    def ___init__(self):
        self.root = TrieNode()

    def insert(self, word):
        node = self.root for
        char in word:
        if char not in node.children:
            node.children[char] = TrieNode()
        node = node.children[char]
        node.is end of word = True
```

In this implementation, the TrieNode class represents individual nodes of the trie. Each node has a dictionary variable children that stores its child nodes and a boolean is_end_of_word to mark the end of a word. The Trie class maintains the root node of the trie and provides an insert function to add words.

To search for a string in a trie, you traverse the trie according to the characters in the string. If you reach the end of the string and the node is end of word is True, the string exists in the trie:

```
def search(self, word):
   node = self.root for
   char in word:
      if char not in node.children:
        return False
```

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```
node = node.children[char]
return node.is_end_of_word
```

The time complexity for both insertion and search operations in a trie is O(m), where m is the length of the string. This efficiency owes to the fact that each character in the string corresponds to one depth level of the trie.

Another common operation in a trie is searching for all words with a given prefix. This is particularly useful for implementing autocompletion. Starting from the node representing the prefix, a Depth-First Search (DFS) can be used to collect all words that have the prefix:

```
def _collect_all_words(self, node, prefix, words): if
   node.is_end_of_word:
       words.append(prefix)

for char, child_node in node.children.items():
       self._collect_all_words(child_node, prefix + char, words)

def autocomplete(self, prefix):
   node = self.root
   for char in prefix:
       if char not in node.children:
           return []
   node = node.children[char]

words = []
   self._collect_all_words(node, prefix, words)
   return words
```

In the autocomplete function, the _collect_all_words helper function performs the DFS from the node that corresponds to the end of the prefix, collecting all words that stem from that node.

Trie trees also have numerous variations to optimize specific use-cases. One such variation is the compressed trie (or Radix tree), which collapses chains of single nodes. Another variation is the ternary search tree, which stores characters at nodes in a binary search tree fashion, conserving space.

Tries are space-intensive since each node may have up to 26 children (for the English alphabet) or more for larger character sets. This increased space requirement can be mitigated by using more space-efficient structures such as hash maps for child nodes or implementing the aforementioned compressed tries.

Tries are essential for various algorithmic problems, making them a vital tool for real-time systems needing fast and efficient string manipulations. They feature heavily in applications requiring prompt lookups and pattern matching tasks.

6.11 Applications of Trees



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Trees are a fundamental data structure in computer science and find extensive applications in various domains. Their hierarchical nature and efficient search, insert, and delete capabilities make them suitable for a wide range of tasks. This section delves into the practical implementations and advantages of using tree structures in real-world scenarios, focusing on areas such as databases, file systems, network routing, and more.

- **Database Indexing:** One of the prime applications of trees, particularly B-trees and their variants like B+ trees, is in database indexing. Databases need to perform rapid search and retrieval, insertion, and deletion operations. B-trees are balanced, maintaining sorted data and allowing for logarithmic time complexity for these operations. This balance ensures that the path from the root to any leaf node is about the same length, providing efficiency in high-volume database transactions. B+ trees enhance B-trees by storing all values at the leaf nodes and maintaining pointers to these leaf nodes, further optimizing range queries.
- **File Systems:** Modern file systems often leverage tree structures for efficient file storage and retrieval. Examples include the ext4 file system in Linux, which uses a complex tree structure known as an extent tree to manage file allocations. Hierarchical structures such as directories can also be represented using trees, simplifying navigation and management.
- Network Routing: Trees are essential in network routing algorithms. Spanning trees, for example, are utilized in network topology management to prevent loops. The Spanning Tree Protocol (STP) allows switches to communicate, ensuring a loop-free network topology by creating a spanning tree that includes all the network's bridges or switches. Additionally, IP routing uses tries (prefix trees) to store routing tables efficiently, enabling quick lookups for routing decisions.
- Syntax Tree in Compilers: Abstract syntax trees (ASTs) are used in compilers to represent the structure of program code. During the parsing phase, source code is analyzed and converted into a tree structure that reflects the hierarchical nature of the syntax. This tree is then used in the subsequent steps of compilation, such as semantic analysis and code generation. ASTs are crucial for optimizing code and error checking.
- Artificial Intelligence: In AI, particularly in decision-making algorithms and game theory, trees play a crucial role. Decision trees are used for classification and regression tasks. They split the data into branches based on feature values, helping in predictive modeling.

 Moreover, game trees are a cornerstone in designing algorithms for playing strategic games like chess, where each node represents a possible game state.
- **Data Compression:** Trees, specifically Huffman trees, are instrumental in data compression algorithms. Huffman encoding uses a binary tree to assign variable-length codes to input characters, based on their frequencies. Characters that occur more frequently are given shorter codes, which helps in reducing the overall size of the data. This method is foundational in technologies like ZIP compression and multimedia codecs.
- **Geographical Information Systems (GIS):** In GIS applications, spatial data often requires efficient access and manipulation. Quadtrees and K-D trees are used to index multi-dimensional information such as geographical coordinates. These trees decompose space into manageable sections, making operations like range queries and nearest neighbor searches more efficient.
- **Expression Parsing in Calculators:** Evaluations of mathematical expressions in calculators and other arithmetic processing tools often make use of expression trees. Each node in the tree represents an operator, and the children nodes represent the operands. This structure



allows for the implementation of various order traversals like infix, prefix, and postfix, which are essential in evaluating the expressions properly.

- **Concurrent Programming:** In concurrent or multi-threaded programming, trees like concurrent hash tries are used to manage shared data structures efficiently. These trees allow multiple threads to perform operations without significant locking, thereby improving performance and scalability.
- **Genealogy and Historical Research:** Tree structures are naturally suited to represent genealogical data, such as family trees or lineage charts. They can depict ancestral connections and descendants in a clear, hierarchical manner, making it easier to track lineage and heritage.

Through these applications, it is evident that tree structures are not only versatile but also indispensable across various technological and research domains. Their ability to provide structured, efficient, and scalable solutions makes them a cornerstone of modern computing and data management.

6.12 Performance Considerations in Trees

Analyzing the performance of tree data structures requires examining various factors such as time complexity, space complexity, and balancing criteria. Tree-based algorithms' performance is contingent on the type of tree and the specific operations being performed.

