2.6 Logical Operations



MIPS Arithmetic Operations

| Category | Instruction | Example | | Meaning | Comments |
|------------|--------------------------------|---------|----------------|---|-------------------------------------|
| | add | add | \$s1,\$s2,\$s3 | \$s1 = \$s2 + \$s3 | Three operands; overflow detected |
| | subtract | sub | \$s1,\$s2,\$s3 | \$s1 = \$s2 - \$s3 | Three operands; overflow detected |
| | add immediate | addi | \$s1,\$s2,100 | \$s1 = \$s2 + 100 | + constant; overflow detected |
| | add unsigned | addu | \$s1,\$s2,\$s3 | \$s1 = \$s2 + \$s3 | Three operands; overflow undetected |
| | subtract unsigned | subu | \$s1,\$s2,\$s3 | \$s1 = \$s2 - \$s3 | Three operands; overflow undetected |
| | add immediate unsigned | addiu | \$s1,\$s2,100 | \$s1 = \$s2 + 100 | + constant; overflow undetected |
| | move from coprocessor register | mfc0 | \$s1,\$epc | \$s1 = \$epc | Copy Exception PC + special regs |
| Arithmetic | multiply | mult | \$s2,\$s3 | Hi, Lo = \$s2 × \$s3 | 64-bit signed product in Hi, Lo |
| | multiply unsigned | multu | \$s2,\$s3 | Hi, Lo = \$s2 × \$s3 | 64-bit unsigned product in Hi, Lo |
| | divide | div | \$s2,\$s3 | Lo = \$s2 / \$s3, Hi = \$s2 mod \$s3 | Lo = quotient, Hi = remainder |
| | divide unsigned | divu | \$s2,\$s3 | Lo = \$s2 / \$s3, Hi = \$s2 mod \$s3 | Unsigned quotient and remainder |
| | move from Hi | mfhi | \$s1 | \$s1 = Hi | Used to get copy of Hi |
| | move from Lo | mflo | \$s1 | \$s1 = Lo | Used to get copy of Lo |

2.6 MIPS logical operations

| | AND | AND | \$s1,\$s2,\$s3 | \$s1 = \$s2 & \$s3 | Three reg. operands; bit-by-bit AND |
|---------|---------------------|------|----------------|-----------------------|-------------------------------------|
| | OR | OR | \$s1,\$s2,\$s3 | \$s1 = \$s2 \$s3 | Three reg. operands; bit-by-bit OR |
| | NOR | NOR | \$s1,\$s2,\$s3 | \$s1 = ~ (\$s2 \$s3) | Three reg. operands; bit-by-bit NOR |
| Logical | AND immediate | ANDi | \$s1,\$s2,100 | \$s1 = \$s2 & 100 | Bit-by-bit AND with constant |
| | OR immediate | ORi | \$s1,\$s2,100 | \$s1 = \$s2 100 | Bit-by-bit OR with constant |
| | shift left logical | s11 | \$s1,\$s2,10 | \$s1 = \$s2 << 10 | Shift left by constant |
| | shift right logical | srl | \$s1,\$s2,10 | \$s1 = \$s2 >> 10 | Shift right by constant |
| | | | | | |

| 논리 연산 | NOT(논리부정) | | AND(논리곱) | | | OR(논리합) | | |
|-------|-----------------------------|-----|-----------------------------------|---|---|------------------------|---|---|
| 수식 | $X = A' = \bar{A} = \sim A$ | | $X = A \cdot B = A \wedge B = AB$ | | | $X = A + B = A \lor B$ | | |
| 진리표 | A | X | Α | В | X | A | В | X |
| | 0 | 0 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| | U | | 0 | 1 | 0 | 0 | 1 | 1 |
| | 1 0 | 0 | 1 | 0 | 0 | 1 | 0 | 1 |
| | | | 1 | 1 | 1 | 1 | 1 | 1 |

• A:1은 짝수다(거짓)

• B: 3 은 짝수다 (거짓)

| 논리 연산 | NOT(논리부정) | | AND(논리곱) | | | OR(논리합) | | |
|-------|-----------------------------|---|-----------------------------------|---|---|------------------------|---|---|
| 수식 | $X = A' = \bar{A} = \sim A$ | | $X = A \cdot B = A \wedge B = AB$ | | | $X = A + B = A \lor B$ | | |
| 진리표 | A | X | A | В | X | Α | В | X |
| | 0 1 | 0 | 0 | 0 | 0 | 0 | 0 | |
| | U | 1 | 0 | 1 | 0 | 0 | 1 | 1 |
| | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 1 |
| | | | 1 | 1 | 1 | 1 | 1 | 1 |

