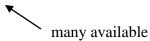
Orbits in Three Dimensions

Previously, we considered everything in 2D

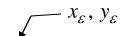
Now, try 3D problems

some background necessary to define an orbit in space

First, define coordinate systems (3D) to help



Two basic types for us to use:



(1) <u>Ecliptic System</u> – fundamental plane is the plane of the ⊕'s orbit about the Sun (latitude, longitude)

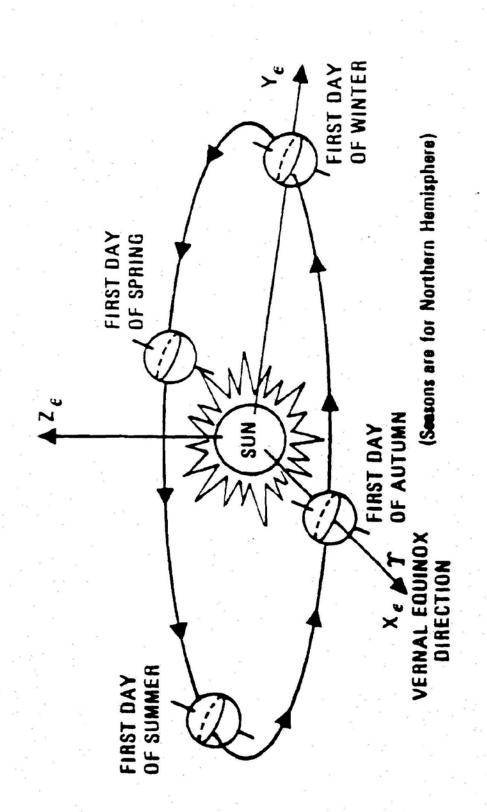
$$\int x, y$$

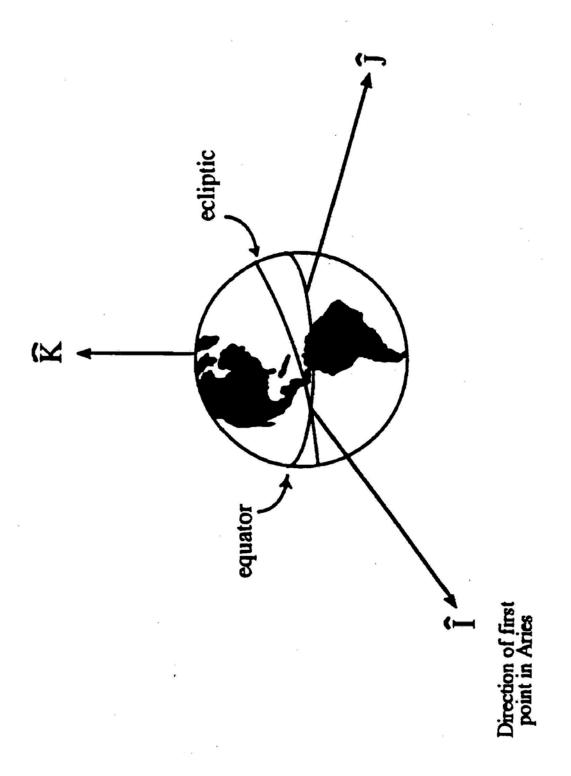
(2) <u>Equatorial System</u> – Fundamental plane is the plane of the body's equator (right ascension, declination)

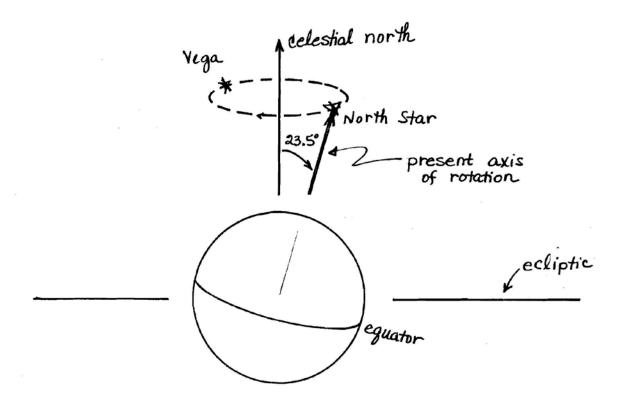
Obliquity of ecliptic (ε) –

To effectively use a coordinate system, reference directions must be known and understood; we need a <u>fixed</u> reference direction in the fundamental plane from which measurements are made









"precession of the equinoxes" -

Caused by perturbing forces on its attitude, i.e., \odot and \P gravity forces

These apply a precessing motion (same as the precessing motion of a spinning top or a torque-free rigid body)

Known as early as 2nd century BC to Greek astronomer Hipparchus

Time for complete precession is 26,000 years

Consequence

- 1. Cataloging of celestial objects must refer to a specific date \rightarrow epoch \rightarrow currently 0.0 hrs
- 2. We will assume Υ fixed; reasonable over the relatively short intervals of interest