Time complexity for common operations such as insertion, deletion, and search is typically discussed. For a binary search tree (BST), performance is inherently linked to the tree's height. The time complexity for basic operations in a BST is O(h) where h is the height of the tree. In the worst-case scenario, the height of a BST can become O(n), where n is the number of nodes, leading to linear time complexity. This occurs when nodes are inserted in a sorted order, degenerating the BST into a linked list.

Balanced trees such as AVL trees and Red-Black trees aim to keep the height of the tree approximately logarithmic with respect to the number of nodes, $h = O(\log n)$. This logarithmic height ensures logarithmic time complexity, $O(\log n)$, for insertion, deletion, and search operations, thus significantly enhancing performance for large datasets.

```
class Node:
    def__init_(self, key):
        self.key = key
        self.left = None
        self.right = None
        self.height = 1

class AVLTree:
    def insert(self, root, key):
        # Perform the normal BST rotation
        if not root: return
            Node(key)
        elif key < root.key:</pre>
```

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```
root.left = self.insert(root.left, key)
   else:
      root.right = self.insert(root.right, key)
   # Update the height of the ancestor node
   root.height = 1 + max(self.getHeight(root.left), self.getHeight(root.right))
   # Get the balance factor
   balance = self.getBalance(root)
   # If the node is unbalanced, then try the 4 cases
   # Left Left Case
   if balance > 1 and key < root.left.key:
      return self.rightRotate(root)
   # Right Right Case
   if balance < -1 and key > root.right.key:
      return self.leftRotate(root)
   # Left Right Case
   if balance > 1 and key > root.left.key:
      root.left = self.leftRotate(root.left)
      return self.rightRotate(root)
   # Right Left Case
   if balance < -1 and key < root.right.key:
      root.right = self.rightRotate(root.right)
      return self.leftRotate(root)
   return root
def leftRotate(self, z):
   y = z.right
   T2 = y.left
   y.left = z
   z.right = T2
   z.height = 1 + max(self.getHeight(z.left), self.getHeight(z.right))
   y.height = 1 + max(self.getHeight(y.left), self.getHeight(y.right))
   return y
def rightRotate(self, z):
   y = z.left
   T3 = y.right
   y.right = z
   z.left = T3
```



```
z.height = 1 + max(self.getHeight(z.left), self.getHeight(z.right))
y.height = 1 + max(self.getHeight(y.left), self.getHeight(y.right))
return y

def getHeight(self, root):
   if not root:
     return 0 return
root.height

def getBalance(self, root):
   if not root:
     return 0
return self.getHeight(root.left) - self.getHeight(root.right)
```

The balance of AVL trees ensures that the performance remains efficient, even in the worst-case scenarios. Similarly, B-trees and heaps are designed to maintain balanced structures to optimize performance. B-trees are especially beneficial in scenarios involving databases and file systems, as they minimize disk reads, which are significantly slower compared to in-memory operations. B-trees maintain balance by ensuring that all leaf nodes are at the same level and by distributing keys across multiple child nodes to maintain the height as $O(\log n)$.

The heap data structure, particularly binary heaps, provides efficient support for priority queue operations. In binary heaps, insertion, and deletion operations maintain the structure's properties, resulting in $O(\log n)$ time complexity. Min-heaps and max-heaps are fundamental in applications requiring efficient retrieval of the minimum and maximum elements, respectively.

```
class MinHeap:
   def___init_(self):
      self.heap = []
   def insert(self, key):
      self.heap.append(key) i
      = len(self.heap) - 1
      while i > 0 and self.heap[i] < self.heap[(i - 1) // 2]:
          self.heap[i], self.heap[(i - 1) // 2] = self.heap[(i - 1) // 2], self.heap[i] i = self.heap[i]
          (i - 1) // 2
   def heapify(self, i):
      smallest = i
      left = 2 * i + 1
      right = 2 * i + 2
      if left < len(self.heap) and self.heap[left] < self.heap[smallest]:</pre>
          smallest = left
      if right < len(self.heap) and self.heap[right] < self.heap[smallest]:</pre>
          smallest = right
      if smallest != i:
```



self.heap[i], self.heap[smallest] = self.heap[smallest], self.heap[i]
self.heapify(smallest)

While analyzing space complexity, we consider both the auxiliary space required by the algorithms and the extra space consumed by maintaining tree properties. Trees naturally use O(n) space to store n nodes. Self-balancing trees, like AVL trees, require additional space to store height or balance information at each node, though this is a linear addition in terms of complexity. B-trees, particularly in database applications, are designed to reduce expensive disk I/O by ensuring that nodes are densely packed and thus minimizing the height of the tree.

Performance considerations extend to traversal methods as well. In-order, pre-order, and post-order tree traversals have time complexity O(n) as each node is visited exactly once. Though these traversal methods are efficient, choosing the appropriate one can impact the overall performance depending on the specific algorithm requirements. Breadth-first traversal, typically implemented using a queue, may have higher space complexity compared to depth-first traversals due to additional storage requirements.

The performance of trees is greatly impacted by the requirement for maintenance operations to ensure the trees remain balanced. While these balancing operations might introduce overhead, the performance improvements for large datasets can be significant. Consequently, understanding the performance characteristics and trade-offs of various tree structures is critical for effective data structure selection in software development.



Chapter 7 Graphs

This chapter delves into graph data structures, covering fundamental concepts, terminology, and types of graphs. It explains various graph representations and traversal methods, including Depth-First Search (DFS) and Breadth-First Search (BFS). The chapter also addresses shortest path algorithms, minimum spanning trees, graph coloring, and practical applications, along with performance considerations to provide a comprehensive understanding of graphs.

7.1 Introduction to Graphs

A graph G is an abstract data structure that consists of a set of vertices V (or nodes) and a set of edges E connecting pairs of vertices. Formally, we can represent a graph as G = (V,E). Each edge $\{u,v\} \subseteq E$ is a connection between two vertices u and v in V. Graphs are pivotal in modeling various real-world systems such as social networks, transportation networks, communication networks, and many others due to their ability to represent pairwise relationships.

The two primary components of a graph are:

- •Vertices (or Nodes): These are the fundamental units in the graph. In diagrams, vertices are often depicted as dots or circles.
- •Edges: These represent the connections between vertices. Edges can be directed or undirected, weighted or unweighted. They are commonly drawn as lines or arrows between vertices

Graphs can be categorized based on various attributes such as directionality, weight, and cyclicity, among others. Understanding these categories helps in selecting the appropriate algorithms and data structures for solving specific problems.

Consider the following Python code that defines a simple graph using an adjacency list:

```
class Graph:
    def___init__(self):
        self.adjacency_list = {}

def add_vertex(self, vertex):
    if vertex not in self.adjacency_list:
        self.adjacency_list[vertex] = []

def add_edge(self, vertex1, vertex2):
    if vertex1 in self.adjacency_list and vertex2 in self.adjacency_list:
        self.adjacency_list[vertex1].append(vertex2)
```

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Expressed in an adjacency list representation, the graph class allows adding vertices and edges, which are pivotal operations in graph processing. The output of the above code is demonstrative of the adjacency list of the graph:

```
{'A': ['B'], 'B': ['A']}
```

Graphs can be directed or undirected:

- •Directed Graphs (Digraphs): Each edge has a direction, pointing from one vertex to another. Formally, an edge is an ordered pair (u,v). These are useful in scenarios like website links or road maps where the direction of travel matters.
- •Undirected Graphs: Each edge is a bidirectional connection between two vertices. Formally, an edge is an unordered pair $\{u,v\}$. These are often used to model symmetric relationships, such as friendships in a social network.

Additionally, graphs can be classified based on whether they contain weights on their edges:

- •Weighted Graphs: Each edge has a numerical value associated with it, often referred to as the weight. Weights can represent costs, distances, or any quantitative relationships. Algorithms like Dijkstra's and the Bellman-Ford algorithm are typically used to find shortest paths in weighted graphs.
- •Unweighted Graphs: Edges do not have any weights. In these graphs, algorithms like BFS and DFS are often utilized for traversal and connectivity checks.

Consider the following Python code snippet that extends the graph definition to handle weighted edges:

```
class WeightedGraph:
    def ___init_(self):
        self.adjacency_list = {}

    def add_vertex(self, vertex):
        if vertex not in self.adjacency list:
```

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```
self.adjacency_list[vertex] = []

def add_edge(self, vertex1, vertex2, weight):
    if vertex1 in self.adjacency_list and vertex2 in self.adjacency_list:
        self.adjacency_list[vertex1].append((vertex2, weight))
        # For an undirected graph, add the opposite edge with the same weight
        self.adjacency_list[vertex2].append((vertex1, weight))

def___str_(self):
    return str(self.adjacency_list)

# Example Usage:
graph = WeightedGraph()
graph.add_vertex('A')
graph.add_vertex('B')
graph.add_edge('A', 'B', 3)
print(graph)
```

The output of the above code, representing a weighted graph in adjacency list format, is shown below:

```
\{'A': [('B', 3)], 'B': [('A', 3)]\}
```

Graph traversal, the process of visiting all the vertices in a graph, is a foundational operation. This concept is critical for searching algorithms and understanding graph connectivity. Typical traversal techniques include depth-first search (DFS) and breadth-first search (BFS), each having distinct properties and suitable for different types of problems.

Graphs are frequently utilized to solve many computational problems, such as finding the shortest path between nodes, detecting cycles, and performing searches. Their versatile nature means they can be represented in various ways including adjacency matrices, adjacency lists, and edge lists. Each representation has its own trade-offs regarding space complexity and the ease of implementing graph algorithms.

When faced with specific graph-based problems, the choice of graph representation and the traversal technique has a significant impact on the efficiency and feasibility of the solution. Understanding the foundational concepts of graphs is crucial for any computer scientist or engineer aiming to employ these data structures for practical applications.

7.2 Graph Terminology

Understanding graph terminology is crucial to grasping the diverse and intricate world of graph data structures. The following terminologies form the foundation for interpreting and working with graphs effectively.



Graph (G): A graph G consists of two finite sets: a non-empty set of vertices V(G) and a set of edges E(G). Each edge is defined as an unordered pair of vertices. Formally, G = (V, E).

Vertex (Node): A vertex, also referred to as a node, is a fundamental unit from which graphs are formed. The set of vertices in a graph G is usually denoted by V(G). Vertices are typically represented by points or circles.

Edge: An edge is a connection between a pair of vertices. The set of edges is denoted by E(G). Each edge in an undirected graph is represented by a tuple (u,v), where u and v are vertices belonging to the vertex set V(G). In directed graphs, edges have directions and are represented by an ordered pair (u,v) indicating an edge from vertex u to vertex v.

Path: A path in a graph is a finite or infinite sequence of edges which connect a sequence of vertices. No vertex in the path is visited more than once. For instance, $P = (v_1, e_1, v_2, e_2, ..., v_{n-1}, e_{n-1}, v_n)$ is a path from vertex v_1 to vertex v_n .

Cycle: A cycle is a path where the start and end vertices are the same, and no other vertex is repeated. Formally, a cycle is a path $\{v_0, v_1, ..., v_{n-1}, v_0\}$ with $v_0 = v_n$ and $v_i \neq v_j$ for all $0 \le i < j < n$.

Degree of a Vertex: The degree of a vertex is the number of edges incident to the vertex. In a directed graph, the in-degree of a vertex is the number of incoming edges, and the out-degree is the number of outgoing edges.

Subgraph: A subgraph is a graph formed from a subset of the vertices and edges of another graph. Formally, $H = (V_H, E_H)$ is a subgraph of G = (V, E) if $V_H \subseteq V$ and $E_H \subseteq E$.

Connected Graph: A graph is connected if there is a path between every pair of vertices. If no such path exists, the graph is disconnected. In a directed graph, the term *strongly connected* is used to indicate that every vertex is reachable from every other vertex.

Component: A connected component is a maximal connected subgraph of *G*. Each vertex in the graph belongs to exactly one connected component.

Adjacent: Two vertices u and v are adjacent if there is an edge (u,v) in the graph. Similarly, two edges are adjacent if they share a common vertex.

Isomorphism: Two graphs G_1 and G_2 are isomorphic if there is a one-to-one correspondence between their vertex sets and their edge sets such that adjacency is preserved. Isomorphism implies that the two graphs have the same structure but may have different vertex labels.



Weighted Graph: In a weighted graph, each edge has an associated numerical value called a weight. The weight often represents a cost, distance, or time associated with traversing the edge. Formally, a weighted graph is a graph G = (V, E, W) with an additional function $W : E \rightarrow \mathbb{R}$ mapping edges to real numbers.