• A:1은 짝수다(거짓)

• B: 3 은 홀수다 (참)

| 논리 연산 | NOT(논리부정) | | AND(논리곱) | | | OR(논리합) | | |
|-------|-----------------------------|---|-----------------------------------|---|---|------------------------|---|---|
| 수식 | $X = A' = \bar{A} = \sim A$ | | $X = A \cdot B = A \wedge B = AB$ | | | $X = A + B = A \vee B$ | | |
| 진리표 | A | X | A | В | X | A | В | X |
| | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| | O | 1 | 0 | 1 | 0 | 0 | 1 | 1 |
| | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 1 |
| | | | 1 | 1 | 1 | 1 | 1 | 1 |

• A:1은 홀수다(참)

• B: 3 은 짝수다 (거짓)

| 논리 연산 | NOT(논리부정) | | AND(논리곱) | | | OR(논리합) | | |
|-------|-----------------------------|-----|-----------------------------------|---|---|------------------------|---|---|
| 수식 | $X = A' = \bar{A} = \sim A$ | | $X = A \cdot B = A \wedge B = AB$ | | | $X = A + B = A \lor B$ | | |
| 진리표 | A | X | A | В | X | A | В | X |
| | 0 | 0 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| | O | | 0 | 1 | 0 | 0 | 1 | 1 |
| | 1 | 0 | 1 | 0 | 0 | 1 | 0 | 1 |
| | | | 1 | 1 | 1 | 1 | 1 | 1 |

• A:1은 홀수다(참)

• B: 3 은 홀수다 (참)

bitwise logical operators

| Α | В | A AND B | A OR B | NOT A |
|-------|-------|---------|--------|-------|
| False | False | False | False | True |
| False | True | False | True | True |
| True | False | False | True | False |
| True | True | True | True | False |

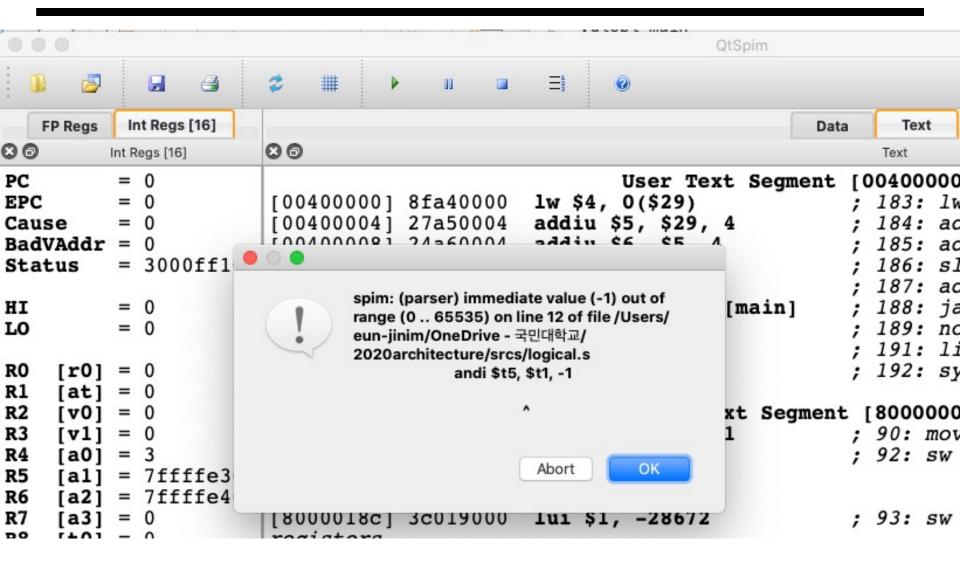
| Logical operations | C operators | Java operators | MIPS instructions |
|--------------------|-------------|----------------|-------------------|
| Shift left | << | << | sll |
| Shift right | >> | >>> | srl |
| Bit-by-bit AND | & | & | and, andi |
| Bit-by-bit OR | | | or, ori |
| Bit-by-bit NOT | ~ | ~ | nor |

