

## MIDTERM EXAM- ALL PROBLEMS CARRY EQUAL WEIGHT

ELECTRONIC SUBMISSION (WITH CODE) DUE NOVEMBER 11, 2020, 4 PM

This is an exam. Please make your submitted work is only attributed to you.

- (1) Demonstrate that PLA for  $d$  dimensional linearly seperable data, can be written as a linear program of the form,

$$\begin{array}{ll} \max_w & c^T w \\ \text{s.t.} & Aw \geq b. \end{array}$$

Please provide the matrix A, vector b, and vector c.

- (2) Argue that the VC dimension of convex d-gons (poylgon with d sides) is  $2d+1$ .  
(3) Exercise 3.10 (From LFD book) (page 98)  
(4) Problem 3.3 (From LFD book)  
(5) Consider the function

$$f(x_1, x_2) = e^{x_1+3x_2-0.1} + e^{x_1-3x_2-0.1} + e^{-x_1-0.1}$$

- (a) Plot the level sets of  $f(x_1, x_2) = k$  for different positive values of  $k$ .  
(b) Compute the gradient of the function.  
(c) Utilize the gradient descent algorithm to optimize the function, report the minimum, and plot the progression towards the minimum.