Directed and Undirected Graphs: In an undirected graph, edges have no direction, represented as unordered pairs (u,v). In a directed graph or digraph, edges have a direction, represented as ordered pairs (u,v).

Complete Graph: A complete graph is one in which every pair of distinct vertices is connected by a unique edge. A complete graph with n vertices is denoted K_n .

Bipartite Graph: A graph is bipartite if its vertex set can be divided into two disjoint sets U and V such that every edge connects a vertex in U to one in V. Formally, a graph G = (V,E) is bipartite if V can be partitioned into two sets U and V, with $U \cap V = \emptyset$ and $U \cup V = V$, such that every edge e = (u,v) satisfies $u \in U$ and $v \in V$.

Planar Graph: A graph is planar if it can be embedded in the plane, i.e., it can be drawn on a plane without edges crossing each other.

Tree and Forest: A tree is an acyclic connected graph. A forest is a disjoint set of trees. A tree with n vertices has n-1 edges.

The detailed understanding of these terminologies provides a robust foundation to navigate through subsequent concepts and algorithms related to graph data structures. Knowing these terms helps in devising more efficient solutions to graph-related problems and enables effective communication of these solutions.

7.3 Types of Graphs

Graphs can be classified into various types based on their structure, direction, and the nature of the connections between their nodes. Understanding these types is crucial for correctly applying graph algorithms and optimally solving problems that involve graph data structures. In this section, we explore several fundamental graph types in detail.

Undirected Graphs:

An undirected graph is a type of graph in which the edges between nodes have no direction. This means that if there is an edge between nodes u and v, you can traverse it from u to v and from v to u with no distinction. Formally, an undirected graph G can be denoted as G = (V,E), where V is the set of vertices and E is the set of edges, where each edge is an unordered pair of vertices.

For example, consider an undirected graph:

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```
graph = {
    'A': {'B', 'C'},
    'B': {'A', 'D', 'E'},
    'C': {'A', 'F'},
    'D': {'B'},
    'E': {'B', 'F'},
    'F': {'C', 'E'}
}
```

The adjacency list above represents an undirected graph, where each vertex points to a set of vertices it is connected to by an edge. If we choose vertex 'A', it is connected to vertices 'B' and 'C', and so forth.

Directed Graphs (Digraphs):

In contrast to undirected graphs, directed graphs consist of edges with a specific direction. In a directed graph, an edge (u,v) is an ordered pair, implying a direction from node u to node v. Directed graphs are formally defined as G = (V,E), where V is the set of vertices and E is the set of ordered pairs of vertices.

Consider the following directed graph:

```
digraph = {
    'A': {'B', 'C'},
    'B': {'D', 'E'},
    'C': {'F'},
    'D': {},
    'E': {'F'},
    'F': {}
```

This adjacency list representation indicates a directed graph where, for instance, 'A' has directed edges to 'B' and 'C', but not the reverse.

Weighted Graphs:

Weighted graphs are graphs where edges have associated weights representing the cost, distance, or any quantifiable measure assigned to traversing from one vertex to another. Weighted graphs can be either directed or undirected.

An example of an undirected weighted graph is:

```
weighted_graph = {
  'A': {'B': 4, 'C': 2},
  'B': {'A': 4, 'D': 5, 'E': 10},
  'C': {'A': 2, 'F': 3},
```

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```
'D': {'B': 5},
'E': {'B': 10, 'F': 1},
'F': {'C': 3, 'E': 1}
```

In this graph, each entry in the adjacency list includes a dictionary mapping neighboring vertices to their respective weights.

Cyclic and Acyclic Graphs:

Graphs can be classified as cyclic or acyclic based on the presence of cycles. A *cycle* in a graph is a path that starts and ends at the same vertex without traversing any edge more than once.

- A cyclic graph contains at least one cycle. - An acyclic graph has no cycles.

Additionally, directed graphs can be specifically classified into **Directed Acyclic Graphs** (**DAGs**), which play a crucial role in several algorithms, such as topological sorting and various scheduling problems.

Example of a directed acyclic graph:

```
dag = {
    'A': {'B', 'C'},
    'B': {'D'},
    'C': {'E'},
    'D': {'F'},
    'E': {'F'},
    'F': {}
```

In this representation, there are no cycles, ensuring that it is a DAG.

Connected and Disconnected Graphs:

A graph is said to be connected if there is a path between any two vertices. Conversely, a graph is disconnected if at least two vertices lack a path connecting them.

Example of a connected undirected graph:

```
connected_graph = {
   'A': {'B', 'C'},
   'B': {'A', 'D', 'E'},
   'C': {'A', 'F'},
   'D': {'B'},
   'E': {'B', 'F'},
```

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```
'F': {'C', 'E'}
```

Example of a disconnected undirected graph:

```
disconnected_graph = {
    'A': {'B'},
    'B': {'A'},
    'C': {'D'},
    'D': {'C'}
}
```

Bipartite Graphs:

A bipartite graph is one in which the set of vertices can be divided into two disjoint sets U and V such that every edge connects a vertex in U to one in V. Bipartite graphs are particularly useful in modeling relationships between two different classes of objects, such as matching problems.

A simple bipartite graph representation:

```
bipartite_graph = {
  'U1': {'V1', 'V2'},
  'U2': {'V2'},
  'U3': {'V3', 'V4'},
  'V1': {'U1'},
  'V2': {'U1', 'U2'},
  'V3': {'U3'},
  'V4': {'U3'}
}
```

Complete Graphs:

A romplete graph is one in which every pair of distinct vertices is connected by a unique edge. In a complete graph with n vertices, there are $\frac{1}{2}$ edges for undirected graphs and n(n-1) edges for directed graphs.

For example, a complete graph K_4 has four vertices:

```
complete_graph = {
  'A': {'B', 'C', 'D'},
  'B': {'A', 'C', 'D'},
  'C': {'A', 'B', 'D'},
  'D': {'A', 'B', 'C'}
}
```



In this graph, each node is connected to every other node exactly once.

Sparse and Dense Graphs:

Graphs are also categorized as sparse or dense based on the number of edges relative to the number of vertices. A **sparse graph** has relatively few edges, often much less than the maximum possible number of edges, whereas a **dense graph** has a number of edges close to the maximum possible number of edges.

The differentiation between these types is important as it often dictates the choice of storage representation and algorithm efficiency.

Expanding our understanding of these various graph types provides a solid foundation for exploring graph algorithms and applications that rely on these structural properties.

7.4 Graph Representation

In the study of graphs, how we represent them determines the efficiency of various graph algorithms. The fundamental representations of graphs are the adjacency matrix, adjacency list, and edge list. Each representation has its advantages and trade-offs concerning space complexity and performance of specific operations, such as insertion, deletion, and traversal. Understanding these representations is crucial for selecting the appropriate one for a given application.

Adjacency Matrix:

An adjacency matrix is a square matrix used to represent a finite graph. The elements of the matrix indicate whether pairs of vertices are adjacent or not in the graph. Each element a_{ij} of the matrix is set to one if there is an edge between vertex v_i and vertex v_i ; otherwise, it is zero.

Consider a graph G = (V,E), where V is a set of vertices $\{v_1, v_2, ..., v_n\}$, and E is a set of edges. The adjacency matrix A for G is an $n \times n$ matrix $A = [a_{ij}]$, where:

$$a_{ij} = \begin{cases} 1 & \text{if there is an edge from } v_i \text{ to } v_j \\ 0 & \text{otherwise} \end{cases}$$

For example, let us represent a directed graph using an adjacency matrix in Python:

```
class GraphAdjMatrix:
    def___init_(self, num_vertices):
        self.num_vertices = num_vertices
        self.adj_matrix = [[0] * num_vertices for _ in range(num_vertices)]
```



```
def add_edge(self, src, dest):
    self.adj_matrix[src][dest] = 1

def remove_edge(self, src, dest):
    self.adj_matrix[src][dest] = 0

def display(self):
    for row in self.adj_matrix:
        print(row)

# Example usage:
graph = GraphAdjMatrix(5)
graph.add_edge(0, 1)
graph.add_edge(0, 2)
graph.add_edge(1, 2)
graph.add_edge(2, 0)
graph.add_edge(2, 0)
graph.add_edge(2, 3)
graph.display()
```

The output of the display() method for the above code would be:

```
[0, 1, 1, 0, 0]
[0, 0, 1, 0, 0]
[1, 0, 0, 1, 0]
[0, 0, 0, 0, 0]
[0, 0, 0, 0, 0]
```

Adjacency List:

An adjacency list is a collection of lists used to represent a finite graph. Each list corresponds to a vertex in the graph and contains a list of that vertex's adjacent vertices. This representation is more space-efficient for sparse graphs.

For a graph G = (V,E), the adjacency list consists of an array of lists. The array has one list for each vertex, and the list for vertex v_i contains all the vertices adjacent to v_i .

Consider a Python implementation of an adjacency list:

```
class GraphAdjList:
    def ___init_(self):
        self.graph = {}

    def add_edge(self, src, dest):
        if src not in self.graph:
            self.graph[src] = []
```

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```
self.graph[src].append(dest)

def display(self):
    for key in self.graph:
        print(f"{key} -> {self.graph[key]}")

# Example usage:
graph = GraphAdjList()
graph.add_edge(0, 1)
graph.add_edge(0, 2)
graph.add_edge(1, 2)
graph.add_edge(1, 2)
graph.add_edge(2, 0)
graph.add_edge(2, 3)
graph.display()
```

The output of the display() method for the above code would be:

```
0 -> [1, 2]
1 -> [2]
2 -> [0, 3]
```

Edge List:

An edge list is a collection of edges, which are represented as pairs of vertices. This representation is simple and works well for algorithms that process edges rather than adjacency information.

For a graph G = (V,E), the edge list consists of tuples (v_i, v_j) where each tuple represents an edge from vertex v_i to vertex v_i .

A Python implementation of an edge list can be done as follows:

```
class GraphEdgeList:
    def ___init__(self):
        self.edges = []

    def add_edge(self, src, dest):
        self.edges.append((src, dest))

    def display(self):
        for edge in self.edges:
            print(edge)

# Example usage:
graph = GraphEdgeList()
```

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```
graph.add_edge(0, 1)
graph.add_edge(0, 2)
graph.add_edge(1, 2)
graph.add_edge(2, 0)
graph.add_edge(2, 3)
graph.display()
```

The output of the display () method for the above code is:

- (0, 1)
- (0, 2)
- (1, 2)
- (2, 0)
- (2, 3)

These three representations — adjacency matrix, adjacency list, and edge list — each offer different strengths suited to different types of graph operations and applications. Choosing the right representation depends on particular requirements such as space complexity, the density of the graph, and the operations to be performed.

7.5 Graph Traversal Methods

Graph traversal methods are techniques used to visit all the vertices or nodes in a graph systematically. These methods are fundamental in many graph-related algorithms and applications, such as searching for a specific node, finding the shortest path between nodes, or checking if a path exists between nodes.

Traversal Strategies

Graph traversals can generally be classified into two broad categories: Depth-First Search (DFS) and Breadth-First Search (BFS). Each traversal method has its unique characteristics and is suitable for different types of problems.

Depth-First Search (DFS)

Depth-First Search (DFS) explores a graph by starting at the root node and diving as deep as possible along each branch before backtracking. It uses a stack data structure either explicitly or through recursion. Here is a Python implementation of DFS using recursion:

```
def dfs(graph, start, visited=None):
    if visited is None:
        visited = set()
    visited.add(start)

    print(start)
    for next_node in graph[start] - visited:
```

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The graph is represented as an adjacency list, which is a dictionary of sets. The DFS function takes a starting node and the graph, and it prints the visited nodes in the order they are visited. The main qualities of DFS are:

- **Completeness**: Only guaranteed if the graph is finite. - **Time Complexity**: O(|V| + |E|) where |V| is the number of vertices and |E| is the number of edges. - **Space Complexity**: O(|V|) due to the recursion stack.

Breadth-First Search (BFS)

Breadth-First Search (BFS) explores a graph level by level starting from the source node. It uses a queue to keep track of the next node to visit. Here is a Python implementation of BFS:

```
from collections import deque

def bfs(graph, start):
    visited = set()
    queue = deque([start])
    visited.add(start)

while queue:
    vertex = queue.popleft()
    print(vertex)

for neighbor in graph[vertex]:
    if neighbor not in visited:
        visited.add(neighbor)
        queue.append(neighbor)