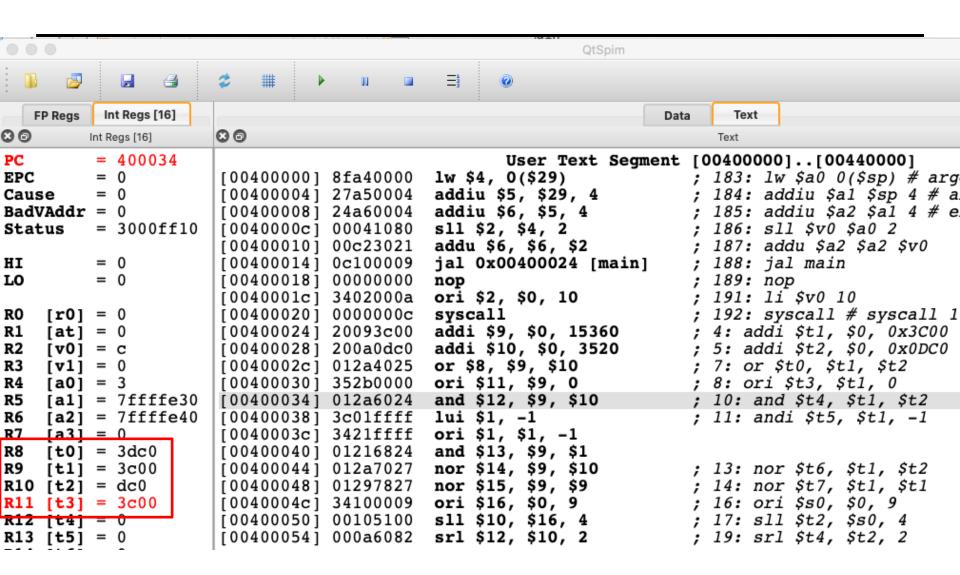
```
.text
    .globl main
    main:
        addi $t1, $0, 0x3C00
 5
        addi $t2, $0, 0x0DC0
 6
        or $t0, $t1, $t2
 8
        ori $t3, $t1, 0
9
10
        and $t4, $t1, $t2
        andi $t5, $t1, -1
11
12
        nor $t6, $t1, $t2
13
14
        nor $t7, $t1, $t1
15
        ori $s0, $0, 9
16
        sll $t2, $s0, 4
17
18
19
        srl $t4, $t2, 2
```

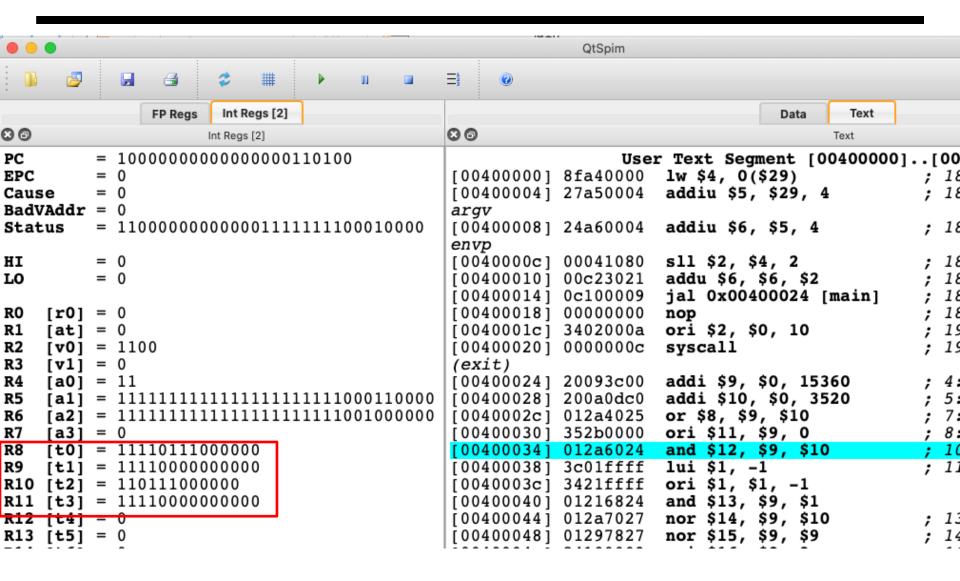
or / ori

```
$t1: 0000 0000 0000 0000 0011 1100 0000 0000<sub>two</sub>
$t2: 0000 0000 0000 0000 0000 1101 1100 0000 two
        or $t0, $t1, $t2
$t0:
      0000 0000 0000 0000 0011 1101 1100 0000<sub>two</sub>
        ori $t3, $t1, 0
                                             A \text{ or } O = A
      0000 0000 0000 0000 0011 1100 0000 0000
      0000 0000 0000 0000 0000 0000 0000 0000
     0000 0000 0000 0000 0011 1100 0000 0000
$t3:
```

당분간 out of range error는 무시하고 실행하세요.