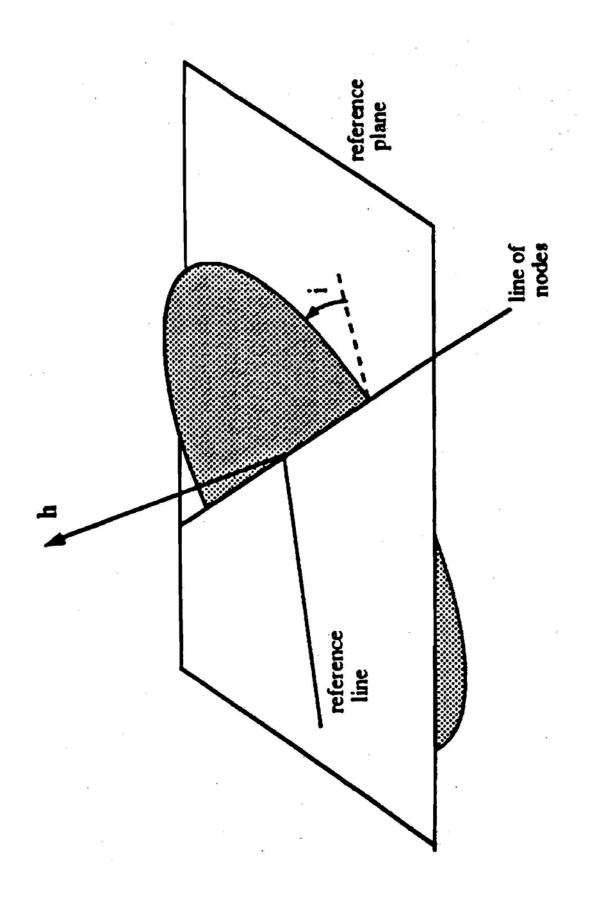


Reference System

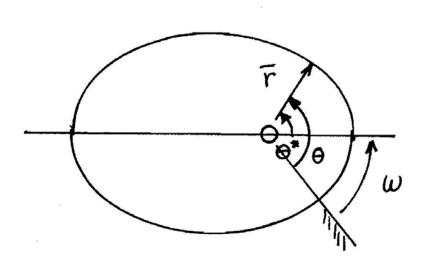
- \hat{x} direction of the vernal equinox
- \hat{z} normal to fundamental plane; + north $\hat{y} = \hat{z} \times \hat{x}$

So, to locate s/c in space:

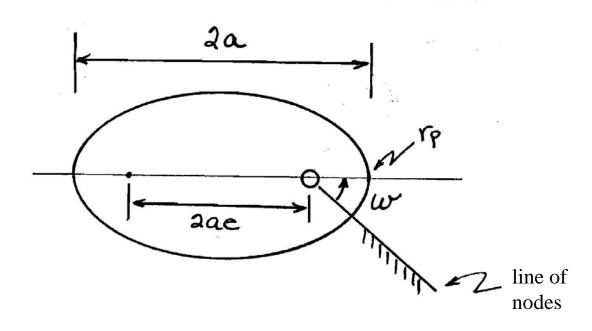
- locate s/c in orbit (θ^*, E, M) (1)
- identify orientation of orbit within orbit plane (ω); (2) size and shape of orbit (a, e)
- (3) identify orientation of orbit plane in space (Ω , i)

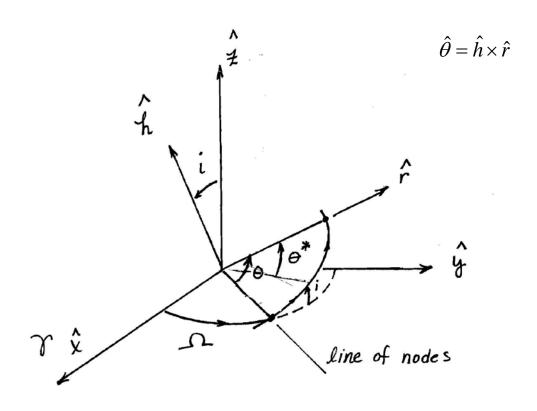


(1) Locate s/c in orbit: time \leftarrow



(2) Within orbit plane: orbit size and shape orbit orientation within plane





$$\omega$$
 $\bigg\{$

$$\Omega + \omega = \varpi$$
 $\left\{ \right.$

$$\varpi + \theta^* = L$$
 $\bigg\{$

3-1-3 (body-two) Euler sequence transformation matrix



ω: argument of periapsis

ῶ = Ω + ω : longitude of periapsisf : true anomaly

 $L = \widetilde{\omega} + f$: true longitude

