

Contents

- [Problem 4](#)
- [Problem 5](#)

```
clear
close all
clc
```

Problem 4

```
% Time delay [s]
h      = 0.25;

% Get non-linear equation roots
w      = fzero(@(w) tan(w*h) + w, 10);

% Verify non-linear equation is near 0.
fprintf('For a time delay of h = %.2f, tan(wh) + w = %.4f if w = %.4f \n'...
        ,h, tan(w*h) + w, w)

% Period of periodic solution
T      = 2*pi/w;

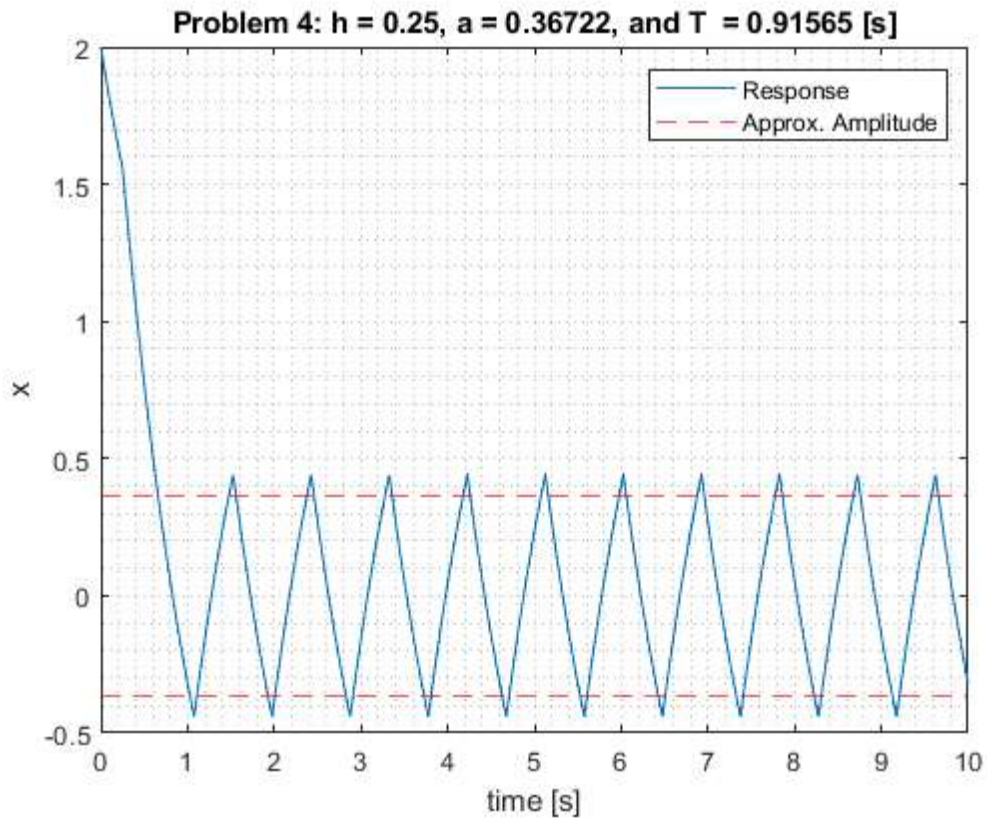
% Amplitude of periodic solution
a      = -8*cos(w*h)/pi;

fprintf(['If h = %.2f, the system has an approximate period of %.3f seconds with an '...
        'amplitude of %.3f \n'],h,T,a)

% Run Model
simout  = sim("Model.slx");

% Plot
figure
plot(simout.tout, simout.logout{1}.Values.Data)
hold on
yline([a -a], '--r')
grid minor
xlabel('time [s]')
legend('Response','Approx. Amplitude')
ylabel('x')
title_str = ['Problem 4: h = ', num2str(h), ', a = ', num2str(a),...
            ', and T = ', num2str(T), ' [s]'];
title(title_str)
```

For a time delay of $h = 0.25$, $\tan(wh) + w = 0.0000$ if $w = 6.8620$
If $h = 0.25$, the system has an approximate period of 0.916 seconds with an amplitude of 0.367



Problem 5

```
% PID Gains
Kp      = 1;
Kd      = 2;

% System Transfer Function: Ki * G
G       = tf([1],[1 Kd Kp 0]);

% Root Locus plot
figure
rlocusplot(G)
[poles,Ki] = rlocus(G,0:.001:5);

% Locate Largest Ki such that poles are in RHP
Ki_max   = max(Ki(max(real(poles)) < 0));

fprintf(['The largest Ki >=0, for which the closed loop system '...
        'is asymptotically stable about q = 0 is %.3f. \n'], Ki_max)

% Check poles of Closed Loop System
disp('The poles of the closed loop system with the max Ki are: ')
CL_poles = pole(feedback(Ki_max*G,1))
```

The largest $K_i \geq 0$, for which the closed loop system is asymptotically stable about $q = 0$ is 1.999.
The poles of the closed loop system with the max K_i are:

CL_poles =

```
-1.9998 + 0.0000i
-0.0001 + 0.9998i
```

-0.0001 - 0.9998i