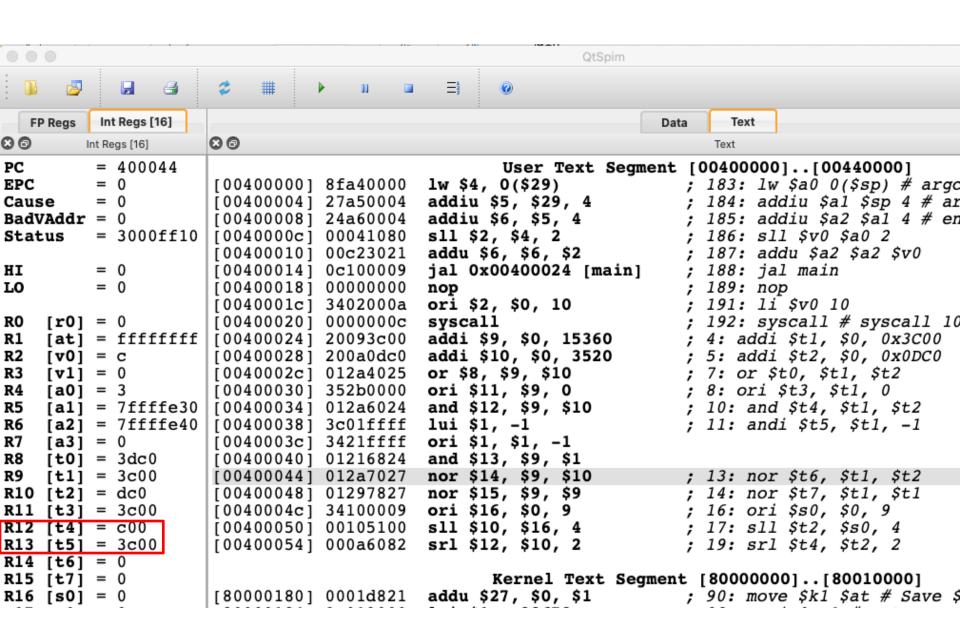


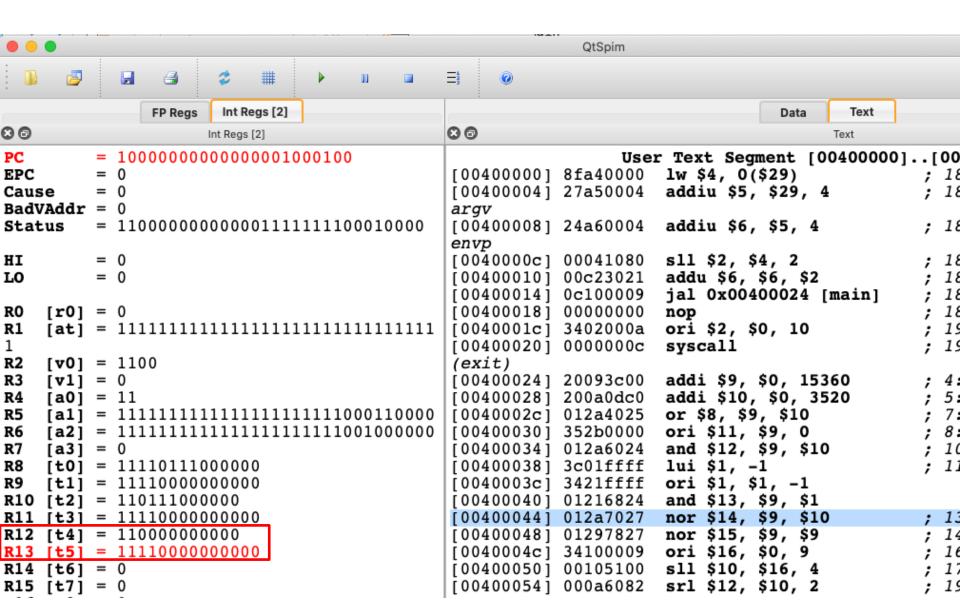


```
.text
    .globl main
    main:
 3
        addi $t1, $0, 0x3C00
 4
 5
        addi $t2, $0, 0x0DC0
 6
        or $t0, $t1, $t2
 8
        ori $t3, $t1, 0
9
        and $t4, $t1, $t2
10
11
        andi $t5, $t1, -1
12
        nor $t6, $t1, $t2
13
14
         nor $t7, $t1, $t1
15
        ori $s0, $0, 9
16
        sll $t2, $s0, 4
17
18
19
         srl $t4, $t2, 2
```