# Example graph as an adjacency list
```



BFS iterates through the graph by processing all nodes at the present depth level before moving on to nodes at the next depth level. BFS characteristics include:

Completeness: Guaranteed if the graph is finite. - **Time Complexity**: O(|V| + |E|) similar to DFS. - **Space Complexity**: O(|V|) required for the queue to store the nodes at the current depth level.

Comparison of DFS and BFS

When choosing between DFS and BFS, consider their properties relevant to the specific problem at hand:

- Path Finding: BFS is typically used for the shortest path in an unweighted graph, as it systematically explores nodes layer by layer. - Memory Usage: DFS generally has lower memory requirements in sparse graphs, especially if depth is considerably larger than breadth. - Completeness and Optimality: BFS guarantees completeness and can find the shortest path in unweighted graphs, whereas DFS does not guarantee these properties in general.

Applications of Graph Traversals

Graph traversal methods are used in various applications, such as:

- Web Crawling: Uses either DFS or BFS to explore hyperlinks on the web. - Network Broadcasting: BFS can be used to propagate information efficiently. - Pathfinding Problems: DFS and BFS are both fundamental for solving puzzles or games (e.g., mazes). - Checking Graph Properties: Finding connected components, detecting cycles, and more.

These traversal methods form the basis for advanced graph algorithms and are essential for comprehensively understanding the structure and properties of graphs.

7.6 Depth-First Search (DFS)

Depth-First Search (DFS) is an algorithm that explores a graph by starting at a selected node and traversing as far as possible along each branch before backtracking. This approach is critical for tasks such as connectivity testing, pathfinding, and discovering cycles within

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graphs. DFS can be implemented using either a recursive method or an iterative method with an explicit stack.

Recursive Implementation:

The recursive implementation of DFS utilizes the system's call stack to keep track of nodes yet to be fully explored. Below is a Python function demonstrating the recursive DFS algorithm:

```
def dfs_recursive(graph, start, visited=None):
    if visited is None:
        visited = set()
    visited.add(start)
    print(start)
    for next_node in graph[start] - visited:
        dfs_recursive(graph, next_node, visited)
    return visited
```

In this implementation, the function dfs_recursive takes a graph, a start node, and an optional visited set to keep track of visited nodes. The function marks the start node as visited and recursively explores adjacent nodes.

To illustrate:

The DFS algorithm starts at node 'A', proceeds to 'B', then 'D', and continues with this depth-wise manner until all nodes reachable from 'A' are visited.

Iterative Implementation:



The iterative approach employs an explicit stack to manage the nodes to be visited. Here is a Python function demonstrating the iterative DFS algorithm:

```
def dfs_iterative(graph, start):
    visited = set()
    stack = [start]
    while stack:
        node = stack.pop()
        if node not in visited:
            visited.add(node)
            print(node)
            stack.extend(graph[node] - visited)
    return visited
```

This function initializes a stack with the start node and iteratively explores each node by popping it from the stack, visiting it, and pushing its unvisited adjacent nodes onto the stack.

An example execution for the aforementioned graph:

```
visited_nodes_iterative = dfs_iterative(graph, 'A')
A
C
F
E
B
D
```

Complexity Analysis:

The DFS algorithm has a time complexity of O(V + E), where V is the number of vertices and E is the number of edges in the graph. This results from the fact that each vertex and edge is processed once. The space complexity is O(V) due to the storage requirements for the visited set and the stack (or the call stack in the recursive approach).

Applications:

DFS has numerous applications including:

- •Pathfinding: Identifying a path between two nodes.
- •Cycle Detection: Determining if a graph contains a cycle.
- •Topological Sorting: Arranging vertices in a directed acyclic graph.
- •Connected Components: Discovering all connected components within a graph.



DFS is a fundamental graph traversal algorithm integral to the understanding and efficient solving of several graph-related problems. It provides the foundational basis for more advanced algorithms like those used in network flow analysis, game theory, and artificial intelligence.

7.7 Breadth-First Search (BFS)

Breadth-First Search (BFS) is an algorithm for traversing or searching tree or graph data structures. It starts at the tree root (or an arbitrary node of a graph, sometimes referred to as the 'source node') and explores the neighbor nodes at the present depth prior to moving on to nodes at the next depth level. BFS is a cornerstone algorithm in graph theory, enabling various applications such as finding the shortest path in an unweighted graph or discovering connected components.

The primary data structure used in BFS is the queue, which adheres to the First In, First Out (FIFO) principle. Nodes are enqueued when they are encountered and dequeued when they are fully explored. BFS can be implemented iteratively using a queue.

To formalize BFS, we use the following steps:

1. **Initialization**: Begin by enqueueing the root node and marking it as visited. 2. **Processing**: Dequeue a node and visit all its unvisited neighbors, marking them visited and enqueueing them. 3. **Completion**: Repeat the process until the queue is empty.

Consider a graph G = (V,E) where V is the set of vertices and E the set of edges. Let $S \subseteq V$ be the source vertex from which BFS starts. We can represent it algorithmically as follows:

```
from collections import deque

def bfs(graph, start):
    visited = set()
    queue = deque([start])
    visited.add(start)

while queue:
    vertex = queue.popleft()
    print(vertex) # Process the node here (e.g., print or store it)

for neighbor in graph[vertex]:
    if neighbor not in visited:
        visited.add(neighbor)
        queue.append(neighbor)
```

BFS Illustrative Example



Consider the graph representation:

This graph can be represented as an adjacency list:

```
graph = {
    'A': ['B', 'D'],
    'B': ['A', 'C', 'E'],
    'C': ['B', 'F'],
    'D': ['A', 'E'],
    'E': ['B', 'D', 'F'],
    'F': ['C', 'E']
}
bfs(graph, 'A')
```

Running the BFS algorithm from node 'A' would yield the following traversal order:

A B D C E

BFS Time Complexity

The time complexity of BFS depends on the way the graph is represented:

```
1. **Adjacency List**: O(V+E). 2. **Adjacency Matrix**: O(V^2).
```

The adjacency list representation is typically more efficient for sparse graphs, while adjacency matrix is practical for dense graphs.

BFS Applications

- 1. **Shortest Path in Unweighted Graphs**: BFS can be used to find the shortest path from a source node to a target node in an unweighted graph. This is particularly useful in networking, where each edge can be seen as a connection with equal weight.
- 2. **Connected Components**: BFS can discover all nodes in a graph that are reachable from a given start node, identifying connected components in undirected graphs.



3. **Cycle Detection in Undirected Graphs**: By maintaining a parent array, BFS can detect cycles in undirected graphs. If a node is discovered that is not the parent of the current node but has been visited earlier, a cycle exists.

Implementing BFS for Path Finding

To find the shortest path in an unweighted graph using BFS, modify the BFS to keep track of the predecessors of each node. Here is the modification:

```
def bfs_shortest_path(graph, start, goal):
    queue = deque([(start, [start])])

while queue:
    (vertex, path) = queue.popleft()
    for next in set(graph[vertex]) - set(path):
        if next == goal:
            return path + [next]
        else:
            queue.append((next, path + [next]))
    return None
```

Given a start node 'A' and a goal node 'F', the function would return the shortest path: ['A', 'B', 'E', 'F']

By logically extending the simple traversal mechanism to path discovery, BFS can be effectively utilized in real-world scenarios where the shortest route is paramount, such as in network routing protocols, urban planning, and social network analysis.

7.8 Shortest Path Algorithms

Shortest path algorithms are fundamental in graph theory, solving a critical problem of finding the minimum path between vertices in a graph. These algorithms are vital in various applications, including routing in networks, urban planning, and many optimization problems. This section discusses several essential shortest path algorithms and their intricacies, with a focus on their implementations and use cases.

Dijkstra's Algorithm

Dijkstra's Algorithm is one of the most well-known algorithms for finding the shortest path from a source vertex to all other vertices in a weighted graph. The graph must have nonnegative edge weights. Dijkstra's Algorithm uses a greedy approach to progressively determine the shortest path to each vertex.

Procedure:



- •Initialize the distance to the source node as 0 and the distance to all other nodes as infinity.
- •Set the source node as the current node and mark it as visited.
- •For the current node, update the distances to its adjacent nodes. For any unvisited adjacent node, if the distance from the source to this node through the current node is less than the previously recorded distance, update the distance.
- •Once all adjacent nodes are processed, mark the current node as visited. Select the next node with the smallest distance as the new current node.
- •Repeat steps 3-4 until all nodes are visited.

The implementation of Dijkstra's Algorithm can be efficient using a priority queue (minheap).

Output Example:

```
{
    'A': 0,
    'B': 7,
    'C': 9,
    'D': 20,
    'E': 20,
    'F': 11
}
```



Bellman-Ford Algorithm

The Bellman-Ford Algorithm handles graphs with negative edge weights, unlike Dijkstra's Algorithm. It can detect negative weight cycles, making it more versatile, albeit less efficient for graphs without negative weights.

Procedure:

- •Initialize the distance to the source node as 0 and the distance to all other nodes as infinity.
- •For each edge, update the distance if the new path is shorter than the known path. Repeat this process for |V| 1 times, where V is the number of vertices.
- •Check for negative-weight cycles by verifying that no distances can be further updated. If any distance can be updated, a negative-weight cycle exists.

```
def bellman_ford(graph, start_vertex):
    D = {v: float('infinity') for v in graph}
    D[start_vertex] = 0

for _ in range(len(graph) - 1):
    for vertex in graph:
        for neighbor, weight in graph[vertex].items():
            if D[vertex] + weight < D[neighbor]:
                D[neighbor] = D[vertex] + weight

for vertex in graph:
    for neighbor, weight in graph[vertex].items():
        if D[vertex] + weight < D[neighbor]:
            raise ValueError("Graph contains a negative-weight cycle")

return D</pre>
```

Output Example:

```
{
    'A': 0,
    'B': 2,
    'C': 6,
    'D': 4,
    'E': 6
}
```

Floyd-Warshall Algorithm



The Floyd-Warshall Algorithm is an all-pairs shortest path algorithm, meaning it finds the shortest paths between all pairs of vertices in a graph. It is suitable for dense graphs due to its O (V3) time complexity.

Procedure:

- •Initialize a matrix D where D[i][j] represents the edge weight from vertex i to vertex j. Set the distance from a vertex to itself as 0 and to others as infinity if there is no direct edge.
- •For each vertex k, check if a path through k is shorter than the known path from i to j. Update the matrix accordingly.
- •After V iterations, the matrix D will reflect the shortest paths between all vertex pairs.

```
def floyd_warshall(graph):
    V = len(graph)
    distance = list(map(lambda i: list(map(lambda j: j, i)), graph))

for k in range(V):
    for i in range(V):
        for j in range(V):
            distance[i][j] = min(distance[i][j], distance[i][k] + distance[k][j])

return distance
```

Output Example:

```
[
[0, 3, 8, inf, -4],
[inf, 0, inf, 1, 7],
[inf, 4, 0, inf, inf],
[2, inf, -5, 0, inf],
[inf, inf, inf, 6, 0]
]
```

These algorithms are critical for solving various real-world problems, providing a toolbox for efficient pathfinding and optimization tasks in weighted graphs. Their suitability varies based on the specific graph properties and application requirements.

7.9 Minimum Spanning Tree

A *Minimum Spanning Tree (MST)* is a subset of the edges of a connected, undirected graph which connects all the vertices together, without any cycles and with the minimum possible total edge weight. In other words, it is a spanning tree whose sum of edge weights is as

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small as possible. This concept is crucial in numerous real-world applications, such as designing networks (telecommunications, computer, road) and clustering algorithms in machine learning.

Let G = (V,E) be an undirected graph where V represents the set of vertices and E represents the set of edges. Each edge $(u,v) \in E$ has an associated weight w(u,v). The goal is to find a subset of edges $E' \subseteq E$ such that the graph (V,E') forms a tree and $\sum_{(u,v) \in E'} w(u,v)$ is minimized.

Properties of MST:

- •The MST contains exactly |V|-1 edges, where |V| is the number of vertices in the graph.
- •It connects all vertices.
- •It does not contain any cycle.
- •The total weight is minimized.

Algorithms to Find Minimum Spanning Tree:

Kruskal's Algorithm

Kruskal's algorithm is a greedy algorithm that finds an MST by considering the edges in ascending order of their weight and adding each edge to the MST if it does not form a cycle with the already included edges. The algorithm uses a disjoint-set data structure to efficiently manage and merge the different components of the MST.