and / andi

```
$t1:
      0000 0000 0000 0000 0000 1101 1100 0000<sub>two</sub>
$t2:
      and $t4, $t1, $t2
$t4:
    andi $t5, $t1, -1
                                    A and 1 = A
      0000 0000 0000 0000 0011 1100 0000 0000
      1111 1111 1111 1111 1111 1111 1111 1111
$t5:
      0000 0000 0000 0000 0011 1100 0000 0000
```

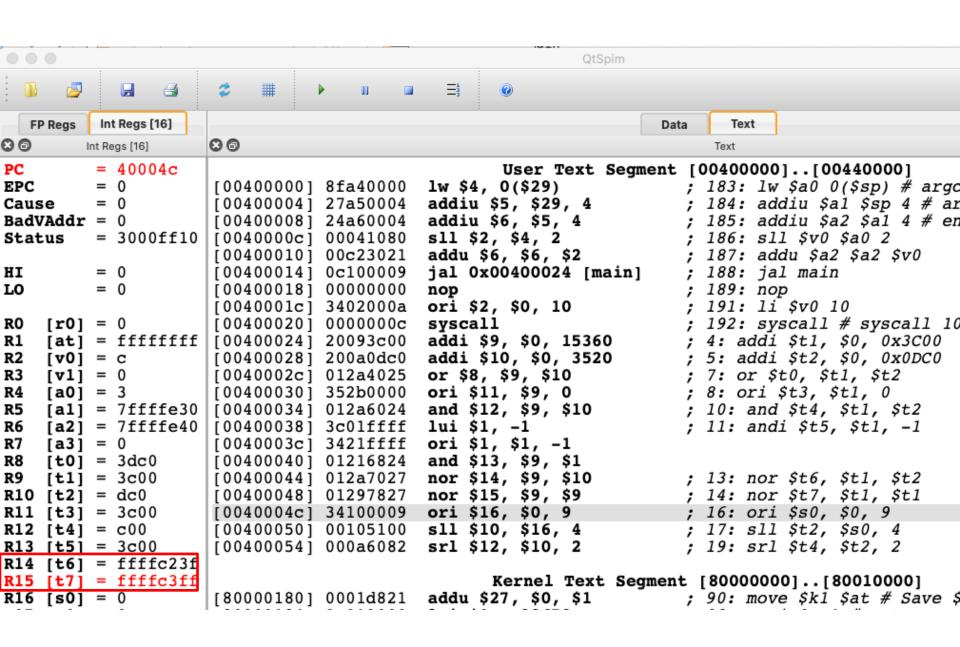


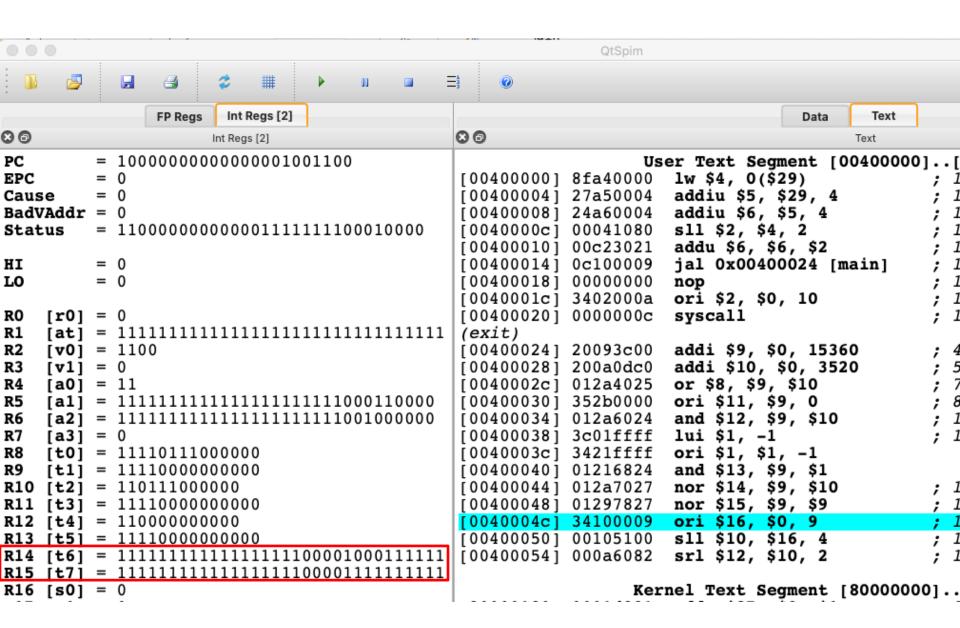


```
.text
    .globl main
    main:
 3
        addi $t1, $0, 0x3C00
 4
        addi $t2, $0, 0x0DC0
 5
 6
        or $t0, $t1, $t2
8
        ori $t3, $t1, 0
9
10
        and $t4, $t1, $t2
        andi $t5, $t1, -1
11
12
        nor $t6, $t1, $t2
13
         nor $t7, $t1, $t1
14
15
        ori $s0, $0, 9
16
         sll $t2, $s0, 4
17
18
19
         srl $t4, $t2, 2
```

nor = not or

```
$t1: 0000 0000 0000 0001 1100 0000 0000
$t2:
    0000 0000 0000 0000 0000 1101 1100 0000
     nor $t6, $t1, $t2
$t6:
    1111 1111 1111 1111 1100 0010 0011 1111
                               not(A) = not(A \text{ or } A) = A \text{ nor } A
                                   = not (A or 0) = A nor 0
     nor $t7, $t1, $t1 # $t7 = ~$t1
     0000 0000 0000 0000 0011 1100 0000 0000
     0000 0000 0000 0000 0011 1100 0000 0000
```



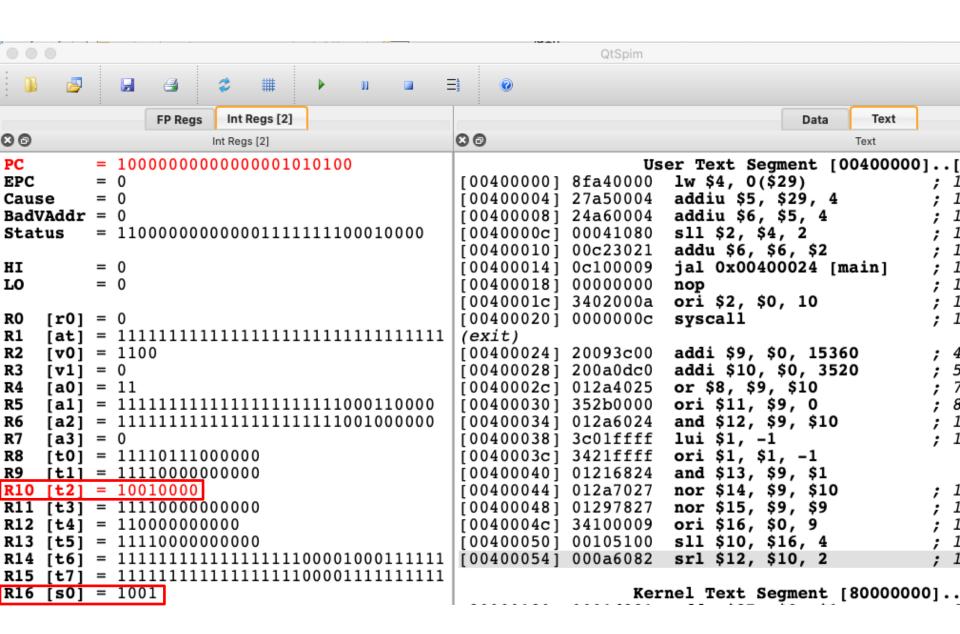


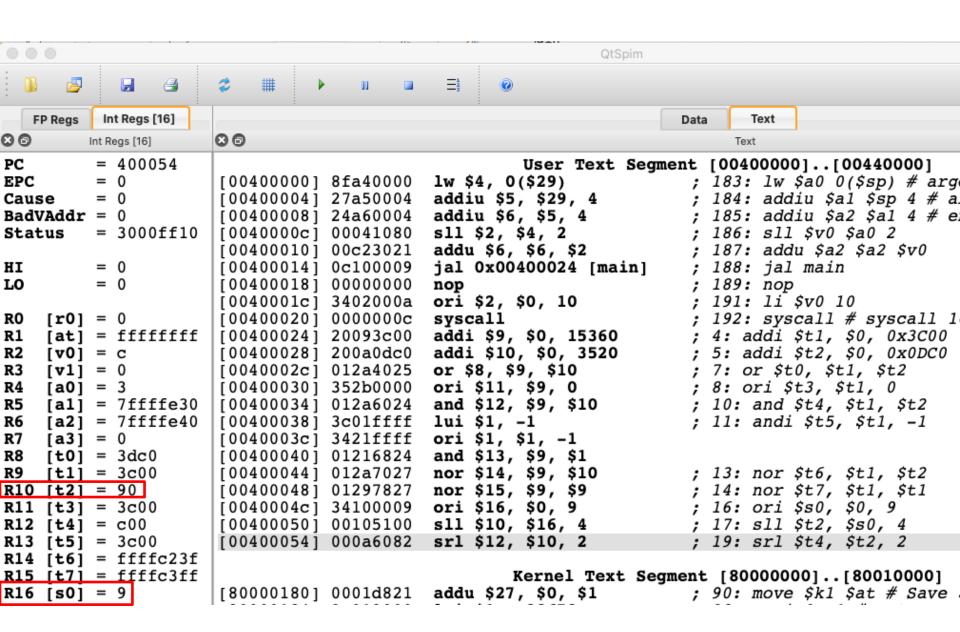
```
.text
    .globl main
    main:
 3
        addi $t1, $0, 0x3C00
 4
 5
        addi $t2, $0, 0x0DC0
 6
        or $t0, $t1, $t2
8
        ori $t3, $t1, 0
9
        and $t4, $t1, $t2
10
        andi $t5, $t1, -1
11
12
        nor $t6, $t1, $t2
13
14
        nor $t7, $t1, $t1
15
        ori $s0, $0, 9
16
        sll $t2, $s0, 4
17
18
19
        srl $t4, $t2, 2
```

sll: shift left logical