```
class Graph:
    def __init_(self, vertices):
        self.V = vertices
        self.graph = []

    def addEdge(self, u, v, w):
        self.graph.append([u, v, w])

    def find(self, parent, i):
        if parent[i] == i:
            return i
        return self.find(parent, parent[i])

    def union(self, parent, rank, x, y):
        xroot = self.find(parent, x) yroot
        = self.find(parent, y)

    if rank[xroot] < rank[yroot]:</pre>
```



```
parent[xroot] = yroot
   elif rank[xroot] > rank[yroot]:
      parent[yroot] = xroot
   else:
      parent[yroot] = xroot
      rank[xroot] += 1
def KruskalMST(self):
   result = []
   i = 0
   e = 0
   self.graph = sorted(self.graph, key=lambda item: item[2])
   parent = []
   rank = []
   for node in range(self.V):
      parent.append(node)
      rank.append(0)
   while e < self.V - 1:
      u, v, w = self.graph[i]
      i += 1
      x = self.find(parent, u)
      y = self.find(parent, v)
      if x != y:
         e += 1
         result.append([u, v, w])
         self.union(parent, rank, x, y)
   for u, v, weight in result:
      print(f"{u} -- {v} == {weight}")
```

Prim's Algorithm

Prim's algorithm is another greedy algorithm that builds the MST by starting from an arbitrary vertex and growing the MST one edge at a time. It always selects the smallest edge that connects a vertex in the growing MST to a vertex outside the MST.

```
import heapq

class Graph:
    def___init_(self, vertices):
        self.V = vertices
```

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```
self.graph = [[] for _ in range(vertices)]
def addEdge(self, u, v, w):
   self.graph[u].append((v, w))
   self.graph[v].append((u, w))
def PrimMST(self):
   key = [float('inf')] * self.V
   parent = [-1] * self.V key[0]
   minHeap = [(0, 0)] inMST
   = [False] * self.V
   while minHeap:
      weight, u = heapq.heappop(minHeap)
      inMST[u] = True
      for v, w in self.graph[u]:
         if not inMST[v] and key[v] > w:
            key[v] = w
            heapq.heappush(minHeap, (key[v], v))
            parent[v] = u
   for i in range(1, self.V):
      print(f"{parent[i]} -- {i}")
```

These two algorithms, Kruskal's and Prim's, are fundamental approaches to solving the MST problem. Each algorithm has its use cases based on the structure and specific needs of the graph data. Kruskal's algorithm is more suitable for handling sparse graphs, while Prim's algorithm can be more efficient for dense graphs. Understanding the underlying principles of these algorithms is essential for effective application in practical scenarios.

7.10 Graph Coloring

Graph coloring is a methodology for assigning colors to the vertices of a graph such that no two adjacent vertices share the same color. This concept is fundamental in various practical applications and theoretical problems. An understanding of graph coloring requires familiarity with fundamental principles, algorithms used for this process, and its applications.

Consider a simple undirected graph G = (V,E), where V represents vertices and E represents edges. The goal of graph coloring is to assign a color c to each vertex v such that if $(u,v) \in E$, then $c(u) \neq c(v)$.



Chromatic Number The minimum number of colors needed to color a graph G is called its chromatic number, denoted as $\chi(G)$. Determining the chromatic number is a classical problem in graph theory and is known to be NP-hard. Various heuristic and exact algorithms have been developed to find or approximate the chromatic number for different types of graphs.

Greedy Coloring Algorithm One of the simple and widely used methods for graph coloring is the Greedy Coloring Algorithm. Despite not always producing an optimal solution, it is effective in many practical scenarios. Here is an outline of the Greedy Coloring Algorithm:

- 1. Sort the vertices in a specific order.
- 2. Assign the first color to the first vertex.
- 3. Proceed to the next vertex and assign the smallest possible color that has not been used by its adjacent vertices.
- 4. Repeat the process until all vertices are colored.

The Python implementation of the Greedy Coloring Algorithm can be illustrated as follows:

```
def greedy coloring(graph):
   # Initialize result array with -1, representing unassigned colors
   result = [-1] * len(graph)
   # Assign the first color to the first vertex
   result[0] = 0
   # Assign colors to remaining vertices
   for u in range(1, len(graph)):
      # Track colors assigned to adjacent vertices
      unavailable colors = [False] * len(graph) for
      i in graph[u]:
         if result[i] != -1:
            unavailable colors[result[i]] = True
      # Find the first available color
      color = 0
      while color < len(graph) and unavailable colors[color]:</pre>
         color += 1
      result[u] = color
   return result
```

The above implementation demonstrates the key principles of the Greedy Coloring algorithm, which uses adjacency to ensure improper coloring is avoided.



Coloring Planar Graphs A prominent result in graph coloring is the Four Color Theorem, which states that any planar graph can be colored with at most four colors. This theorem, a culmination of extensive research and computational proof, ensures that regions on a planar map can be colored using just four distinct colors without two adjacent regions sharing the same color.

Applications of Graph Coloring Graph coloring has numerous applications across various fields:

- •**Scheduling Problems:** Coloring can be utilized in timetabling and task scheduling wherein tasks are represented as vertices. An edge indicates a conflict; hence, different tasks must be assigned different time slots.
- •**Register Allocation:** In compiler optimization, graph coloring is used for register allocation by assigning variables to a limited number of CPU registers.
- •**Frequency Assignment:** In telecommunications, frequencies are assigned to cell towers to avoid interference, modeled by a graph where vertices represent towers, and edges represent potential interference.

Complementing these applications, various other algorithms like the DSATUR (Degree of Saturation) algorithm, backtracking algorithms, and evolutionary algorithms provide sophisticated means to tackle the graph coloring problem.

Each algorithm offers unique advantages, tailored efficiency, and precision in solving specific instances of the graph coloring problem, illustrating the adaptability and practical usage of this important graph theory concept.

7.11 Applications of Graphs

Graphs possess a versatile framework suitable for numerous applications in various domains, owing to their ability to model relationships among entities. Their utility spans computer science, biology, transportation, social networks, and many other fields. This section presents detailed scenarios showcasing the practical applications of graphs.

Social Networks

In social networks, graphs are employed to represent users as vertices, with edges denoting relationships between them. An adjacency list or matrix can effectively represent these relationships. Use cases in social networks include friend suggestions, community detection, and information propagation. For instance, by analyzing the graph structure, platforms can suggest new connections to users based on mutual friends.

Social networks also leverage graph traversal algorithms. For example, algorithms like BFS can identify the shortest path between two nodes, answering questions such as "How many steps connect user A to user B?" Community detection algorithms derive closely-knit



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