\$t2 : 0000 0000 0000 0000 0000 0000 1001 0000_{two} = 144_{ten}

왼쪽으로 i bits shift 하는 것은 2ⁱ 만큼 곱하는 것과 같은데 연산 속도는 곱셈보다 빠르다.





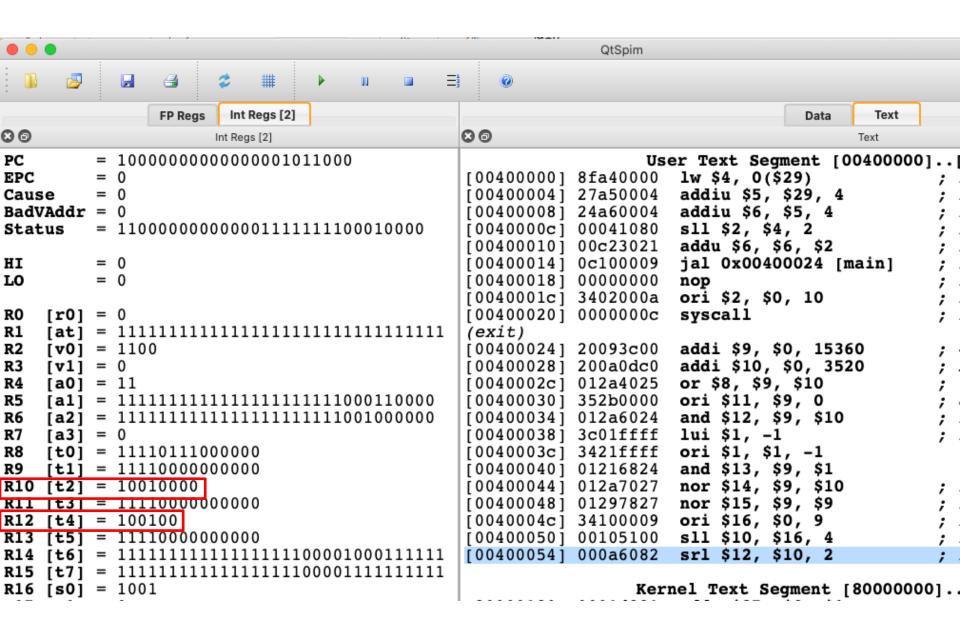
```
.text
    .globl main
    main:
 3
        addi $t1, $0, 0x3C00
 4
 5
        addi $t2, $0, 0x0DC0
 6
        or $t0, $t1, $t2
8
        ori $t3, $t1, 0
9
10
        and $t4, $t1, $t2
        andi $t5, $t1, -1
11
12
        nor $t6, $t1, $t2
13
14
        nor $t7, $t1, $t1
15
        ori $s0, $0, 9
16
        sll $t2, $s0, 4
17
18
19
        srl $t4, $t2, 2
```

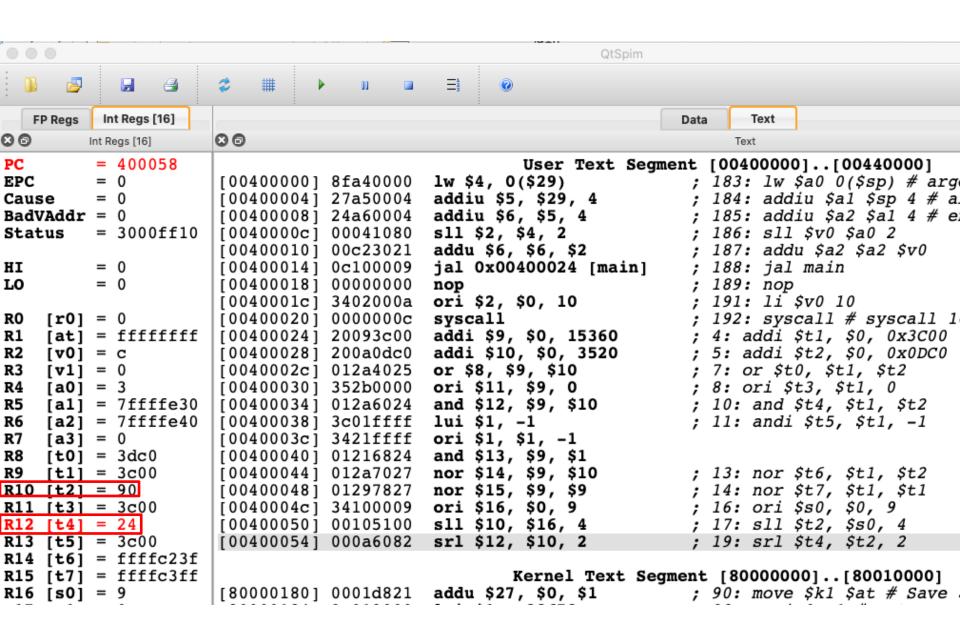
srl: shift right logical

\$t2:0000 0000 0000 0000 0000 0000 1001 0000 = 0x90 srl \$t4, \$t2, 2

\$t4: 0000 0000 0000 0000 0000 0000 0010 0100 = 0x24

오른쪽으로 i bits shift 하는 것은 2ⁱ 로 나누는 것과 같은데 연산 속도는 나눗셈보다 빠르다.





| | AND | AND | \$s1,\$s2,\$s3 | \$s1 = \$s2 & \$s3 | Three reg. operands; bit-by-bit AND |
|---------|---------------------|------|----------------|-----------------------|-------------------------------------|
| | OR | OR | \$s1,\$s2,\$s3 | \$s1 = \$s2 \$s3 | Three reg. operands; bit-by-bit OR |
| | NOR | NOR | \$s1,\$s2,\$s3 | \$s1 = ~ (\$s2 \$s3) | Three reg. operands; bit-by-bit NOR |
| Logical | AND immediate | ANDi | \$s1,\$s2,100 | \$s1 = \$s2 & 100 | Bit-by-bit AND with constant |
| | OR immediate | ORi | \$s1,\$s2,100 | \$s1 = \$s2 100 | Bit-by-bit OR with constant |
| | shift left logical | s11 | \$s1,\$s2,10 | \$s1 = \$s2 << 10 | Shift left by constant |
| | shift right logical | srl | \$s1,\$s2,10 | \$s1 = \$s2 >> 10 | Shift right by constant |